

Obscurum Higgs @ Colliders

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HEP Seminars @ IITH

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Istituto Nazionale di Fisica Nucleare
Sezione di Bologna

based on

[arXiv:2010.02597](#)

P. Bandyopadhyay, AC

Phys.Rev.D 103 (2021) 1

[arXiv:2005.10289](#)

AC, F. De Lillo, F. Maltoni, L. Mantani, O. Mattelaer, R. Ruiz and X. Zhao

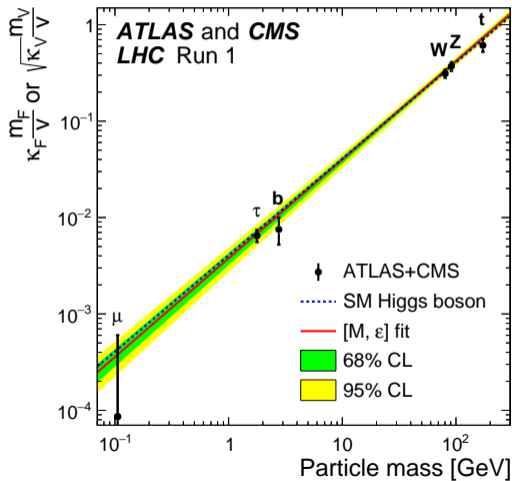
JHEP 09 (2020) 080

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- Introduction
- Simple SM Extension
- Phenomenology of cTSM
 - Dark Matter
 - Long-Lived Particles
 - Collider Signatures
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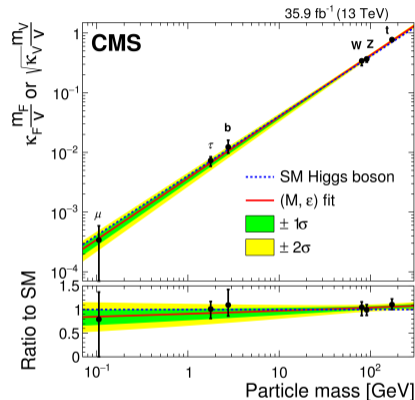
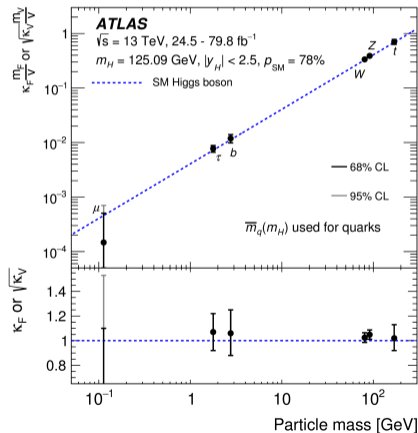
Introduction

The Higgs Boson @ LHC - (Run 1)



ATLAS and CMS, JHEP 08 (2016) 045

The Higgs Boson @ LHC - (Run 2)



ATLAS and CMS (Sopczak), PoS FFK2019 (2020) 006

Still Need for...



TOM GAULD for NEW SCIENTIST

...BSM Physics

Simple SM Extension

SM + Complex Triplet

Scalar Sector

$$\Phi = \begin{pmatrix} \varphi^+ \\ \Phi_0 \end{pmatrix} \quad T = \frac{1}{\sqrt{2}} \begin{pmatrix} t_0 & \sqrt{2} t_1^+ \\ \sqrt{2} t_2^- & -t_0 \end{pmatrix}$$

Massive Vector Bosons

$$m_W = \frac{1}{2} g_2 \sqrt{v^2 + 4v_T^2} \quad m_Z = \frac{1}{2} \sqrt{(g_1^2 + g_2^2)} v$$

⇓

$$v_T \lesssim 5 \text{ GeV}$$

SM + Complex Triplet: Scalar Spectrum

$$V = V_1 + V_2$$

$$V_1 = \mu^2 \Phi^\dagger \Phi + \frac{\lambda_H}{2} \Phi^\dagger \Phi \Phi^\dagger \Phi + m_T^2 \text{tr}[T^\dagger T] + \frac{\lambda_T}{2} \text{tr}[T^\dagger T] \text{tr}[T^\dagger T] + \frac{\lambda_{T'}}{2} \text{tr}[T^\dagger T T^\dagger T] \\ + \frac{\lambda_{HT}}{2} \Phi^\dagger \Phi \text{tr}[T^\dagger T] + \kappa_{HT} (\text{tr}[\Phi^\dagger T \Phi] + \text{h.c.})$$

$$V_2 = \left(m_T'^2 \text{tr}[T T] + \frac{\lambda_T^{(2)}}{2} \text{tr}[T T T T] + \frac{\lambda_T^{(3)}}{2} \text{tr}[T^\dagger T T T] \right. \\ \left. + \frac{\lambda_{HT}^{(2)}}{2} \Phi^\dagger \Phi \text{tr}[T T] \right) + \text{h.c.}$$

SM + Complex Triplet: Scalar Spectrum

After EWSB

$$m_{aP}^2 = \kappa_{HT} \frac{v^2}{2v_T} - 4m_T'^2 - \lambda_{HT}^{(2)} v^2 - (4\lambda_T^{(2)} + \lambda_T^{(3)}) v_T^2 \quad \leftarrow \text{pure state}$$

$$m_{h_T^\pm}^2 = \kappa_{HT} \left(\frac{v^2}{2v_T} + 2v_T \right)$$

$$m_{h_P^\pm}^2 = \kappa_{HT} \frac{v^2}{2v_T} - 4m_T'^2 - \lambda_{HT}^{(2)} v^2 - (2\lambda_T^{(2)} + \lambda_T^{(3)} + \frac{\lambda_{T'}}{2}) v_T^2 \quad \leftarrow \text{pure state}$$

$$m_{h_D}^2 = \lambda_H v^2 - 2\kappa_{HT} v_T + 2 \left(\lambda_{HT} + 2\lambda_{HT}^{(2)} - 2\lambda_H \right) v_T^2$$

$$m_{h_T}^2 = \frac{\kappa_{HT}}{2v_T} (v^2 + 4v_T^2) + \left(4\lambda_H - 2\lambda_{HT} - 4\lambda_{HT}^{(2)} + \lambda_T + \frac{\lambda_{T'}}{2} + 2(\lambda_T^{(2)} + \lambda_T^{(3)}) \right) v_T^2$$

