Novel Light Weight Compressed Data Aggregation Using Sparse Measurements for IoT Networks

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Abstract

Optimal data aggregation aimed at maximizing IoT network lifetime by minimizing constrained on-board resource utilization continues to be a challenging task. The existing data aggregation methods have proven that compressed sensing is promising for data aggregation. However, they compromise either on energy efficiency or recovery fidelity and require complex on-node computations. In this paper, we propose a novel Light Weight Compressed Data Aggregation (LWCDA) algorithm that randomly divides the entire network into nonoverlapping clusters for data aggregation. The random non-overlapping clustering offers two important advantages: 1) energy efficiency, as each node has to send its measurement only to its cluster head, 2) highly sparse measurement matrix, which leads to a practically implementable framework with low complexity. We analyze the properties of our measurement matrix using restricted isometry property, the associated coherence and phase transition. Through extensive simulations on practical data, we show that the measurement matrix can reconstruct data with high fidelity. Further, we demonstrate that the LWCDA algorithm reduces transmission cost significantly against baseline approaches,

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implying thereby the enhancement of the network lifetime.Keywords: Compressed sensing, data aggregation, Internet of Things, network lifetime.

1 1. Introduction

Internet of Things (IoT) is a communication paradigm that benefits society in many ways by providing vast and diverse applications [1]. In IoT, Wireless 3 Sensor Network (WSN) takes an active part in the integration of physical world information. WSN encompasses huge number of tiny devices called sensor nodes 5 which are deployed in the sensing area of interest to measure the data. IoT enables access to a wide variety of WSNs for providing a plethora of services 7 to the citizens [1]. In most of the IoT applications such as remote sensing and 8 environmental monitoring, seamless data aggregation from the sensor nodes is 9 the fundamental requirement for data processing (data analytics) to facilitate 10 the user with a useful interface and ubiquitous access to the network data. 11

The sensor nodes used in IoT application deployments are typically, inex-12 pensive, unterhered and are powered through batteries [2]. However, relying 13 on battery power limits the lifetime of the nodes. Further, regular recharg-14 ing or replacement of batteries leads to additional cost and is a laborious task 15 [3]. Thus, the network lifetime is a critical concern for data aggregation in IoT 16 networks. Wireless transmission consumes significant amount of energy during 17 the data aggregation [4]. Indeed, reducing the number of packet transmissions 18 and minimizing routing path for data aggregation in the network can improve 19 the network lifetime. Several approaches have been proposed to address this 20 problem [5]. 21

Compressed Sensing (CS) [6] is a signal processing technique that has been proven to be very promising for data aggregation [7]. CS provides a new perspective for data aggregation in IoT networks enabling the compression and route minimization jointly for energy efficiency over the network [8]-[11]. Most of the CS aided data aggregation techniques use either dense [8]-[11] or sparse

random measurements [12]-[15]. These methods have proposed the encoding by 27 utilizing the structural properties of the measurement matrix. In dense ran-28 dom measurements based data aggregation techniques, it is assumed that the 29 individual columns of the measurement matrix are generated at the respective 30 nodes and compute the corresponding measurement [8]-[11]. The sparse random 31 measurements based data aggregation techniques computes the measurements 32 by collecting the data from the interested nodes for each measurement, while 33 assuming that the sparse measurement matrix is stored at each node [12]-[15]. 34 These approaches [8]-[15] aggregate the measurements from all the nodes by 35 minimizing the routing path to reduce the energy consumption in data aggre-36 gation. 37

Most of the existing CS aided data aggregation approaches do not consider the feasibility of hardware implementation [8]-[15]. The bottleneck for hardware 39 implementation of the CS aided data aggregation techniques is in the encoding 40 process at IoT nodes that are severely resource constrained. The size of the 41 measurement matrix depends on sparsity of the sensing data and the number 42 of nodes deployed in the network [7]. As IoT nodes are resource constrained 43 devices, for sparse random measurements based data aggregation techniques, 44 storage issues can crop up in large-scale network applications. In case of dense 45 random measurements, the dependency of column size on sensing data spar-46 sity poses multiple constraints in real-time implementation for the applications 47 where data to be sensed has low sparsity [16]. In contrast, the measurement 48 matrix content can be combined enroute to the sink instead of generating in-49 dividual columns or storing the matrix while aggregating the data from the 50 nodes using CS. This class of methods is called as routing measurements based 51 data aggregation approaches. Some existing methods in the literature [17]-[19] 52 have investigated data aggregation using routing measurements. However, these 53 methods compromise either on recovery fidelity (due to poor coherence) [18] or 54 energy efficiency (due to higher number of transmissions) [17] [19]. 55

⁵⁶ On the other-hand some existing approaches in the literature [2, 20] proposed ⁵⁷ data aggregation methods by using dense random projections [8] for optimizing

the energy consumption [2] and recovery fidelity [20]. However, these meth-58 ods do not consider the feasibility of real-time implementation. Further, the 59 proposed method in [20] does not consider the energy optimization during the 60 data aggregation while only concentrating on recovery. Recently, in [21], the au-61 thors proposed a data aggregation method by utilizing the short and long range 62 communication resources for achieving energy efficiency. However, in this work, 63 most of the nodes will be required to send their data to multiple aggregators 64 (hubs) leading to energy inefficiency in data aggregation for large-scale network applications. 66

Designing a low complexity CS based data aggregation technique that mini-67 mizes total energy consumption as well as guarantees the reconstruction is still 68 a challenging problem. To address this problem, in this article, we propose a 69 data aggregation method called "Light Weight Compressed Data Aggregation 70 (LWCDA)", which is light-weight (low complexity), energy efficient and pro-71 vides good recovery fidelity. In contrast to some existing approaches [17]-[19], 72 we utilize clustering for data aggregation which is proven to be promising for 73 energy efficient routing [15] [22]. In addition, the aggregated data from cluster 74 heads is collected using a minimum spanning tree to minimize energy consump-75 tion. In the proposed algorithm, each node measures a data sample followed 76 by generating a random value from a Bernoulli distribution for computing the 77 measurement. The cluster heads receive the measurements from their descen-78 dants, process them to compute the final measurement before transporting it to 79 the sink. We find that the measurement matrix constructed from our algorithm 80 is highly sparse and possesses properties to guarantee the recovery of data such 81 as high incoherence, good recovery region and satisfy the Restricted Isometry 82 Property (RIP) when combined with some popular bases. 83

⁸⁴ The contributions of this article are summarized as follows:

- Low complexity CS aided data aggregation technique that constructs a
 sparse measurement matrix from the network.
- 2. Performance evaluation of the measurement matrix with respect to RIP,

- so coherence and phase transition.
- 3. Comparative analysis of the algorithm in terms of reconstruction error
 and transmission cost using real data sets.
- 4. A practical implementation using IITH Motes [23] to demonstrate hardware feasibility of the proposed LWCDA algorithm.

The paper is organized as follows: Section II explains the basics of compressed sensing in IoT networks. Section III describes the proposed LWCDA data aggregation method. Section IV evaluates the RIP and coherence of the proposed measurement matrix and presents the phase transition analysis. Section V describes the hardware implementation performed and simulation results of LWCDA method are described in Section VI. Section VII concludes the paper.

