Machine learning for Dynamic Social Network Analysis

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IIT HYDERABAD, DECEMBER 2017

Interconnected World



Many discrete events in continuous time



Qmee, 2013

Variety of processes behind these events



Example I: Idea adoption/viral marketing





They can have an impact in the off-line world



Click and elect: how fake news helped 5 Donald Trump win a real election

Example II: Information creation & curation



Example III: Learning trajectories



Detailed event traces





Warren is in the house.



Manuel Gomez Rodriguez updated his cover photo. April 17 at 1:14pm · G



Pique-Longue, French Pyrenees Easter 2017

The availability of event traces boosts a new generation of data-driven models and algorithms



t Like	Comment	A Share	
O Mehrdad Farajtabar, Lili Yavis-Hound and 24 others			
Rob Like	er Tab Pu 😂wow! • Reply • April 17 at	1:32pm	

Previously: discrete-time models & algorithms



Outline of the Seminar

REPRESENTATION: TEMPORAL POINT

PROCESSE\$. Intensity function

- 2. Basic building blocks
- 3. Superposition
- 4. Marks and SDEs with jumps

APPLICATIONS: MODELS

- 1. Information propagation
- 2. Opinion dynamics
- 3. Information reliability
- 4. Knowledge acquisition

APPLICATIONS:

- GOMTR@hce maximization
- 2. Activity shaping
- 3. When to post
- 4. When to fact check

This lecture

Representation: Temporal Point Processes

Intensity function Basic building blocks Superposition Marks and SDEs with jumps

Temporal point processes



Model time as a random variable





Likelihood of a $f^*(t_1) f^*(t_2) f^*(t_3) f^*(t) S^*(T)$ timeline:

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Problems of density parametrization (I)



It is difficult for model design and interpretability:

- 1. Densities need to integrate to 1 (i.e., partition function)
- 2. Difficult to combine timelines

Problems of density parametrization (II)

Difficult to combine timelines:



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Intensity function

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Observation $\lambda^*(t)$ It is a rate = # of events / unit of time

Advantages of intensity parametrization (I)



Suitable for model design and interpretable: 1. Intensities only need to be nonnegative

2. Easy to combine timelines

Advantages of intensity parametrization (II)

Easy to combine timeline:



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Relation between f*, F*, S*, λ^*



Representation: Temporal Point Processes

Intensity function
 Basic building blocks

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Poisson process



Intensity of a Poisson process

$$\lambda^*(t) = \mu$$

Observations

•

- 1. Intensity independent of history
- 2. Uniformly random occurrence
- 3. Time interval follows exponential distribution ²¹

Fitting a Poisson from (historical) timeline



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Sampling from a Poisson process



We would like to sample $t \sim \mu \exp(-\mu(t-t_3))$ We sample using inversion sampling: $F_t(t) = 1 - \exp(-\mu(t-t_3))$ $rightarrow t \sim -\frac{1}{\mu} \log(1-u) + t_3$ $\mathbb{P}(F_t^{-1}(u) \leq t) = \mathbb{P}(u \leq F_t(t)) = F_t(t)$ $F_u(u) = u$

Inhomogeneous Poisson process



Intensity of an inhomogeneous Poisson process

$$\lambda^*(t) = g(t) \ge 0$$

Observations

•

1. Intensity independent of history

Fitting an inhomogeneous Poisson



Nonparametric inhomogeneous Poisson process



Sampling from an inhomogeneous Poisson



Thinning procedure (similar to rejection sampling): 1. Sample t from Poisson process with inte μ ity

$$Uniform(0,1)$$

$$\downarrow$$

$$t \sim -\frac{1}{\mu} \log(1-u) + t_3$$
Inversion sampling
Inversion
Solution
Inversion

Terminating (or survival) process



Intensity of a terminating (or survival) process

$$\lambda^*(t) = g^*(t)(1 - N(t)) \ge 0$$

Observations

•

1. Limited number of occurrences Try sampling and fitting and fitting

Self-exciting (or Hawkes) process

Observations

- 1. Clustered (or bursty) occurrence of events
- 2. Intensity is stochastic and history dependent

Fitting a Hawkes process from a recorded timeline

Sampling from a Hawkes process

Thinning procedure (similar to rejection sampling): 1. Sample t from Poisson process with inte μ_3^i ty

$$Uniform(0,1)$$

$$\downarrow$$

$$t \sim -\frac{1}{\mu_3} \log(1-u) + t_3$$
Inversion sampling
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Summary

Building blocks to represent different dynamic processes: Poisson processes: $\lambda^*(t) = \lambda$ Inho We know how to fit them and how to sample from them Term IV(t) ι (11)

Self-exciting point processes:

$$\lambda^*(t) = \mu + \alpha \sum_{t_i \in \mathcal{H}(t)} \kappa_\omega(t - t_i)$$

Representation: Temporal Point Processes

Intensity function
 Basic building blocks
 Superposition
 Marks and SDEs with jumps

Superposition of processes

$$t = \min(\tau_{i}, \tau_{1}, \tau_{2}, \tau_{3}) \implies \lambda^{*}(t) = \mu + \alpha \sum_{t_{i} \in \mathcal{H}(t)} \kappa_{\omega}(t - t_{i})$$

Mutually exciting process

Clustered occurrence affected by neighbors

$$\lambda^{*}(t) = \mu + \alpha \sum_{t_{i} \in \mathcal{H}_{b}(t)} \kappa_{\omega}(t - t_{i}) + \beta \sum_{t_{i} \in \mathcal{H}_{c}(t)} \kappa_{\omega}(t - t_{i})$$

$$(35)$$

Mutually exciting terminating process

Clustered occurrence affected by neighbors

$$\lambda^*(t) = (1 - N(t)) \left(g(t) + \beta \sum_{t_i \in \mathcal{H}_c(t)} \kappa_\omega(t - t_i) \right)$$

Representation: Temporal Point Processes

Intensity function
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 Superposition

4. Marks and SDEs with jumps

Marked temporal point processes

Marked temporal point process:

A random process whose realization consists of discrete marked events localized in time

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Independent identically distributed marks

Distribution for the marks:

 $x^*(t_i) \sim p(x)$

Observations

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- 1. Marks independent of the temporal dynamics
- 2. Independent identically distributed (I.I.D.)

Dependent marks: SDEs with jumps

2. Defined for all values of t

Dependent marks: distribution + SDE with jumps

Distribution for the marks:

$$x^{*}(t_{i}) \sim p(x^{*}|x(t)) \Rightarrow dx(t) = f(x(t), t)dt + h(x(t), t)dN(t)$$
Observations
$$f(x(t), t)dt + h(x(t), t)dN(t)$$
Drift Event
$$f(x(t), t)dN(t)$$

2. Distribution represents additional source of uncertainty

Mutually exciting + marks

Marks affected by neighbors

$$dx(t) = f(x(t), t)dt + g(x(t), t)dM(t)$$

Drift Neighbor

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Next lecture