Physical Pseudoscalar: Features

a_P is a pure pseudoscalar state



no interaction with fermions (triplet!)

pseudoscalar nature



no loop-level coupling with massless
gauge bosons

no interaction with massive gauge
bosons



pNG Dark Matter candidate

3-point vertices are $a_P W^\pm h_P^\mp$, $a_P a_P h_{D/T}$, ... (purity must be conserved in each vertex)

pNG Dark Matter: other Examples

Probing pseudo-Goldstone dark matter at the LHC #1

Katri Huitu (Helsinki U.), Niko Koivunen (Helsinki U.), Oleg Lebedev (Helsinki U.), Subhadeep Mondal (Helsinki U.), Takashi Toma (Kyoto U.) (Dec 14, 2018)

Published in: *Phys.Rev.D* 100 (2019) 1, 015009 • e-Print: 1812.05952 [hep-ph]

 pdf  DOI  cite

 23 citations

Is a Miracle-less WIMP Ruled Out?

Jason Arakawa, Tim M.P. Tait (Jan 26, 2021)

e-Print: 2101.11031 [hep-ph]

 pdf  cite

Direct and indirect probes of Goldstone dark matter #1

Tommi Alanne (Heidelberg, Max Planck Inst.), Matti Heikinheimo (Helsinki U. and Helsinki Inst. of Phys.), Venus Keus (Helsinki U. and Helsinki Inst. of Phys.), Niko Koivunen (Helsinki U. and Helsinki Inst. of Phys.), Kimmo Tuominen (Helsinki U. and Helsinki Inst. of Phys.) (Dec 14, 2018)

Published in: *Phys.Rev.D* 99 (2019) 7, 075028 • e-Print: 1812.05996 [hep-ph]

 pdf  DOI  cite

 15 citations

Pseudo-Nambu-Goldstone dark matter and two-Higgs-doublet models

Xue-Min Jiang (Zhongshan U. and Yunnan U.), Chengfeng Cai (Zhongshan U.), Zhao-Huan Yu (Zhongshan U.), Yu-Pan Zeng (Zhongshan U.), Hong-Hao Zhang (Zhongshan U.) (Jul 22, 2019)

Published in: *Phys.Rev.D* 100 (2019) 7, 075011 • e-Print: 1907.09684 [hep-ph]



 pdf  DOI  cite

 7 citations

Pseudo-Nambu-Goldstone dark matter from gauged $U(1)_{B-L}$ symmetry #1

Yoshihiko Abe (Kyoto U.), Takashi Toma (McGill U.), Koji Tsumura (Kyushu U.) (Jan 12, 2020)

Published in: *JHEP* 05 (2020) 057 • e-Print: 2001.03954 [hep-ph]



 pdf  DOI  cite

 7 citations

Pseudo Nambu-Goldstone Dark Matter: Examples of Vanishing Direct Detection Cross Section #1

Dimitrios Karamitros (NCBJ, Warsaw) (Jan 28, 2019)

Published in: *Phys.Rev.D* 99 (2019) 9, 095036 • e-Print: 1901.09751 [hep-ph]

 pdf  DOI  cite

Global fit of pseudo-Nambu-Goldstone Dark Matter #1

Chiara Arina (Louvain U., CP3), Ankit Beniwal (Louvain U., CP3), Céline Degrande (Louvain U., CP3), Jan Heisig (Louvain U., CP3), Andre Scaffidi (Melbourne U.) (Dec 9, 2019)

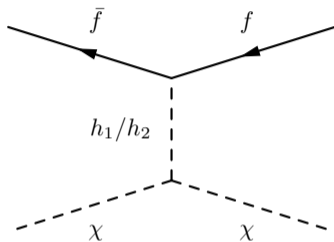
Published in: *JHEP*04 (2020) 015, *JHEP* 04 (2020) 015 • e-Print: 1912.04008 [hep-ph]

 pdf  DOI  cite

 15 citations

Why pNG Dark Matter?

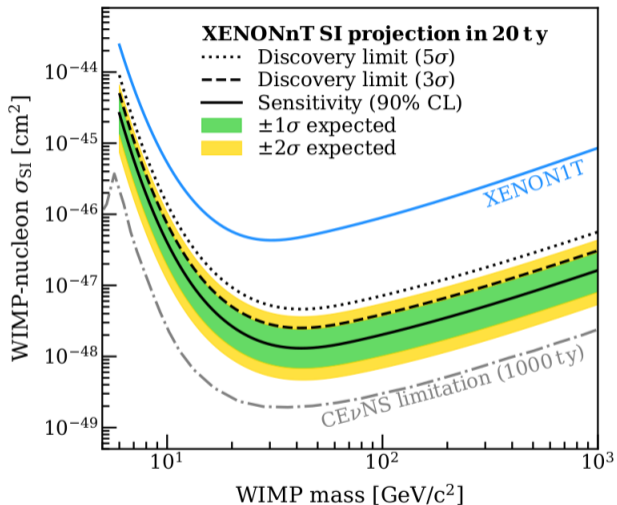
Tree-level amplitude for $\chi N \rightarrow \chi N$



$$\mathcal{A}_{ff} \propto \sin \theta \cos \theta \left(\frac{m_{h_2}^2}{t - m_{h_2}^2} - \frac{m_{h_1}^2}{t - m_{h_1}^2} \right) \sim \sin \theta \cos \theta t \frac{m_{h_2}^2 - m_{h_1}^2}{m_{h_1}^2 m_{h_2}^2} \sim 0$$

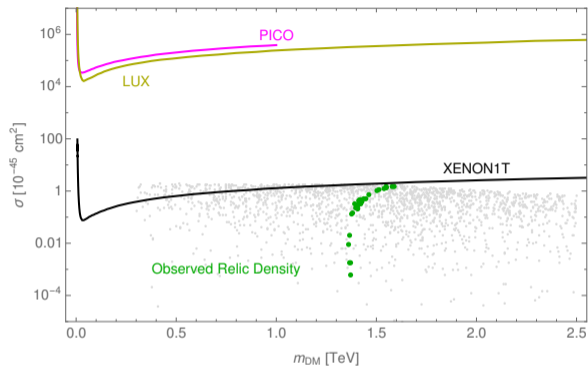
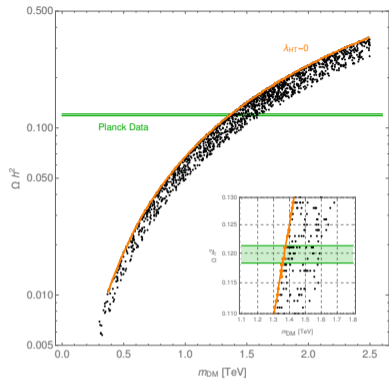
cancellation spoiled at loop level and/or with higher-order breaking terms

Why pNG Dark Matter?