99 2. Related work

100 2.1. Compressed Sensing for IoT Networks

For a given N dimensional signal (hereafter data and signal are used in-101 terchangeably) that can be sparsely represented using a basis, CS promises 102 to deliver a full recovery of the signal with high probability from far fewer 103 samples [24]. Let $X = [x_1, x_2, x_3, \dots, x_N]^T \in \mathbb{R}^N$ be sparsely represented in 104 a basis (e.g., Discrete Cosine Transform (DCT), Discrete Fourier Transform 105 (DFT), Discrete Wavelets Transform (DWT), etc.) $\Psi = [\psi_1, \psi_2, \dots, \psi_N] \in$ 106 $\mathbb{R}^{N \times N}$ with k large coefficients (k-sparse), where $k \ll N$, i.e., $X = \Psi \theta$, $\theta =$ 107 $[\psi_1^T X, \psi_2^T X, \dots, \psi_N^T X] \in \mathbb{R}^N$ and $\|\theta\|_0 \leq k$. The CS theory computes the com-108 pressed *M*-dimensional vector. 109

$$Y = \Phi X,\tag{1}$$

where $Y \in \mathbb{R}^M$ is the measurement vector and M is the number of measurements and M < N which influences reconstruction of the signal. It has been shown that the number of random measurements required for successful reconstruction of a k-sparse signal is $M = \mathcal{O}(k \log N)$ [25]. The matrix $\Phi = [\varphi_1^T, \varphi_2^T, \dots, \varphi_M^T]^T \in \mathbb{R}^{M \times N} \text{ is called the measurement matrix. The prob$ lem here is to reconstruct X from Y, which is under-determined and can haveinfinitely many solutions. CS theory shows that the problem of recovering X $from its linear measurements can be posed as a <math>l_0$ -minimization problem as shown in (2) and it is computationally intractable. A family of greedy algorithms has been proposed in [26] and [27] to solve the l_0 -minimization problem.

$$\min_{\theta} \|\theta\|_0 \text{ subject to } \Phi\Psi\theta = Y.$$
(2)

The most prevalent decoding technique to solve the problem in (2) is l_1 minimization, which is a convex optimization problem [28] and hence, computationally tractable [29],

$$\min_{\theta} \|\theta\|_1 \text{ subject to } \Phi \Psi \theta = Y.$$
(3)

From the solution θ obtained using l_0 or l_1 -minimization, X can be reconstructed as,

$$\widehat{X} = \Psi \theta. \tag{4}$$

The CS matrix $A = \Phi \Psi$ plays a crucial role in the recovery of the N dimensional original signal X. In [30], it is shown that the CS matrix A should satisfy the property known as RIP for successful recovery of X using l_1 minimization. A matrix $A \in \mathbb{R}^{M \times N}$ is said to satisfy the RIP of order k with constant $\delta_k \in (0, 1)$ if

$$(1 - \delta_k) \|u\|_2^2 \le \|Au\|_2^2 \le (1 + \delta_k) \|u\|_2^2, \forall u \in \Sigma_k,$$
(5)

¹³⁰ where u is a k-sparse vector and Σ_k is set of all k-sparse vectors.

On the other hand, if X can be sparsely represented in Ψ domain, then to achieve successful recovery, the theory of CS requires low mutual coherence between the columns of the CS matrix $A = \Phi \Psi$. The mutual coherence of the CS matrix can be defined as

$$\mu(A) = \max_{1 \le p \ne q \le N} |\langle a_p, a_q \rangle|, \qquad (6)$$

use where a_p and a_q are normalized columns of A.

136 2.2. Literature Review

In this section we discuss the contributions of the relevant literature. Most of the CS aided data aggregation techniques can be classified into three classes, dense random measurements [8]-[11], sparse random measurements [12]-[15] and routing measurements [17]-[19] based data aggregation methods.

Dense random measurements based methods [8]-[11] achieve CS aided data 141 aggregation by considering individual column generation of the measurement 142 matrix at node level using pseudo-random sequences. These methods aggregate 143 the measurements from all the nodes by minimizing routing path to achieve 144 energy efficiency. The size of the measurement matrix depends on the number 145 of nodes and sparsity of the data. IoT nodes are constrained devices possessing 146 minimal on-board resources (in terms of physical memory, processing capability, 147 internal memory, energy). Therefore, generating individual columns of the mea-148 surement matrix at a node in case of a large-scale network application where 149 sensing data sparsity is low is computationally intensive and poses multiple 150 constraints in real-time implementation. 151

Wang et al. [12] showed that sparse random measurements (projections) re-152 duce communication cost per sensor node for data aggregation. In [13]-[15], 153 data aggregation techniques have been proposed to achieve energy efficiency 154 for IoT networks by using the sparse random measurements [12]. These algo-155 rithms find the optimal route to collect data from the interested nodes for each 156 measurement, while assuming that the sparse measurement matrix is stored at 157 each node. Since the measurement matrix depends on the network size, storage 158 issues can crop-up for large-scale networks. In other words, commercially avail-159 able nodes that have minimal on-board resources may not be able to support 160 the storage large measurement matrices. 161

In contrast to dense and sparse random measurements, the routing measurements ments based data aggregation methods aggregate the measured data from the nodes by computing measurements on the fly enroute to the sink [17]-[19]. In [17], the routing paths are iteratively built through a greedy choice to minimize the coherence of the CS matrix and energy required for data aggregation.

However, building of routing paths in an iterative manner is computationally 167 intensive and requires more transmissions rendering the process highly energy 168 inefficient. In [18], the algorithm picks up a portion of the nodes randomly 169 from the network to generate measurements by utilizing shortest path routing. 170 However, such an approach does not achieve good performance with respect to 171 coherence. In [19], the authors showed that data aggregation from fixed length 172 random walks starting at randomly located nodes can reconstruct the data us-173 ing CS. However, recovery performance of the method depends on the length of 174 the random walks. An increase in the length of the walk increases the number 175 of transmissions which in turns data aggregation to be energy inefficient. 176

177 2.3. Problem Statement

In most of the IoT applications, seamless data aggregation from sensor nodes 178 is the fundamental requirement for data processing (data analytics) and facilitat-179 ing the user with useful interface and ubiquitous access to the network data[1]. 180 Typically, the sensor nodes used in IoT application deployments such as re-181 mote sensing and monitoring are resource constrained (e.g., battery powered 182 and low-end computational resources). CS has been proved to be very promis-183 ing for data aggregation in IoT networks [6, 7, 21]. However, most of the CS 184 based data aggregation algorithms proposed in the literature do not address 185 the aspects of low complexity, energy efficiency and recovery fidelity jointly 186 which is an important requirement as sensor nodes are resource constrained. 18 The approaches proposed based on dense random measurements [8]-[11] as well 188 as sparse random measurements [12]-[15] are energy efficient but not real-time 189 implementable. On the other hand, the approaches proposed in [17]-[18] are 190 light weight, however, they are either energy inefficient or do not achieve good 191 performance in terms of coherence and recovery. These limitations provide the 192 motivation for this work. Specifically, the problem is to design a low-complexity 193 (real-time) CS aided data aggregation method that is energy efficient and can 194 guarantee a successful recovery of the measured data from IoT networks. 195

¹⁹⁶ 3. Proposed Data Aggregation Protocol

In this section we first present the network model that will be used in our
analysis and next describe the proposed data aggregation protocol which forms
the light weight measurement matrix.

