

INDIAN INSTITUTE OF TECHNOLOGY KHARAGPUR MA20013 - Discrete Mathematics Problem Sheet 1 Spring 2020

Problem 1. Show that a graph G can not exist with vertices of degreees 2, 3, 4, 4, and 5.

Problem 2. Let G be a graph of order  $n \ge 2$ , and suppose that for every vertex v of G,  $deg(v) \ge \frac{(n-1)}{2}$ . Prove that G is connected.

Problem 3. Prove that every u-v trail contains a u-v path, and every circuit contains a cycle.

Problem 4. Let G be a connected graph containing only even vertices. Prove that G cannot contain a bridge,

Problem 5. Give an example of a connected graph containing more bridges than the cut-vertices.

Problem 6. Give an example of a connected graph containing more cut-vertices than the bridges.

Problem 7. If G is a connected graph on n vertices other than the complete graph. If e is a bridge of G, then, show that e is incident with a cut-vertex in G.

Problem 8. Let G be graph of order n and size m so that  $m \ge n \ge 3$ . Show that G must contain a cycle.

Problem 9. Let G be a graph such that for every vertex v of G,  $deg(v) \ge 2$ . Show that G contains a cycle.

Problem 10. Let T be a tree on  $n(\geq 3)$  vertices. Show that T contains two vertices of degree 1.