Phenomenology of cTSM

Dark Matter Phenomenology: Relic Density and Direct Detection



generated with MadDM

$$m_{h_D} = 125.18 \pm 0.16 \text{ GeV} \quad |\mathcal{R}_{11}^S| \geq 99/100$$

$$\mu_{\gamma\gamma} = \Gamma_{h \rightarrow \gamma\gamma}^{\text{SM}} / \Gamma_{\Phi \rightarrow \gamma\gamma} \longrightarrow \mu_{\gamma\gamma}^{\text{ATLAS}} = 0.99_{-0.14}^{+0.15}, \quad \mu_{\gamma\gamma}^{\text{CMS}} = 1.10_{-0.18}^{+0.20}$$

Long-Lived Charged Particle

Pure charged Higgs h_P^\pm only possible decay is

$$h_P^\pm \rightarrow a_P (W^\pm)^*$$

with

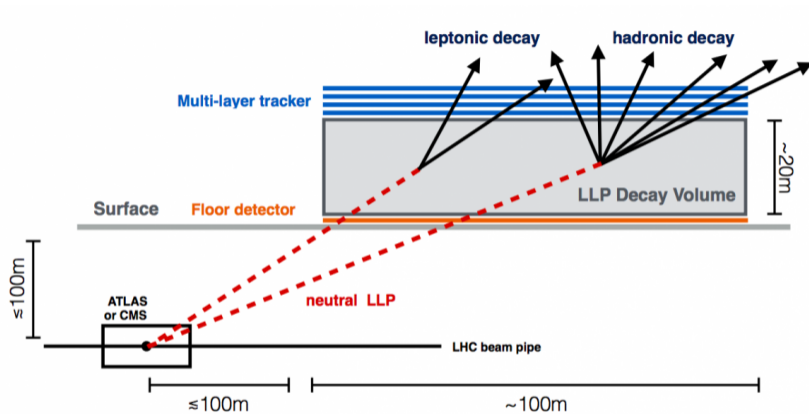
$$\frac{d\Gamma}{dx_1 dx_2} (h_P^\pm \rightarrow a_P W^{*\pm} \rightarrow a_P ff') = \frac{9}{8\pi^3} G_F^2 m_W^4 m_{h_P^\pm} F_{a_P W^\pm}(x_1, x_2)$$

\Downarrow

$$\tau_{h_P^\pm} = \mathcal{O}(10^{15}) \text{ GeV}^{-1} = \mathcal{O}(1) \text{ m}$$

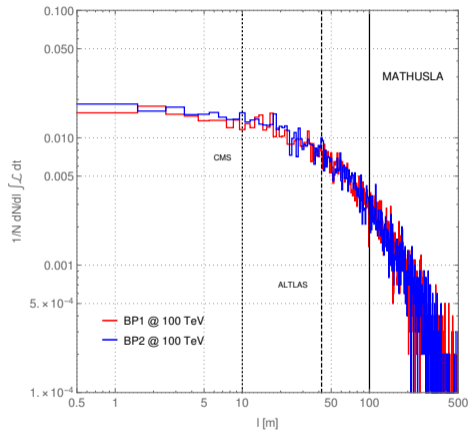
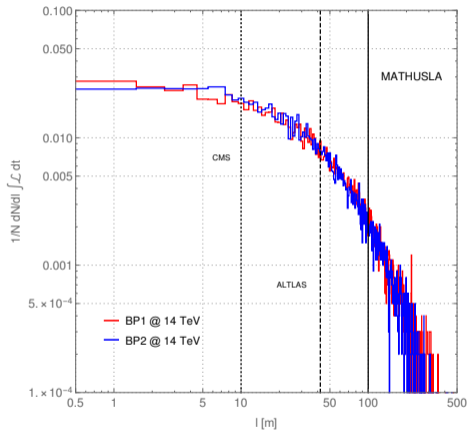
h_P^\pm is a long-lived state

Long-Lived Charged Particle



Beacham, Exploring the Lifetime Frontier at the LHC and Beyond

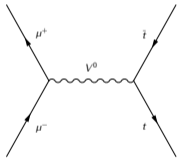
Long-Lived Charged Particle



Generic Process at μ Collider

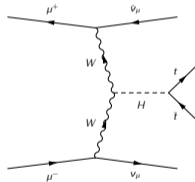
Different class of processes are relevant at different \sqrt{s}

$\sqrt{s} \lesssim 5 \text{ TeV}$
s-channel



$$\sigma \sim \frac{1}{s}$$

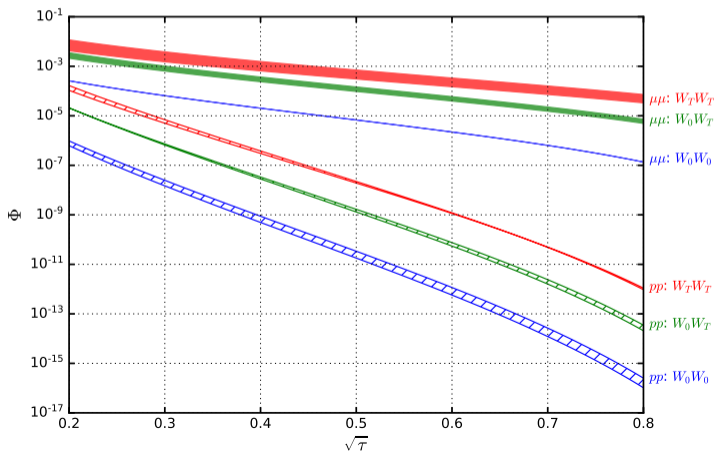
$\sqrt{s} \gtrsim 5 \text{ TeV}$
VBF



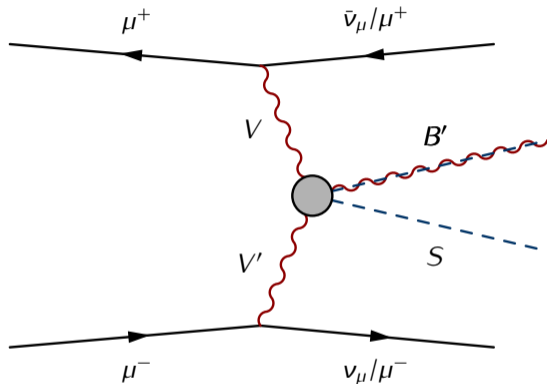
$$\sigma \sim \frac{1}{M^2} \log^n \frac{\sqrt{s}}{M}$$