200 3.1. Network Model

Consider an IoT network with N nodes deployed in a rectangular area (an 201 example network with grid-wise deployment of N = 100 nodes is shown in 202 Fig. 1). The network can be represented by a graph G(V, E), where V is 203 the set of vertices or nodes and E represents the set of edges or links between 204 the nodes. The sink node S is the node that collects data from all the other 205 nodes in the network. We assume that all the nodes are loosely time synchro-206 nized and have homogeneous transmission coverage. Unit disc coverage model 207 is considered for all the nodes. We consider the communication range of the 208 nodes to be $D = \sqrt{\frac{5}{N} * a}$ [18]. Here, a is the length of the maximum side 209 of the considered area and N is the number of nodes. Data aggregation pro-210 ceeds in cycles (rounds) and each node generates one sample per cycle. For 211 example, the i^{th} node acquires data sample x_i in each cycle and N samples 212 $X = [x_1, x_2, x_3, \dots, x_N]^T \in \mathbb{R}^N$ will be acquired from all the nodes per cycle. 213 We also assume that there is no packet loss in data aggregation. We consider 214 both grid [31] [32] and random deployment [33] scenarios for analysis in further 215 sections as these network deployments have their own significance in different 216 application scenarios. 217

218 3.2. Proposed Data Aggregation Protocol

As described above, $X \in \mathbb{R}^N$ is a signal of length N that contains measurements from N nodes in the network. To aggregate data from all the nodes, M nodes are randomly picked such that each node is a Cluster Head (CH) with a probability $P_{CH} = \frac{M}{N}$. The remaining (N - M) leaf nodes connect to their respective nearest CH through the shortest path (route with minimum distance). Accordingly, the whole network gets divided into M non-overlapping

clusters to aggregate sensors data. The M clusters $\{c_1, c_2, \ldots, c_M\}$ can contain 225 distinct $\{n_1, n_2, \ldots, n_M\}$ number of nodes. Every node in the cluster measures 226 its data sample x_i (e.g., temperature, humidity, light intensity, etc.) and mul-22 tiplies it with a random value α_i generated from a Bernoulli distribution with 228 a success probability of 0.5. In other words, the i^{th} node performs $\alpha_i x_i$, where 229 α_i is randomly drawn from the set $\{-1,1\}$ with a Bernoulli distribution and 230 $i \in [1, N]$. Each leaf node sends the measurement $\alpha_i x_i$ to its CH. The CH adds 231 the received measurements from the leaf nodes including its own measurement. 232 The final measurement at j^{th} CH, $y_j = \sum_{i \in c_i} \alpha_i x_i$ is the linear combination of 233 α_i and x_i , where the nodes belonging to the cluster take non-zero values i.e., 234 $\{\alpha_i \neq 0, x_i \neq 0\} \in c_i$ and the nodes that do not belong to the cluster can be 235 assumed to be zeros i.e., $\{\alpha_i = 0, x_i = 0\} \notin c_j$. The CHs deliver the computed 236 measurements to the sink node through the Minimum Spanning Tree (MST). 237 Dijkstra's and Kruskal algorithms can be used to create MST of CHs along with 238 the sink node. The CHs follow the pack and forward method [9] that provides 239 the feasibility to encapsulate the current measurement of a CH with the relaying 240 packet from descendant CHs along the MST towards the sink. 241

From the CS formalism in Section II, each cluster can be considered as a row 242 of the measurement matrix Φ and each node in the network corresponds to a 243 column of Φ . In other words, M randomly formed clusters and the nodes in each 244 cluster correspond to rows and respective columns of Φ . The j^{th} cluster c_i forms 245 the j^{th} row of Φ , i.e., φ_j . The support vector of φ_j is $\Delta_j = \{i : i \in [1, N], i \in c_j\},\$ 246 $\varphi_{j_{\Delta_j}} = \{\alpha_i : i \in \Delta_j\}$ and $\varphi_{j_{\Delta_j^c}} = 0$. In other words, the j^{th} row of Φ at 247 respective columns of nodes that are connected as a cluster $i \in c_i$ will be assigned 248 values from the set $\{-1, +1\}$ with a Bernoulli distribution. The remaining 249 entries in the row will be zeros. 250

More concretely, $\Phi \in \mathbb{R}^{M \times N}$, $\Phi = [\varphi_1^T, \varphi_2^T, \dots, \varphi_M^T]^T$ contains elements in each row

$$\varphi_{ji} = \begin{cases} -1 \text{ or } +1 & \text{if } i \in c_j \\ 0 & \text{otherwise} \end{cases}$$

Packets received at the sink node from the MST contain elements of the measurement vector $Y = [y_1, y_2, \dots, y_M]^T \in \mathbb{R}^M$ which are linear combinations of the measured data and the random values of nodes, i.e.,

$$Y = \begin{pmatrix} y_1 \\ y_2 \\ \vdots \\ y_M \end{pmatrix} = \begin{pmatrix} \varphi_1 \\ \varphi_2 \\ \vdots \\ \varphi_M \end{pmatrix} (X) = \Phi X,$$
(7)

where $X = [x_1, x_2, \dots, x_N]^T$, $X \in \mathbb{R}^N$, $\varphi_m \in \mathbb{R}^N$, $y_m \in \mathbb{R}$ where $m \in [1, M]$. 256 To gain insight into the described LWCDA, we consider a network of grid-257 wise deployed 100 nodes with a sink node (S = 101), which is placed at the 258 center of the network as shown in Fig. 1. Fig. 1 shows the measurement matrix 259 formation from the network and the sink node. Consider the example node of 260 98 from Fig. 1, which is a CH and has two descendant nodes 88,97. The mea-261 surement matrix Φ contains a row which represents the cluster with the nodes 262 98, 88, 97 and contains non-zero values from the set $\{-1, +1\}$ that are drawn 263 from a Bernoulli distribution with a success probability of 0.5 at respective 264 columns, as shown in Fig. 1. 265

To recover the original signal $X \in \mathbb{R}^{\mathbb{N}}$ from the measurement vector $Y \in$ 266 \mathbb{R}^{M} , the sink node needs to have the knowledge of Φ . The information of Φ 267 can be shared with the sink by maintaining synchronized seeds and pseudo-268 random number generators between the nodes and the sink [8]. Practically, to 269 share pseudo-random number seeds, each node has to send its seed to the sink 270 [19] and this requires a large number of transmissions for large-scale networks. 271 Another approach is to transmit information of Φ to the sink along with the 272 measured data if the message overhead is negligible [18]. In our data aggregation 273 algorithm, each node needs to send or share the information of $\alpha = -1$ or +1274



Figure 1: The procedure of measurement matrix designing from a network with N = 100 nodes and M = 40. The sink S = 101 is represented by a star, square boxes represent the CHs and remaining nodes are leaf nodes. The red line represents MST and black line represents connection from leaf node to CH.

with the sink, which can take a maximum of one octet of packet payload. We 275 consider the case that every j^{th} CH sends individual α values of the nodes 276 that belong to that cluster c_i and their indices Δ_i along with the measurement 277 $\sum_{i \in c_i} \alpha_i x_i$ to the sink in the first cycle of data collection. The system of linear 278 equations in (7) (M < N) is under-determined and will give infinitely many 279 solutions while recovering X from Y. The sink node reconstructs full dimension 280 $\widehat{X} \in \mathbb{R}^N$ from the received measurement vector $Y \in \mathbb{R}^M$ by solving either of 281 the optimization problems discussed in Section 2. 282

283 3.2.1. Node-level Complexity for Encoding

The node-level computation complexity required for computing the measurements during the data aggregation is computed in terms of generating or storing the number of random values. The proposed data aggregation algorithm constructs Φ on the fly while data is being aggregated from the nodes. Note that each node is required to generate only a random value -1 or +1 from a Bernoulli distribution as discussed above. The node level complexity of our method in terms of generating or storing number of random values is $\Theta(1)$ which

is independent of sensing data sparsity and network size. The $\Theta()$ refers the 291 formal notation for stating the exact bound on growth of resource needs (com-292 putation and storage) of an algorithm. Baseline data aggregation approaches 293 [8]-[11] which utilize dense random measurements require the generation of the 294 respective columns at each node which is the size of $\Theta(M)$ units. In case of 295 sparse random measurements based data aggregation methods [13]-[15], every 296 node in the network stores the complete Φ . The size of the required storage is 297 $\Theta(MN)$. Some of the methods which use sparse random measurements such as 298 [12] generate the respective row of Φ at every node and the row size is $\Theta(N)$ 299 units. The values of M and N are proportionally related and depend on sensing 300 data sparsity and the network size. This dependency poses multiple constraints 301 on the real-time implementation of the large-scale network applications where 302 the data to be sensed has low sparsity. The proposed approach is lightweight as 303 it completely eliminates the burden of generating a specific column or storing 304 the entire Φ at the node to perform data aggregation in the network. Conse-305 quently, the proposed method can be implemented in commercially available 306 low end IoT nodes. 307

The measurement matrix Φ should satisfy certain properties as discussed in Section 2 for it to allow data recovery. In the following section we evaluate the properties of the Φ and demonstrate how it can guarantee the reconstruction.

