

# Problem set 5

Spring 2018

## MATHEMATICS-II (MA10002)(Numerical Analysis)

1. Find  $f(0.05)$  using the Newton's forward difference formula from the given table:

$x$	0	0.1	0.2	0.3	0.4
$f(x)$	1	1.2214	1.4918	1.8221	2.2255

2. Using Newton's forward difference formula find  $f(1.5)$  from the given table

$x$	0	2	4	6	8
$f(x)$	-1	13	43	89	151

3. Given:

$x$	2.0	2.2	2.4	2.6	2.8	3.0
$f(x) = \log_{10} x$	0.30103	0.34242	0.38021	0.41497	0.44716	0.47721

Find the value of  $\log_{10} 2.91$  using Newton's backward difference formula.

4. Find the value of  $f(1.45)$  using Newton's backward difference formula.

$x$	1.0	1.1	1.2	1.3	1.4	1.5
$f(x)$	0.24197	0.21785	0.19419	0.17137	0.14973	0.12952

5. In an examination the number of candidates who secured marks between certain limit were as follows:

Marks	0-19	20-39	40-59	60-89	80-99
No. of candidates	41	62	65	50	17

Estimate the number of candidates getting marks less than 70.

6. A certain function  $f$ , defined on the interval  $(0, 1)$  is such that  $f(0) = 0$ ,  $f(1/2) = -1$ ,  $f(1) = 0$ . Find the quadratic polynomial  $p(x)$  which agrees with  $f(x)$  for  $x = 0, 1/2, 1$ .  
If  $|\frac{d^3 f}{dx^3}| \leq 1$  for  $0 \leq x \leq 1$ . Show that  $|f(x) - p(x)| \leq \frac{1}{12}$  for  $0 \leq x \leq 1$ .

7. Show that the sum of Lagrangian functions or coefficients is unity, i.e.,  $\sum_{r=0}^n w_r(x) = 1$ .

8. Use Lagrange's formula to find the value of  $y$  when  $x = 102$ , from the given data:

$x$	93	96.2	100	104.2	108.7
$y = f(x)$	11.38	12.80	14.70	17.07	19.91

9. Find by Lagrange's formula the interpolation polynomial which corresponds to the following data:

$x$	-1	0	2	5
$f(x)$	9	5	3	15

10. Evaluate  $\int_0^1 (4x - 3x^2)dx$ , taking ten equal intervals, by (i) trapezoidal rule, (ii) Simpson's one-third rule. Compute the exact value and find the errors in your result.

11. Evaluate  $\int_0^1 \frac{1}{1+x^2} dx$ , by (i) trapezoidal rule and (ii) Simpson's one-third rule taking six equal intervals, correct up to three decimal places and find the errors in both the methods.

12. Find the value of  $\int_0^{\pi/2} e^{\sin x} dx$ , by (i) trapezoidal rule and (ii) Simpson's one-third rule taking  $h = \frac{\pi}{12}$ , correct up to five decimal places.

13. Find the value of  $\int_0^1 \cos x dx$ , taking five equal intervals. Explain the reason behind your choice of the integration formula used.