Lepton vs. Hadron Colliders

$$\Phi_{W_{\lambda_1}^+ W_{\lambda_2}^-}(\tau, \mu_f) = \int_{\tau}^1 \frac{d\xi}{\xi} f_{W_{\lambda_1}/\mu}(\xi, \mu_f) f_{W_{\lambda_2}/\mu}\left(\frac{\tau}{\xi}, \mu_f\right)$$



cTSM @ multi-TeV μ Collider

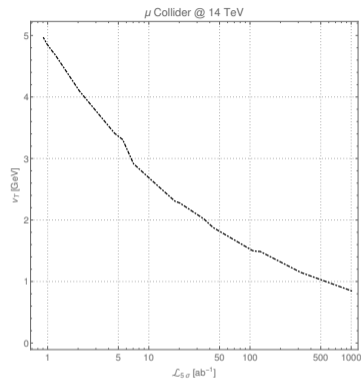
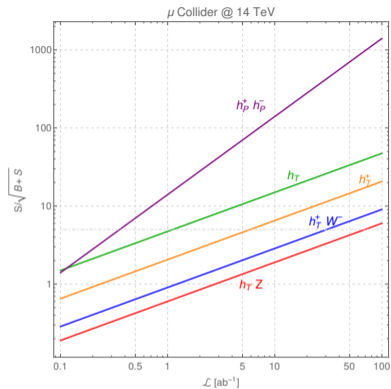


S is a scalar boson, B' can be either a scalar or a massive vector boson, V, V' are vector bosons

cTSM @ multi-TeV μ Collider

Production modes	σ [fb]			
	$\sqrt{s} = 14$ TeV		$\sqrt{s} = 30$ TeV	
	BP1	BP2	BP1	BP2
$\mu^+ \mu^- \rightarrow h_T v_\mu \tilde{\nu}_\mu$	$1.8 \cdot 10^{-2}$	$6.2 \cdot 10^{-1}$	$2.9 \cdot 10^{-2}$	$9.6 \cdot 10^{-1}$
$\mu^+ \mu^- \rightarrow h_T^+ \mu^- \tilde{\nu}_\mu$	$5.3 \cdot 10^{-3}$	$1.8 \cdot 10^{-1}$	$8.4 \cdot 10^{-3}$	$2.8 \cdot 10^{-1}$
$\mu^+ \mu^- \rightarrow h_T h_T v_\mu \tilde{\nu}_\mu$	$1.9 \cdot 10^{-2}$	$2.0 \cdot 10^{-2}$	$4.8 \cdot 10^{-2}$	$5.1 \cdot 10^{-2}$
$\mu^+ \mu^- \rightarrow a_P a_P v_\mu \tilde{\nu}_\mu$	$1.8 \cdot 10^{-2}$	$2.0 \cdot 10^{-2}$	$4.7 \cdot 10^{-2}$	$5.0 \cdot 10^{-2}$
$\mu^+ \mu^- \rightarrow h_T^+ h_T^- v_\mu \tilde{\nu}_\mu$	$1.3 \cdot 10^{-2}$	$1.4 \cdot 10^{-2}$	$3.4 \cdot 10^{-2}$	$3.6 \cdot 10^{-2}$
$\mu^+ \mu^- \rightarrow h_P^+ h_P^- v_\mu \tilde{\nu}_\mu$	$1.3 \cdot 10^{-2}$	$1.4 \cdot 10^{-2}$	$3.4 \cdot 10^{-2}$	$3.6 \cdot 10^{-2}$
$\mu^+ \mu^- \rightarrow h_D h_T v_\mu \tilde{\nu}_\mu$	$1.6 \cdot 10^{-4}$	$5.7 \cdot 10^{-3}$	$3.7 \cdot 10^{-4}$	$1.3 \cdot 10^{-2}$
$\mu^+ \mu^- \rightarrow h_D h_T^+ \mu^- \tilde{\nu}_\mu$	$4.8 \cdot 10^{-5}$	$1.6 \cdot 10^{-3}$	$1.1 \cdot 10^{-4}$	$3.8 \cdot 10^{-3}$
$\mu^+ \mu^- \rightarrow h_T Z v_\mu \tilde{\nu}_\mu$	$7.7 \cdot 10^{-4}$	$2.6 \cdot 10^{-2}$	$1.7 \cdot 10^{-3}$	$5.6 \cdot 10^{-2}$
$\mu^+ \mu^- \rightarrow h_T W^+ \mu^- \tilde{\nu}_\mu$	$4.1 \cdot 10^{-4}$	$1.4 \cdot 10^{-2}$	$1.0 \cdot 10^{-3}$	$3.4 \cdot 10^{-2}$
$\mu^+ \mu^- \rightarrow h_T^+ Z \mu^- \tilde{\nu}_\mu$	$1.4 \cdot 10^{-4}$	$4.8 \cdot 10^{-3}$	$3.6 \cdot 10^{-4}$	$1.2 \cdot 10^{-2}$
$\mu^+ \mu^- \rightarrow h_T^+ W^- v_\mu \tilde{\nu}_\mu$	$9.7 \cdot 10^{-4}$	$3.2 \cdot 10^{-2}$	$1.9 \cdot 10^{-3}$	$6.1 \cdot 10^{-2}$

cTSM @ multi-TeV μ Collider



background is $VBF_{W^+W^-}$ or $VBF_{W^\pm Z}$ or $VBF_{W^+W^-Z}$
 with
 $M_{W^+W^-} = m_{h_T}$ or $M_{W^\pm Z} = m_{h_T^\pm}$

exclusion plot
 from VBF production of h_T

Conclusions

- == astonishing tests of the SM at the LHC but...BSM is still needed
- == simple extensions of the SM scalar sector can address DM pheno
- == interplay between collider and cosmological experiments
- == multi-TeV μ -collider is suitable for both precision AND discovery
- == multi-Higgs model can shed light on EWSB

A close-up photograph of a red cricket ball and a wooden cricket bat lying on a grassy field. The ball is in the foreground, slightly out of focus, showing its characteristic red color and white stitching. The bat is behind it, also slightly out of focus, showing its wooden texture and dark handle. The background is a soft, out-of-focus green field.