311 4. Measurement Matrix Analysis

To analyze the proposed measurement matrix Φ , we rely on RIP, coher-312 ence and Phase Transition (PT) [34] analyses. We considered both grid and 313 random deployments scenarios as both deployments have their own significance 314 for different application scenario [31]-[33]. We considered DCT, DFT, DWT, 315 Laplacian and Diffusion Wavelet (DiWT) bases (Ψ) for the analyses. The DCT. 316 DFT and DWT bases (Ψ) can sparsify data from regular (grid-wise) IoT de-317 ployments [8], [19]. In case of randomly deployed networks, the Laplacian [19] 318 and Diffusion wavelet (DiWT) [35] can accommodate irregularity and provide 319

320 a sparse representation of the data.

321 4.1. Numerical Experiments: RIP Analysis

As discussed in Section 2, RIP is a standard tool to analyze near-orthonormal performance of a CS matrix while operating with sparse input vectors. This property measures the performance of a compressed sensing matrix in terms of the Restricted Isometry Constant (RIC) δ_k . As a result, δ_k can be used to evaluate the ability to recover a sparse signal from the measurement vector. From the definition of RIP of a matrix $A \in \mathbb{R}^{M \times N}$, for k-sparse vectors with a constant δ_k , (5) can be rewritten as,

$$\delta_k = \max_{T \subset [N], |T| \le k} \|A_T^* A_T - Id\|_{2 \to 2},$$
(8)

where $Id \in \mathbb{R}^{|T| \times |T|}$ is an identity matrix and T is the support set of k-sparse vector [24].

For any matrix A that satisfies RIP with a RIC of δ_k , the following condition holds:

$$(1 - \delta_k) \le \lambda_{\min}(A_T^* A_T) \le \lambda_{\max}(A_T^* A_T) \le (1 + \delta_k), \tag{9}$$

where λ_{min} and λ_{max} are the minimum and maximum eigenvalues of the symmetric matrix $A_T^* A_T$ respectively.

335 4.1.1. Numerical verification of δ_k , λ_{min} and λ_{max}

The DFT, DCT, DWT, Laplacian and DiWT matrices are separately consid-336 ered as bases $\Psi_{N\times N}$ for the empirical evaluation of δ_k . To verify with DWT, we 337 evaluated the performance of the CS matrix A across several popular wavelets 338 such as Daubechies, Symlets, Coiflets and chose the Daubechies-4 wavelet for 339 all our analysis as it gives a better range for k compared to other wavelets. The 340 compressed sensing matrix $A_{M \times N} = \Phi_{M \times N} \Psi_{N \times N}$ with N = 1024, at different 341 compression rates with M = 103, 308, 717, 922 are considered for evaluation. 342 For a compressed sensing matrix $A \in \mathbb{R}^{M \times N}$, the compression rate $\Gamma\%$ can be written as, $\Gamma\% = \left(1 - \frac{M}{N}\right) \times 100.$ 344



Figure 2: RIC δ_k and eigenvalue bounds $(\lambda_{min}, \lambda_{max})$ for the proposed CS matrix $A = \Phi \Psi$. Here, Φ is the measurement matrix constructed using LWCDA algorithm and analyzed for different Ψ (DCT, DFT, DWT, Laplacian and DiWT) matrices. (a) - (d) show values of δ_k , λ_{max} and λ_{min} for matrix A at different compression rates Γ . CS matrix A gives a better range of k with DFT and DCT compared to DWT basis in grid deployment. In the random deployment case, CS matrix A gives slightly better range of k with Laplacian compared DiWT.

Sparsity value k										
	Regular deployment			Random deployment						
Compression rate Γ	DFT	DCT	DWT	Laplacian	DiWT					
90%	7	6	1	2	1					
70%	15	14	3	4	3					
30%	36	35	9	13	9					
10%	67	66	11	19	13					

Table 1: Sparsity value k where RIC $\delta_k \in (0, 1) \ \forall \ u \in \Sigma_k$ for different Γ .

The procedure followed for empirical evaluation of δ_k , λ_{min} and λ_{max} is described below:

- 1. Generate the measurement matrix Φ and the basis Ψ for fixed N = 1024and for each M.
- **2.** For a combination (N, M), k is varied across [1:M].
- 350 3. Consider a k-sparse vector $u \in \mathbb{R}^N$. The vector u contains non-zero values at k randomly chosen locations and the values themselves are chosen from a normal distribution.
- **4.** Find the support set for u, i.e., T.
- 5. Repeat steps 2 and 3 for 10000 iterations for each combination (N, M, k)and calculate δ_k from (8).
- 6. Compute $\lambda_{min}(A_T^*A_T)$, $\lambda_{max}(A_T^*A_T)$, where T is the support set corresponding to δ_k from step 5.

The calculated RIC δ_k values, λ_{max} , λ_{min} with respect to sparsity value kat different compression rates Γ , are plotted in Fig. 2. In Fig. 2, δ_{kf} , δ_{kc} , δ_{kw} , δ_{kl} , δ_{kd} refer to RICs of CS matrix A where Ψ is DFT, DCT, DWT, Laplacian and DiWT respectively. λ_{min} , λ_{max} refer to the minimum and the maximum eigenvalues of CS matrix A respectively when Ψ is DFT. Similar behavior of eigenvalues is also observed with DCT, DWT, Laplacian and DiWT bases. Sparsity values k obtained while $\delta_k \in (0, 1)$ for the proposed CS matrix A with different bases are tabulated in Table I (the same can be observed from Fig. 2 as well). The interesting observation made from Table I is that the CS matrix A gives better range for k with DFT compared to that of DCT and DWT bases. In the random deployment case, CS matrix A gives slightly better range for k with Laplacian then DiWT basis.

370 4.2. Coherence Analysis

As discussed in Section 2, if X can be sparsely represented in an arbitrary basis Ψ , then for successful recovery, CS theory requires low mutual coherence between columns of the matrix $A = \Phi \Psi$. The mutual coherence μ of the matrix A with different bases at various compression rates Γ is calculated using (6), i.e., the CS matrix $A_{M \times N} = \Phi_{M \times N} \Psi_{N \times N}$ where N = 1000 and M is chosen to vary from 100 to 900 in steps of 100 (M = 100 : 100 : 900) for calculating μ .



Figure 3: Comparison of mutual coherence μ of the CS matrix $A = \Phi \Psi$ with different bases where matrix Φ is constructed from LWCDA. Columns of the matrix A are highly incoherent with DFT basis among all.

The resultant mutual coherence with different bases are shown in Fig. 3. The CS matrix A provides better incoherence for the DCT and DFT bases compared to the DWT basis where Φ is constructed from grid deployment. In case of random deployment, the coherence of the matrix A with Laplacian is fairly better compared to DiWT basis across all compression rates. It is
observed from Fig. 3 that among all the bases, DFT provides high incoherence
for all compression rates.



384 4.3. Phase Transition Analysis

Figure 4: Phase transition analysis of CS matrix $A = \Phi \Psi$ for different bases, where Φ is the proposed measurement matrix and Ψ is the basis matrix. The color bar indicates successful recovery probability P_s . CS matrix A with DCT and DFT basis yields promising recovery region.