Thanks

Backup Slides

SM + Singlet

$$\mathcal{L} = \mathcal{L}_{\text{SM}} + \frac{1}{2} \partial_\mu \sigma \partial_\mu \sigma - \frac{1}{2} m_\sigma^2 \sigma^2 - \frac{\lambda_\sigma}{4!} \sigma^4 - \frac{\kappa_\sigma}{2} \sigma^2 \Phi^\dagger \Phi.$$

$$\langle \sigma \rangle = v_s$$

$$\lambda_{hhh} = -\frac{3m_h^2}{v v_s} (v_s \cos^3 \theta + v \sin^3 \theta)$$

$$\lambda_{sss} = \frac{3m_s^2}{v v_s} (v \cos^3 \theta - v_s \sin^3 \theta)$$

$$\lambda_{hss} = -\frac{(m_h^2 + 2m_s^2)}{2v v_s} \sin 2\theta (v \cos \theta + v_s \sin \theta)$$

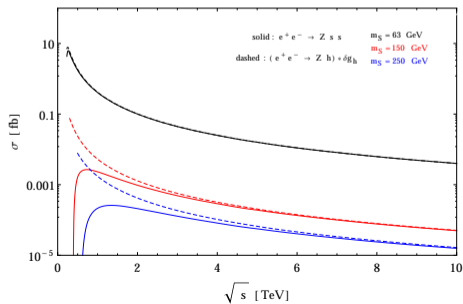
$$\lambda_{hhs} = \frac{(2m_h^2 + m_s^2)}{2v v_s} \sin 2\theta (v_s \cos \theta - v \sin \theta)$$

SM + Singlet: Inert Pair Production vs. Loop Corrections

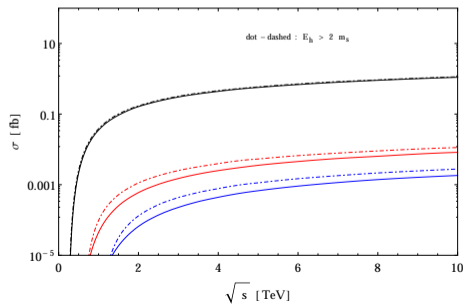
$$\delta g_h = -\frac{\kappa_\sigma^2 v^2}{16\pi^2 m_h^2} \left(1 - 4m_S^2 \frac{\tan^{-1} \sqrt{\frac{m_h^2}{(4m_S^2 - m_h^2)}}}{\sqrt{m_h^2(4m_S^2 - m_h^2)}} \right)$$

Heinemann, Nir, Phys.Usp. 62 (2019) no.9, 920-930

s-channel



VBF



2HDM

$$\begin{aligned} V = & \mu_1 \Phi_1^\dagger \Phi_1 + \mu_2 \Phi_2^\dagger \Phi_2 + \left(\mu_3 \Phi_1^\dagger \Phi_2 + \text{H.c.} \right) + \lambda_1 \left(\Phi_1^\dagger \Phi_1 \right)^2 + \lambda_2 \left(\Phi_2^\dagger \Phi_2 \right)^2 \\ & + \lambda_3 \left(\Phi_1^\dagger \Phi_1 \right) \left(\Phi_2^\dagger \Phi_2 \right) + \lambda_4 \left(\Phi_1^\dagger \Phi_2 \right) \left(\Phi_2^\dagger \Phi_1 \right) + \left(\lambda_5 \left(\Phi_1^\dagger \Phi_2 \right)^2 + \text{H.c.} \right) \\ & + \Phi_1^\dagger \Phi_1 \left(\lambda_6 \left(\Phi_1^\dagger \Phi_2 \right) + \text{H.c.} \right) + \Phi_2^\dagger \Phi_2 \left(\lambda_7 \left(\Phi_1^\dagger \Phi_2 \right) + \text{H.c.} \right) \end{aligned}$$

$$\Phi_1 \equiv \begin{pmatrix} -ih_1^+ \\ \frac{h_1^0 + ia_1 + v}{\sqrt{2}} \end{pmatrix} \quad \text{and} \quad \Phi_2 \equiv \begin{pmatrix} h_2^+ \\ \frac{h_2^0 + ia_2}{\sqrt{2}} \end{pmatrix}$$

$$\begin{pmatrix} h_1^0 \\ h_2^0 \end{pmatrix} = \begin{pmatrix} \cos \theta & \sin \theta \\ -\sin \theta & \cos \theta \end{pmatrix} \begin{pmatrix} h \\ H \end{pmatrix}$$

where h is identified as the observed, SM-like Higgs boson with $m_h \approx 125$ GeV and H is heavier with $m_H > m_h$

GM Model

$$\Phi = \begin{pmatrix} \varphi^{0*} & \varphi^+ \\ -\varphi^{+*} & \varphi^0 \end{pmatrix}, \quad X = \begin{pmatrix} \chi^{0*} & \xi^+ & \chi^{++} \\ -\chi^{+*} & \xi^0 & \chi^+ \\ \chi^{+++} & -\xi^{+*} & \chi^0 \end{pmatrix}$$

$$\begin{aligned} V(\Phi, X) = & \frac{\mu_2^2}{2} \text{Tr}(\Phi^\dagger \Phi) + \frac{\mu_3^2}{2} \text{Tr}(X^\dagger X) + \lambda_1 [\text{Tr}(\Phi^\dagger \Phi)]^2 + \lambda_2 \text{Tr}(\Phi^\dagger \Phi) \text{Tr}(X^\dagger X) \\ & + \lambda_3 \text{Tr}(X^\dagger X X^\dagger X) + \lambda_4 [\text{Tr}(X^\dagger X)]^2 - \lambda_5 \text{Tr}(\Phi^\dagger \tau^a \Phi \tau^b) \text{Tr}(X^\dagger t^a X t^b) \\ & - M_1 \text{Tr}(\Phi^\dagger \tau^a \Phi \tau^b) (UXU^\dagger)_{ab} - M_2 \text{Tr}(X^\dagger t^a X t^b) (UXU^\dagger)_{ab} \end{aligned}$$