For a given CS matrix, the phase diagram can be generated as a numerical 385 representation of successful recovery probability P_s over the space (k/M, 1 -386 $(M/N) \in [0,1]^2$, as in [34]. This space is discretized and we performed multiple 38 compression and decompression experiments at each grid point. The phase 388 diagram is finally approximated by using successful recovery probability $P_s =$ 389 $Pr\{e \leq e_{TH}\}$, where the reconstruction error $e = \left\|X - \hat{X}\right\|_2 / \|X\|_2$, with an 390 appropriately selected threshold e_{TH} . We considered error threshold $e_{TH} =$ 391 10^{-8} in our analysis. For PT analysis, $A_{M \times N} = \Phi_{M \times N} \Psi_{N \times N}$ is considered 392 with N = 1000 and evaluated for different compression rates (Γ) with M =393

³⁹⁴ 100 : 100 : 900. Fig. 4 shows the phase diagram of CS matrix $A = \Phi \Psi$, where ³⁹⁵ Φ is the measurement matrix and Ψ is the basis. Fig. 4 also illustrates that the ³⁹⁶ proposed measurement matrix Φ with DCT and DFT bases provides promising ³⁹⁷ recovery region compared to DWT where Φ is constructed from grid deployment. ³⁹⁸ In case of random deployment, Laplacian basis provides slightly better recovery ³⁹⁹ region compared to DiWT basis.

This evaluation has shown that the proposed measurement matrix Φ gives 400 better performance with DCT and DFT bases compared to the DWT basis 401 in terms of RIC, coherence and PT analysis where Φ is designed from grid-402 wise deployed network. Further, in random deployment scenario, Laplacian 403 and DiWT bases give comparable performance. The proposed matrix Φ with 404 DCT and DFT bases (Ψ) has the ability to recover the signals successfully even 405 though they have fairly low sparsity. Whereas in case of DWT, Laplacian and 406 DiWT, the matrix Φ can recover the signals on the condition that they are 407 highly sparse. 408

To extend the proposed LWCDA method to fairly low sparse data cases especially in random deployment scenario, we propose a technique called spatial logical node mapping, which is described in the following subsection.

412 4.4. Spatial Logical Node Mapping

Before invoking the LWCDA algorithm, we first model the network as a 413 logical chain based on the Euclidean distance between the nodes. The algorithm 414 starts from any random node and gives sequential node IDs along the chain. The 415 method used to form the logical chain is similar to that in [36]. We consider 416 that in the initial phase, each node sends the distance information of the nodes 417 that are in its coverage area to the sink. The sink maps the new node IDs 418 from old node IDs and sends it back to the nodes to change. Fig. 5 provides 419 more insight into the Spatial Logical Node Mapping (SLNM) with an example 420 network of N = 30 nodes. This preprocessing will introduce spatial correlation 421 in the data since adjacent nodes in the chain tend to be the nodes which are 422 geographically close to each other [36] [37]. The spatial correlation among the 423

samples generated from the nodes which are geographically close to each other
can make the signal sparse in the regular DFT and DCT bases. SLNM adds
the advantage to LWCDA to guarantee the recovery of the measured data from
the random deployment as it introduces sparsity for the data in DFT and DCT
bases.



Figure 5: Logical node mapping.

The data aggregation algorithms proposed in the literature such as [8]-[19] do not discuss hardware implementation details. The implementation procedure and assumptions considered for software simulations differ when it comes to realtime hardware implementation. For the completeness of the proposed algorithm and analysis, we describe an optimal way of implementation which shows the efficacy of the proposed method in a real-time scenario.

435 5. Real-time Implementation

The in-house IITH Motes [23] are used for implementing the proposed data aggregation algorithm (LWCDA). The IITH Mote is a ZigBee system-on-chip combining a 2.4 GHz IEEE 802.15.4 radio transceiver with a 8 MHz, 8-bit processor having 128 kB of flash memory and 8 kB of RAM. TinyOS [38] is used to program the proposed LWCDA algorithm on the nodes. Based on the required compression rate Γ , the threshold value T_{hr} will be decided. From

the selected M CHs, the probability of the i^{th} node becoming a CH is $P_{CH} =$ 442 $\frac{M}{N}$ as discussed in Section III. Let T_{u_i} denote the generated uniform random 443 value at the i^{th} node, i.e., $T_{u_i} \in U \sim [0,1]$. If $T_{u_i} \leq T_{hr}$ then the i^{th} node 444 becomes a CH. CH probability can be rewritten as $P_{CH} = Pr\{T_{u_i} \leq T_{hr}\} = T_{hr}$ 445 where $i \in [1, N]$. For example, if the threshold is considered to be $T_{hr} = 0.3$ 446 then on an average 30% of the nodes become CHs ($P_{CH} = 0.3$) and $\Gamma = 70\%$ 447 compression can be achieved. The sink node broadcasts a starting packet with 448 the specified threshold T_{hr} value. Each node in the network broadcasts this 449 packet once so that the threshold value reaches every other node in the network. 450 The nodes calculate Received Signal Strength Indication (RSSI) values from the 451 received packets and stores them in a table. It is important to note that each 452 node will have RSSI values of all the other nodes that are in its radio range 453 (communication range). Using the created RSSI table, the nodes, which are 454 selected as leaf nodes, connect to nearest CHs and CHs form MST. 455

As the sink node requires the knowledge of Φ , i.e., $\{\alpha_i\}$ values and respective 456 indices Δ_j , where $i \in c_j$ and $j \in [1, M]$, in the initial phase (i.e., first cycle of 457 data aggregation), CH sends $\{\alpha_i\}, \Delta_j$ to the sink along with the final measure-458 ment $\sum_{i \in c_i} \alpha_i x_i$. This is a small overhead as α and the respective node index 459 (node address) together can take a maximum of three octets when short address 460 mode is considered. By the end of the initial phase, all the nodes register their 461 respective destination node addresses. In data sensing phase (i.e., from second 462 data aggregation cycle on-wards), in each cycle, all the leaf nodes compute their 463 measurements and send them to their respective destined CHs. Further, each 464 CH computes the final measurement and forwards it to the sink. Pseudo code 465 of the node level implemented algorithm is described in Algorithm 1. 466

The proposed LWCDA algorithm is independent of the deployment scenario. As an example to verify the implementation efficacy of the LWCDA, we deployed 50 nodes grid-wise in an area of 321.44 ft^2 as shown in Fig. 6. The sink node is connected to a PC that collects measured data from all the nodes in the network. For illustration, we considered a threshold $T_{hr} = P_{CH} = 0.3$ and obtained 14 CHs among the deployed 50 nodes in a particular realization of the experiment,

Algorithm 1 Pseudo code for the data aggregation algorithm at node level

Require: T_{hr}

1:	Data collection round r $\leftarrow 0$						
2:	Generate uniform random value $T_{u_i} \in U \sim [0,1]$ (i refers node number)						
3:	$\mathbf{if} \ (T_{u_i} \leq T_{hr}) \mathbf{then}$						
4:	$Type \leftarrow CH$						
5:	else						
6:	$Type \leftarrow Leaf node$						
7:	end if						
8:	while $r \ge 0$ do						
9:	if $(Type \text{ is CH})$ then						
10:	$r \leftarrow r+1$						
11:	if $(r \text{ is } 1)$ then						
12:	Broadcast CH packet						
13:	Generate uniform random value $R_i \in U \sim [0, 1]$						
14:	if $(R_i \leq 0.5)$ then						
15:	$lpha_i \leftarrow -1$						
16:	else						
17:	$\alpha_i \leftarrow 1$						
18:	end if						
19:	Discover the next hop destination node CH_{dest} : other CH or the leaf node in MST						
	towards the sink						
20:	end if						
21:	Measure data sample x_i						
22:	Compute: $\alpha_i x_i$						
23:	Receive data packets from all the leaf nodes and descendant CHs						
24:	Compute: $\sum_{i \in c_j} \alpha_i x_i$						
25:	Send CH data packet to CH_{dest} using pack and forward method						
26:	else						
27:	$r \leftarrow r+1$						
28:	if $(r \text{ is } 1)$ then						
29:	Find $RSSI_h \leftarrow \operatorname*{argmax}_h \{ RSSI \text{ of CHs which are in the radio range} \}$						
30:	$Leaf_{dest} \leftarrow CH_h$						
31:	if $(Leaf_{dest} \text{ is NULL})$ then						
32:	Discover the next hop destination node $Leaf_{dest} \leftarrow$ neighboring leaf node in the						
	shortest path towards nearest CH						
33:	end if						
34:	Generate uniform random value $R_i \in U \sim [0, 1]$						