Custodial Limit

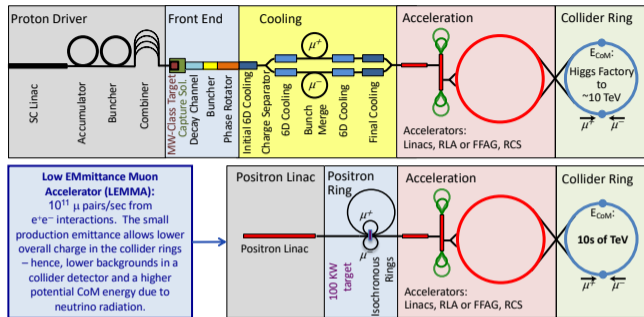
$$\langle \chi^0 \rangle = \langle \xi^0 \rangle \equiv v_X$$

$$(\sqrt{2}G_F)^{-1} = v_\varphi^2 + 8v_X^2$$

cTSM @ Hadron Colliders

Production modes	σ [fb]			
	$\sqrt{s} = 14$ TeV		$\sqrt{s} = 100$ TeV	
	BP1	BP2	BP1	BP2
$p p \rightarrow h_T$	$6.7 \cdot 10^{-7}$	$2.7 \cdot 10^{-5}$	$8.4 \cdot 10^{-5}$	$3.2 \cdot 10^{-3}$
$p p \rightarrow h_T^\pm$	$8.2 \cdot 10^{-7}$	$3.2 \cdot 10^{-5}$	$9.5 \cdot 10^{-5}$	$3.5 \cdot 10^{-3}$
$p p \rightarrow h_T h_T$	$2.3 \cdot 10^{-7}$	$1.6 \cdot 10^{-8}$	$4.3 \cdot 10^{-4}$	$2.7 \cdot 10^{-5}$
$p p \rightarrow a_P a_P$	$2.2 \cdot 10^{-7}$	$1.1 \cdot 10^{-9}$	$4.2 \cdot 10^{-4}$	$1.8 \cdot 10^{-6}$
$p p \rightarrow h_T^+ h_T^-$	$3.9 \cdot 10^{-3}$	$4.9 \cdot 10^{-3}$	$1.3 \cdot 10^0$	$1.4 \cdot 10^0$
$p p \rightarrow h_P^+ h_P^-$	$3.9 \cdot 10^{-3}$	$4.9 \cdot 10^{-3}$	$1.3 \cdot 10^0$	$1.4 \cdot 10^0$
$p p \rightarrow h_D h_T$	$1.5 \cdot 10^{-5}$	$5.4 \cdot 10^{-4}$	$5.1 \cdot 10^{-3}$	$1.8 \cdot 10^{-1}$
$p p \rightarrow h_D h_T^\pm$	$1.7 \cdot 10^{-6}$	$6.7 \cdot 10^{-5}$	$1.1 \cdot 10^{-4}$	$4.1 \cdot 10^{-3}$
$p p \rightarrow h_T Z$	$1.3 \cdot 10^{-6}$	$5.0 \cdot 10^{-5}$	$1.0 \cdot 10^{-4}$	$3.7 \cdot 10^{-3}$
$p p \rightarrow h_T W^\pm$	$1.9 \cdot 10^{-6}$	$7.3 \cdot 10^{-5}$	$1.2 \cdot 10^{-4}$	$4.3 \cdot 10^{-3}$
$p p \rightarrow h_T^\pm Z$	$1.9 \cdot 10^{-6}$	$7.5 \cdot 10^{-5}$	$1.2 \cdot 10^{-4}$	$4.4 \cdot 10^{-3}$
$p p \rightarrow h_T^+ W^-$	$2.4 \cdot 10^{-5}$	$9.1 \cdot 10^{-4}$	$4.2 \cdot 10^{-2}$	$1.5 \cdot 10^0$
$p p \rightarrow h_T p p'$	$3.1 \cdot 10^{-7}$	$1.4 \cdot 10^{-5}$	$7.9 \cdot 10^{-5}$	$3.9 \cdot 10^{-3}$
$p p \rightarrow h_T^\pm p p'$	$3.6 \cdot 10^{-7}$	$1.4 \cdot 10^{-5}$	$8.5 \cdot 10^{-5}$	$3.1 \cdot 10^{-3}$

μ Collider















J. P. Delahaye *et al.*, arXiv:1901.06150

Muon Accelerator Program
map.fnal.gov

Low EMittance Muon Accelerator
web.infn.it/LEMMA

New results on μ cooling by MICE collaboration
 Nature 508(2020)53

μ Collider: Interest is Growing...

 2101.10334	 2101.10469
 2101.04956	 2012.14818
 2012.03928	 2012.02769
 2011.03055	 2009.11287
 2008.12204	 2007.15684
 2007.14300	 2006.16277
 2003.13628	 1910.04170

...definitely a non-exhaustive list...

μ Collider: Pros and Cons

μ vs. e
(circular collider)

Pros 

- ✓ reduced synchrotron radiation
- ✓ increased \mathcal{L}
- ✓ cool physics

Cons 

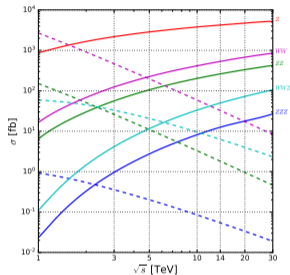
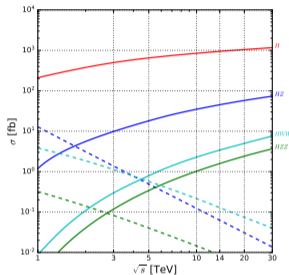
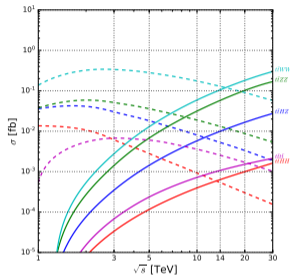
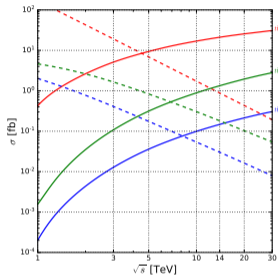
- ✗ μ decay
- ✗ ν radiation
- ✗ lots of R&D (true cons?)

μ Collider: SM Processes

$$\text{VBF} \equiv W^+W^- \rightarrow X \quad \text{s-ch.} \equiv \mu^+\mu^- \rightarrow X$$

σ [fb]	$\sqrt{s} = 1$ TeV		$\sqrt{s} = 3$ TeV		$\sqrt{s} = 14$ TeV		$\sqrt{s} = 30$ TeV	
	VBF	s-ch.	VBF	s-ch.	VBF	s-ch.	VBF	s-ch.
$t\bar{t}$	$4.3 \cdot 10^{-1}$	$1.7 \cdot 10^2$	$5.1 \cdot 10^0$	$1.9 \cdot 10^1$	$2.1 \cdot 10^1$	$8.8 \cdot 10^{-1}$	$3.1 \cdot 10^1$	$1.9 \cdot 10^{-1}$
$t\bar{t}Z$	$1.6 \cdot 10^{-3}$	$4.6 \cdot 10^0$	$1.1 \cdot 10^{-1}$	$1.6 \cdot 10^0$	$1.3 \cdot 10^0$	$1.8 \cdot 10^{-1}$	$2.8 \cdot 10^0$	$5.4 \cdot 10^{-2}$
$t\bar{t}H$	$2.0 \cdot 10^{-4}$	$2.0 \cdot 10^0$	$1.3 \cdot 10^{-2}$	$4.1 \cdot 10^{-1}$	$1.5 \cdot 10^{-1}$	$3.0 \cdot 10^{-2}$	$3.1 \cdot 10^{-1}$	$7.9 \cdot 10^{-3}$
$t\bar{t}WW$	$4.8 \cdot 10^{-6}$	$1.4 \cdot 10^{-1}$	$2.8 \cdot 10^{-3}$	$3.4 \cdot 10^{-1}$	$1.1 \cdot 10^{-1}$	$1.3 \cdot 10^{-1}$	$3.0 \cdot 10^{-1}$	$5.8 \cdot 10^{-2}$
$t\bar{t}ZZ$	$2.3 \cdot 10^{-6}$	$3.8 \cdot 10^{-2}$	$1.4 \cdot 10^{-3}$	$5.1 \cdot 10^{-2}$	$5.8 \cdot 10^{-2}$	$1.3 \cdot 10^{-2}$	$1.7 \cdot 10^{-1}$	$5.4 \cdot 10^{-3}$
$t\bar{t}HZ$	$7.1 \cdot 10^{-7}$	$3.6 \cdot 10^{-2}$	$3.5 \cdot 10^{-4}$	$3.0 \cdot 10^{-2}$	$1.0 \cdot 10^{-2}$	$5.3 \cdot 10^{-3}$	$2.7 \cdot 10^{-2}$	$1.9 \cdot 10^{-3}$
$t\bar{t}HH$	$7.2 \cdot 10^{-8}$	$1.4 \cdot 10^{-2}$	$3.4 \cdot 10^{-5}$	$6.1 \cdot 10^{-3}$	$6.4 \cdot 10^{-4}$	$5.4 \cdot 10^{-4}$	$1.6 \cdot 10^{-3}$	$1.5 \cdot 10^{-4}$
$t\bar{t}t\bar{t} (j)$	$5.1 \cdot 10^{-8}$	$5.4 \cdot 10^{-4}$	$6.8 \cdot 10^{-5}$	$6.7 \cdot 10^{-3}$	$1.1 \cdot 10^{-3}$	$2.5 \cdot 10^{-3}$	$2.1 \cdot 10^{-3}$	$1.0 \cdot 10^{-3}$
H	$2.1 \cdot 10^2$	-	$5.0 \cdot 10^2$	-	$9.4 \cdot 10^2$	-	$1.2 \cdot 10^3$	-
HH	$7.4 \cdot 10^{-2}$	-	$8.2 \cdot 10^{-1}$	-	$4.4 \cdot 10^0$	-	$7.4 \cdot 10^0$	-
HHH	$3.7 \cdot 10^{-6}$	-	$3.0 \cdot 10^{-4}$	-	$7.1 \cdot 10^{-3}$	-	$1.9 \cdot 10^{-2}$	-
HZ	$1.2 \cdot 10^0$	$1.3 \cdot 10^1$	$9.8 \cdot 10^0$	$1.4 \cdot 10^0$	$4.5 \cdot 10^1$	$6.3 \cdot 10^{-2}$	$7.4 \cdot 10^1$	$1.4 \cdot 10^{-2}$
HHZ	$1.5 \cdot 10^{-4}$	$1.2 \cdot 10^{-1}$	$9.4 \cdot 10^{-3}$	$3.3 \cdot 10^{-2}$	$1.4 \cdot 10^{-1}$	$3.7 \cdot 10^{-3}$	$3.3 \cdot 10^{-1}$	$1.1 \cdot 10^{-3}$
$HHHZ$	$1.5 \cdot 10^{-8}$	$4.1 \cdot 10^{-4}$	$4.7 \cdot 10^{-6}$	$1.6 \cdot 10^{-4}$	$1.9 \cdot 10^{-4}$	$1.6 \cdot 10^{-5}$	$5.1 \cdot 10^{-4}$	$5.4 \cdot 10^{-6}$
HWW	$8.9 \cdot 10^{-3}$	$3.8 \cdot 10^0$	$3.0 \cdot 10^{-1}$	$1.1 \cdot 10^0$	$3.4 \cdot 10^0$	$1.3 \cdot 10^{-1}$	$7.6 \cdot 10^0$	$4.1 \cdot 10^{-2}$
$HHWW$	$7.2 \cdot 10^{-7}$	$1.3 \cdot 10^{-2}$	$2.3 \cdot 10^{-4}$	$1.1 \cdot 10^{-2}$	$9.1 \cdot 10^{-3}$	$2.8 \cdot 10^{-3}$	$2.9 \cdot 10^{-2}$	$1.2 \cdot 10^{-3}$
HZZ	$2.7 \cdot 10^{-3}$	$3.2 \cdot 10^{-1}$	$1.2 \cdot 10^{-1}$	$8.2 \cdot 10^{-2}$	$1.6 \cdot 10^0$	$8.8 \cdot 10^{-3}$	$3.7 \cdot 10^0$	$2.5 \cdot 10^{-3}$
$HHZZ$	$2.4 \cdot 10^{-7}$	$1.5 \cdot 10^{-3}$	$9.1 \cdot 10^{-5}$	$9.8 \cdot 10^{-4}$	$3.9 \cdot 10^{-3}$	$2.5 \cdot 10^{-4}$	$1.2 \cdot 10^{-2}$	$9.5 \cdot 10^{-5}$
WW	$1.6 \cdot 10^1$	$2.7 \cdot 10^3$	$1.2 \cdot 10^2$	$4.7 \cdot 10^2$	$5.3 \cdot 10^2$	$3.2 \cdot 10^1$	$8.5 \cdot 10^2$	$8.3 \cdot 10^0$
ZZ	$6.4 \cdot 10^0$	$1.5 \cdot 10^2$	$5.6 \cdot 10^1$	$2.6 \cdot 10^1$	$2.6 \cdot 10^2$	$1.8 \cdot 10^0$	$4.2 \cdot 10^2$	$4.6 \cdot 10^{-1}$
WWZ	$1.1 \cdot 10^{-1}$	$5.9 \cdot 10^1$	$4.1 \cdot 10^0$	$3.3 \cdot 10^1$	$5.0 \cdot 10^1$	$6.3 \cdot 10^0$	$1.0 \cdot 10^2$	$2.3 \cdot 10^0$
ZZZ	$2.3 \cdot 10^{-2}$	$9.3 \cdot 10^{-1}$	$9.6 \cdot 10^{-1}$	$3.5 \cdot 10^{-1}$	$1.2 \cdot 10^1$	$5.4 \cdot 10^{-2}$	$2.7 \cdot 10^1$	$1.9 \cdot 10^{-2}$