45:	end while
44:	end if
43:	Send the data packet to $Leaf_{dest}$
42:	Compute: $\alpha_i x_i$
41:	Measure data sample \boldsymbol{x}_i
40:	end if
39:	end if
38:	$\alpha_i \leftarrow 1$
37:	else
36:	$\alpha_i \leftarrow -1$
35:	if $(R_i \leq 0.5)$ then



Figure 6: Experimental setup with N = 50 nodes deployed in an area of 321.44 ft^2 .

while the remaining nodes are connected to their respective CHs. Accordingly, 473 14 clusters were formed, and thus the rows of the measurement matrix $\Phi_{14\times 50}$ 474 were generated. The resultant measurement matrix $\Phi_{14\times 50}$ is shown in Fig. 7. 475 To evaluate the efficacy of the proposed method, we considered coherence as 476 the metric. We repeated the above experiment for a range of threshold values 477 $T_{hr} = 0.1 : 0.1 : 0.9$, and in each case of T_{hr} , the measurement matrix Φ was 478 constructed. To compute the coherence of Φ against all the compression rates, 479 we obtained Φ for 10 realizations and for each T_{hr} . Each realization gives one 480 mutual coherence value μ for a pair of Φ and Ψ . We then averaged μ over 10 481



Figure 7: Measurement matrix $\Phi_{14\times 50}$ constructed from the real field deployment with N = 50 nodes and $\Gamma = 70\%$.

realizations for each T_{hr} . To compare with the real deployment, we simulate a 482 similar scenario in software. Average coherence values of the matrix A designed 483 from both the experiment (exp.) as well as the simulation (sim.) are plotted in 484 Fig. 8. Fig. 8 illustrates that the coherence values of the matrix A where the 485 proposed measurement matrix is constructed from the experiment as well as the 486 simulation with DFT, DCT and DWT bases are in excellent agreement. These 487 results show efficacy of the proposed method in a real-time implementation. 488 It justifies our claim that the proposed method does not require any extra 489 computational overhead (such as the generation of the individual columns of the 490 matrix Φ , storage of Φ etc.). Hence, the proposed method can be implemented 491 on low end commercial off-the-shelf IoT nodes. 492

In the following section, we evaluate the performance of the proposed data aggregation method in an application scenario.

495 6. Results And Evaluation

In this section, the performance of the proposed data aggregation method is analyzed using the following metrics:

498 1. Reconstruction error.



Figure 8: Comparison of the mutual coherence μ for the CS matrix $A = \Phi \Psi$ where Φ is constructed from the real-time deployment and simulations against different compression rates Γ , with N = 50 nodes and for different bases DFT, DCT and DWT. Mutual coherence curves from simulation and real-time deployment are very close and demonstrate the efficacy of the proposed method.



Figure 9: Temperature sensing field.

- 499 2. Transmission cost.
- 500 6.1. Reconstruction Error Analysis
- 501 We extend the application of the proposed algorithm for compressible signals
- ⁵⁰² by using a real data set for evaluation. Real temperature data which is obtained



Figure 10: Measured data from random (top) and grid-wise (bottom) deployed 1024-node network.

by capturing thermal images from the top view of an area $100m \times 100m$ is con-503 sidered for analysis. Thermal images were captured in a region using a mobile 504 phone interfaced thermal camera [39] in the campus of IIT Hyderabad on August 505 14, 2016 centered at location of Latitude:17.593978 and Longitude:78.123359. 506 Fig. 9 visualizes the considered temperature data for evaluating recovery perfor-507 mance of the proposed method. Fig. 10 shows the measured data from random 508 and grid-wise deployed 1024 sensor nodes on the field. We used MATLAB 509 R2015b software for performing all our simulations. Ideally the sparsity value 510 k of X in a basis Ψ is measured using the l_0 norm, $k = \|\theta\|_0$, where $\theta = \Psi X$. 511 For real-time data which is approximately sparse, only few large coefficients 512 contribute a large proportion of the total energy. We use numerical sparsity 513 [35] as the measure of sparsity which represents the number of effective large 514 coefficients. If a vector X can be represented using a sparsifying basis Ψ as 515 $X = \Psi \theta$, then the numerical sparsity of X can be calculated as 516

$$s = \frac{\|\theta\|_1^2}{\|\theta\|_2^2}.$$
 (10)

- Numerical sparsity of the considered temperature data with different bases (Ψ)
- (DFT, DCT, DiWT and Laplacian) are tabulated in Table II.
- Table II shows considered data is more sparse in DCT and DFT bases com-

Table 2: Sparsity measure of the temperature data

Numerical sparsity value s									
Regular deployment			Random deployment						
				SLNM					
DFT	DCT	DWT	Laplacian	DiWT	DFT	DCT			
2.2205	2.5251	7.6707	15.925	53.0402	2.6219	2.7569			



Figure 11: Average reconstruction error against different compression rates. Here, 1024 temperature data points are considered. Figures (a) and (b) depicts recovery of grid-wise and Randomly deployed nodes measured data respectively. DFT basis provides low recovery error compared to all bases in both grid and random deployment scenario.

pared to the others in both grid-wise and random deployment scenarios. To 520 evaluate recovery performance of the measured data from grid-wise deployed 521 nodes the basic LWCDA is used to construct the measurement matrix Φ . In 522 case of random deployment, Φ is constructed from LWCDA and SLNM. The 523 OMP algorithm [27] is used for the recovery of the compressed data. We evalu-524 ated the performance of the proposed data aggregation method in terms of the 525 reconstruction error e against the compression rate Γ . Fig. 11 compares average 526 reconstruction error of our method with different bases. In our analysis, e is 527 averaged over 100 iterations for each Γ . From Fig. 11a, it can be observed that 528 DFT and DCT can recover the data which is measured from grid-wise deployed 529

nodes with a low error compared to DWT for all compression rates. Fig. 11b 530 illustrates the data recovery performance of the proposed method where the 531 data is measured from randomly deployed sensor nodes. From Fig. 11b, it can 532 be observed that DCT and DFT can recover the data with a low error across 533 all compression rates compared to other bases. However, DiWT and Laplacian 534 result in high recovery error as they require the signal to be highly sparse. This 535 evaluation has shown that the proposed LWCDA method provides high recovery 536 fidelity using the DFT basis for the data measured from both the random and 537 grid-wise deployed nodes. 538



Figure 12: Comparison of average reconstruction error against different compression rates for grid and random deployment scenarios. Here, 1024 temperature data points are considered. Figures 12a and 12b depict recovery performance of the data measured from grid-wise and randomly deployed nodes respectively. In the grid-wise deployment scenario, the proposed LWCDA performs superior to SPRM. However, in case of random deployment, the proposed LWCDA provides superior performance compared to CWCDA and a comparable performance with Hybrid CS.