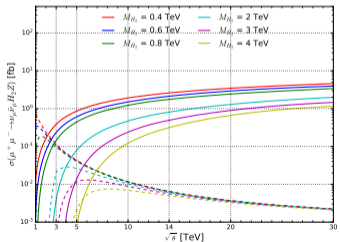
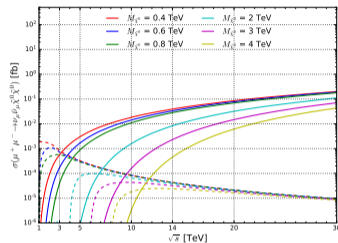
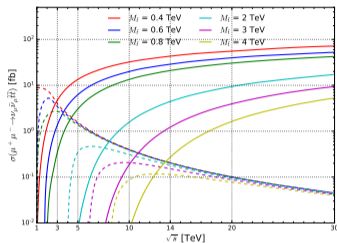
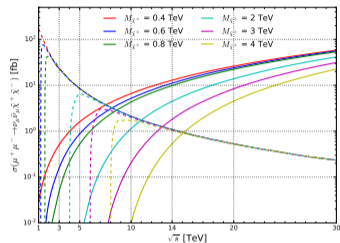
μ Collider: SM Processes



heavier final state \rightarrow larger \sqrt{s} for t-channel to win

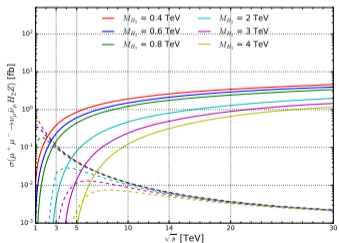
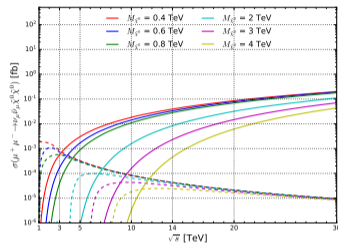
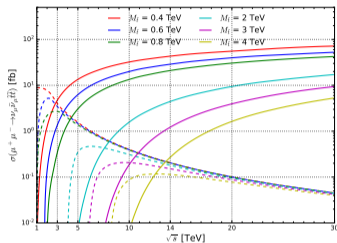
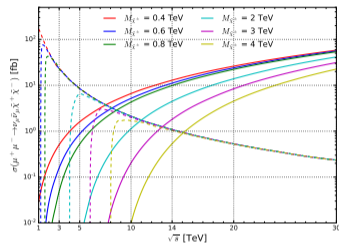
possible exceptions, e.g. HZZ vs HWW , ZZZ vs WWZ

VBF for various BSM Models



results are qualitatively similar for
SM+Singlet, 2HDM, GM Model, VLQ Models,
MSSM, Heavy Neutrino Models, etc.

VBF for various BSM Models

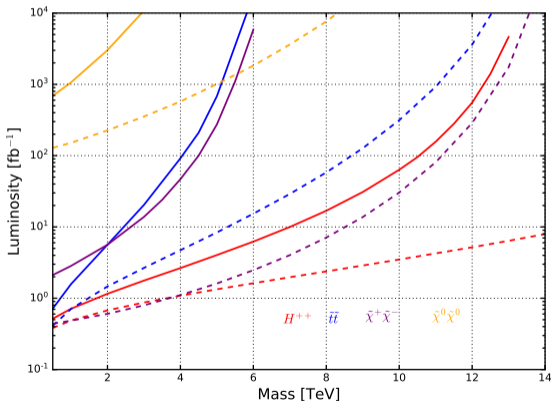


$$\frac{\sigma^{VBF}}{\sigma^{s-ch.}} \sim \frac{s}{m_X^2} \log^2 \frac{s}{m_V^2} \log \frac{s}{m_X^2}$$

New Physics Reach (via VBF) @ μ Collider

$$\mathcal{L} \equiv \frac{\# \text{ events}}{\sigma}$$

dashed lines $\rightarrow \sqrt{s} = 30$ TeV
solid lines $\rightarrow \sqrt{s} = 14$ TeV



Luminosity required for 25 events, with assumed zero background