On the other hand, we perform recovery error comparative analysis of the proposed algorithm with existing CS based data gathering methods. To demonstrate the efficiency of our algorithm, we compare with Shortest Path Routing Measurements (SPRM) [18] for the grid-wise deployment scenario, and Clusterbased Weighted Compressive Data Aggregation (CWCDA) [15], Hybrid Compressed Sensing (Hybrid CS) [8] methods for the random deployment scenario. SPRM [18] is closely related to our work, and CWCDA [15] is a data aggrega-



Figure 13: Sea surface temperature sensing field.

tion method based on sparse random measurements. In contrast, the Hybrid 546 CS [8] method utilizes dense random measurements. Fig. 12 compares average 547 reconstruction error of the proposed LWCDA method with baseline approaches 548 against compression rate Γ . Here, *e* is averaged over 100 iterations for each Γ . 549 From Fig. 12a, it can be observed that the proposed LWCDA method has lower 550 recovery error compared to SPRM for all considered compression rates. Fig. 12b 551 illustrates the data recovery performance of the proposed method where the data 552 is measured from randomly deployed sensor nodes. From Fig. 12b, it can be 553 observed that the proposed method yields superior recovery performance com-554 pared to CWCDA across all considered compression rates. Relative to Hybrid 555 CS, the performance of the proposed method is comparable at lower compression 556 rates ($\Gamma \leq 50$) and superior at higher compression rates ($\Gamma > 50$). 557

To evaluate the proposed data aggregation method on independently generated data set, we have considered sea surface temperature data of the region of Latitude:23-25 and Longitude:78-80 measured from INSAT 3D remote sensing system at 12:30 IST, December 21, 2017 [40]. Fig. 13, visualizes the considered sea surface temperature sensing field and Fig. 14 shows the measured data from random and grid-wise deployed 1024-node network upon the sensing field. Comparison of average reconstruction error of the proposed LWCDA method with



Figure 14: Measured data from random (top) and grid-wise (bottom) deployed 1024-node network upon considered sea surface temperature sensing field.

baseline approaches against compression rate Γ is depicted in Fig. 15. From 565 Fig. 15a (where data is measured from grid-wise deployment), one can observe 566 that the proposed LWCDA method has lower recovery error compared to SPRM 567 for all considered compression rates. From Fig. 15b (where data is measured 568 from random deployment), one can observe that the proposed method yields 569 superior recovery performance compared to CWCDA across all considered com-570 pression rates. Relative to Hybrid CS, the performance of the proposed method 571 is comparable at lower compression rates ($\Gamma \leq 50$) and superior at higher com-572 pression rates ($\Gamma > 50$). From Fig. 12 and Fig. 15, one can infer that the pro-573 posed LWCDA can recover the data with high fidelity in both grid and random 574 deployment scenarios while being at par or better than competing algorithms. 575 In the following section, we perform a comparative analysis of the transmis-576 sion cost of our algorithm with traditional CS based data gathering methods. 577 To demonstrate the efficiency of our algorithm, we compare with SPRM for 578 the grid-wise deployment scenario, CWCDA, Hybrid CS and a Non-compressed 579

580 Sensing (Non-CS) method for the random deployment scenario.



Figure 15: Comparison of average reconstruction error against different compression rates for grid and random deployment scenarios. Figures 15a and 15b depict recovery performance of the data measured from grid-wise and randomly deployed 1024 data points (nodes) on sea surface temperature sensing field respectively. In the grid-wise deployment scenario, the proposed LWCDA performs superior to SPRM. However, in case of random deployment, the proposed LWCDA provides superior performance compared to CWCDA and a comparable performance with Hybrid CS.

581 6.2. Transmission Cost Analysis

We considered a cost model for computing the required transmission cost (or 582 energy) for data aggregation as in [8]. Let c_{ij} be the energy expense of sending 583 one unit of data across link $(i, j) \in E$ where nodes $i, j \in V$. Assuming identical 584 data rate and bandwidth for all links, we can show that c_{ij} is proportional to 585 the path loss on the link (i, j), hence c_{ij} is a function of link length. Further, we 586 considered c_{ij} as the Euclidean distance between the nodes i, j and one packet 587 as one unit of traffic on the link $(i, j) \in E$. The total transmission cost (or 588 energy consumption) of the network is computed as, 589

$$T_{cst} = \sum_{(i,j)\in E} t_{ij}c_{ij},\tag{11}$$

where t_{ij} represents the traffic on the link $(i, j) \in E$. ZigBee protocol is considered for simulations as the ZigBee stack is one of the most commonly used protocols among commercially available off-the-shelf IoT solutions. The size of PHY layer data field of the packet of ZigBee is 128 bytes, of which 87 bytes can be used for application payload as the remaining octets are reserved for packet



Figure 16: Comparison of the transmission cost required for data aggregation from 625 nodes deployed in an area $256m \times 256m$ using the proposed LWCDA and SPRM, Hybrid CS, CWCDA and Non-CS methods against the compression rate Γ . Transmission cost of the LWCDA is significantly low compared to all methods almost for all compression rates ($\Gamma \leq 80\%$).

header information of higher layers. The number of bits required to represent
the data sample and the address field (short address mode) is considered to be
2 octets.

For transmission cost comparison, a network deployment of 625 nodes in an 598 area of $256m \times 256m$ is considered. The comparison of the transmission cost 599 for data aggregation using the proposed method (LWCDA), SPRM, Hybrid CS, 600 CWCDA and a Non-CS method with respect to the change in compression rate 601 (Γ) is shown in Fig. 16. In particular, we considered the conventional shortest 602 path algorithm [41] for data gathering as the Non-CS approach, where each node 603 in the network sends its data to the sink through the shortest path. From Fig. 16, 604 it can be observed that our LWCDA (labeled as LWCDA-Random for random 605 deployment) method requires very low transmission cost for data aggregation 606 compared to Non-CS, Hybrid CS and CWCDA for all compression rates where 607 nodes are randomly deployed. In case of grid deployment, compared to SPRM 608 the proposed LWCDA (labeled as LWCDA-Grid for grid deployment) method 609 outperforms until $\Gamma = 80\%$ for data aggregation. In the proposed LWCDA 610 method, an increase in compression rate Γ decreases the number of required 611



Figure 17: Comparison of the percentage of disbursed transmission cost of the proposed LWCDA with respect to SPRM, Hybrid CS, CWCDA and Non-CS methods against the compression rate Γ . Here, data aggregation is considered from 625 nodes deployed in an area $256m \times 256m$. Percentage of disbursed transmission cost of the LWCDA with respect to SPRM, Hybrid CS, CWCDA and Non-CS methods is low for almost all compression rates ($\Gamma \leq 80\%$).

clusters for data aggregation. A decrease in number of clusters increases the 612 required transmission cost for data aggregation as the leaf nodes need to send 613 their measurements to CHs from farther distance. Further, as Γ increases, 614 the required transmission cost to collect measurements from CHs (using MST) 615 also decreases. This results in an increase of total transmission cost T_{cst} at 616 higher compression rates ($\Gamma > 80\%$) as shown in Fig. 16. Fig. 17 illustrates the 617 percentage of disbursed transmission cost $D_{T_{est}}$ of the proposed LWCDA with 618 respect to that of Hybrid CS, LWCDA, SPRM and Non-CS methods. Percentage 619 of disbursed transmission cost $D_{T_{cst}}$ of a given method P with respect to the 620 method Q is defined as, 621

$$D_{T_{cst}}\% = \frac{T_{cst} \text{ of method } P}{T_{cst} \text{ of method } Q} \times 100.$$
(12)

The SPRM method at high compression rates ($\Gamma > 80\%$) results in lesser transmission cost as compared to that of the proposed LWCDA method. This in turn results in the percentage of disbursed transmission cost of LWCDA (LWCDA-Grid) to go beyond 100% as shown in Fig. 17 for higher compression rates.



Figure 18: Transmission cost comparison of the proposed LWCDA method against node density with SPRM, Hybrid CS, CWCDA and Non-CS methods at $\Gamma = 50\%$. Here, an area of $256m \times 256m$ is considered for the network deployment and number of nodes deployed (N) are varied. Transmission cost of the LWCDA is significantly low compared to SPRM, Hybrid CS, CWCDA and Non-CS methods for all considered node densities.

This is because, in the SPRM method, very few randomly selected nodes are 626 required to send data through the shortest path to the sink at high compression 627 rates. Although, SPRM offers higher compression rates with lower transmission 628 costs, it does not achieve good performance with respect to coherence leading to 629 higher reconstruction errors at higher compression rates, thereby not guarantee-630 ing a successful reconstruction (as discussed in [18]). For all compression rates 631 in both grid-wise ($\Gamma \leq 80\%$) and random deployment scenario, the proposed 632 LWCDA method can deliver the data to the sink with a lower transmission cost 633 as illustrated in Fig. 16 and with a lower percentage of disbursed transmission 634 cost as shown in Fig. 17, thereby enhancing the network lifetime as compared 635 to the considered baseline approaches. 636

To evaluate the effect of changing the node density on the required transmission cost for data aggregation of the proposed LWCDA, we performed an experiment where the number of nodes deployed is varied in the considered area of $256m \times 256m$. The transmission cost of data aggregation with respect to the changing in node density with $\Gamma = 50\%$ compression rate is shown in Fig. 18.



Figure 19: Comparison of the percentage of saved transmission cost of the proposed LWCDA with respect to SPRM, Hybrid CS, CWCDA and Non-CS methods against node density at $\Gamma = 50\%$. Here, an area of $256m \times 256m$ is considered for the network deployment and number of nodes (N) deployed are varied. The proposed LWCDA method offers savings in the transmission cost consistently with respect to the baseline approaches for all the considered node densities.

From Fig. 18, it is observed that the transmission cost increases with an in-642 crease in the node density. The interesting observation made from Fig. 18 is 643 that the transmission cost for LWCDA is significantly low as compared to that 644 of the traditional methods for all considered density levels in both deployment 645 scenarios. Fig. 19 shows the percentage of savings in the transmission cost with 646 respect to Non-CS, Hybrid CS, CWCDA and SPRM methods. Percentage of 647 saved transmission cost $S_{T_{cst}}$ of a given method P with respect to the method 648 Q is defined as, 649

$$S_{T_{cst}}\% = \left(1 - \frac{T_{cst} \text{ of method } P}{T_{cst} \text{ of method } Q}\right) \times 100.$$
(13)

From Fig. 19, one can observe that the proposed method consistently offers savings in transmission cost under the considered varying node densities. We can
infer that for large-scale dense networks, LWCDA algorithm can achieve significant improvements in the network lifetime compared to traditional approaches.
The location of the sink node affects the required transmission cost for data
aggregation [42]. To analyze the dependence of the transmission cost on the
sink location for data aggregation, we considered a 625-node network deployed



Figure 20: Comparison of the transmission cost required for data aggregation from 625 nodes deployed in an area of $256m \times 256m$ using the proposed LWCDA and SPRM, Hybrid CS, CWCDA and Non-CS methods against the sink location. The sink node location (X, Y) varies according to the line X = Y where $X, Y \in [0, 256]$. Transmission cost of the proposed LWCDA method is robust and lower compared to all baseline approaches for all considered sink locations.

(grid and random deployment) in an area of $256m \times 256m$ with varying sink 657 locations. Fig. 20 compares the transmission cost of the proposed LWCDA al-658 gorithm with that of SPRM (for grid-wise deployment) and Non-CS, Hybrid CS 659 and CWCDA (for random deployment) with respect to various sink locations. 660 Note that the variables $X, Y \in [0, 256]$ represent the geographic coordinates of 661 the sink node on the considered area. The sink location (X, Y) varies on the line 662 X = Y. The observation that can be made from Fig. 20 is that the transmission 663 cost of baseline approaches except CWCDA strongly depends on the sink loca-664 tion. Transmission cost required for data aggregation with CWCDA is robust 665 to sink location, but it requires more transmission cost compared to the pro-666 posed method across all sink locations. The considered traditional approaches 667 (SPRM, Hybrid CS and NoN-CS) yield lower transmission cost when the sink 668 is at the center of the considered area. In fact, if the sink is at the center of the 669 considered area, every node can connect to the sink with the shortest distance. 670 An interesting inference that can be made from Fig. 20 is that the transmission 671 cost of the proposed LWCDA algorithm for data aggregation in both grid-wise 672

and random deployment scenario is robust to the sink location and is much lower compared to that of the traditional methods for all the considered sink locations. This can be justified by noting that the proposed LWCDA algorithm aggregates data through clustering where required transmission cost is independent of the sink location. In addition, to aggregate measurements from randomly distributed CHs, which are connected through MST along with the sink node, incur almost same transmission cost irrespective of the sink location.

The evaluation has shown that the proposed method can deliver data with 680 high fidelity compared to SPRM (Figs. 12a, 15a) and CWCDA (Figs. 12b, 15b). 681 In comparison with Hybrid CS, the proposed method is competitive for lower 682 compression rates ($\Gamma \leq 50$) and yields superior performance for higher com-683 pression rates ($\Gamma > 50$) (Figs. 12b, 15b). However, Hybrid CS approach is 684 computationally intensive and impose multiple constraints on hardware imple-685 mentation. This is especially true for lower compression rates as the generation 686 of the column size increases. In case of transmission cost, the evaluation has 687 illustrated that the proposed LWCDA method requires less transmission cost 688 for data aggregation compared to SPRM ($\Gamma \leq 80\%$), Hybrid CS and CWCDA 689 for all compression rates. Transmission cost analysis with respect to the node 690 density (shown in Fig. 18) has shown that the proposed method can achieve 691 significant improvement in the network lifetime for large-scale dense networks. 692 Further, transmission cost analysis with respect to sink location (Fig. 20) has 693 illustrated that the proposed method's transmission cost is robust to the sink 694 location. This makes our approach attractive for various IoT applications. Fur-695 thermore, the complexity analysis discussed in Section 3.2.1 illustrates that the 696 proposed method eliminates the burden of storing or generating the measure-697 ment matrix information at the node level. This allows the proposed method to 698 be implementable on low-end IoT nodes. Thus, the proposed method is attrac-699 tive as it yields an optimal trade-off between transmission cost, recovery fidelity 700 and complexity for numerous IoT applications. 701

37

702 7. Conclusion and Future Work

In this paper, we proposed a CS based data aggregation method for IoT net-703 works which is both low-complex and energy efficient. In the proposed method, 704 we exploited non-overlapped clustering for data aggregation where each node 705 contributes to only one measurement. Hence, the columns of the measurement 706 matrix constructed from the proposed algorithm are coherent and recovery is 707 not possible for the data which is sparse in the canonical basis (Identity ma-708 trix). However, we showed that the measurement matrix, when combined with 709 the popular bases (DFT, DCT, DWT, Laplacian, and DiWT) could guarantee 710 the recovery of data with high fidelity. Unlike conventional methods, in the pro-711 posed data aggregation method the node-level complexity is independent of the 712 network size and data sparsity. The comparison of the transmission cost with 713 traditional approaches concludes that the proposed method is energy efficient 714 and can aid in extending the network lifetime by achieving minimal transmis-715 sion cost. Hardware implementation demonstrated the efficacy of the proposed 716 algorithm in a real-time implementation. Further, through the analysis of the 717 measurement matrix combined with the popular bases, we found that our data 718 aggregation method using the DFT basis yields a better reconstruction qual-719 ity compared to other bases. In future, we will pursue a thorough analysis of 720 this discrepancy and present theoretical guarantees. Another future direction 721 of the proposed work is to include the energy harvesting mechanism [43] to the 722 sensor nodes which helps in conserving the energy from renewable resources 723 (e.g., piezoelectric energy harvesters and thermoelectric devices) to extend the 724 network lifetime. Further, improving the robustness of the proposed data aggre-725 gation algorithm to the effects of dynamic characteristics of energy harvesting 726 (due to environmental impacts) [44] is another future direction of the proposed 727 work. Optimizing the energy required for data aggregation in the presence of 728 heterogeneity (with respect to energy resource and delay sensitivity) [45] of sen-729 sor nodes and channel interference is another future extension of the proposed 730 work. 731

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