# Term Project Submission Vehicle Dynamics



Cornering of Vehicle
(Based on Understeer Gradient Theory)

#### Submitted By:

AAKASH JADHAV (ME15MTECH11018)

**BIJOY PAL (ME15MTECH11021)** 

PANKAJ PANDYA (ME15MTECH11026)

UTTAM KUMAR MAHATO (ME15MTECH11008)

#### **Major Aspects**

- Car Body
- Overview
- Bicycle model
- Very slow speed cornering
- High speed cornering
- Understeer gradient
- Stability analysis with Graphs
- Conclusion
- References

# Car Body

A surface model of AUDI RS4 B7 (Sedan) [5] Made in Solid Works Design Software



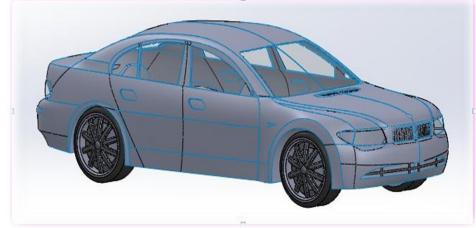
Side View of Solid part after and before rendering in preview mode



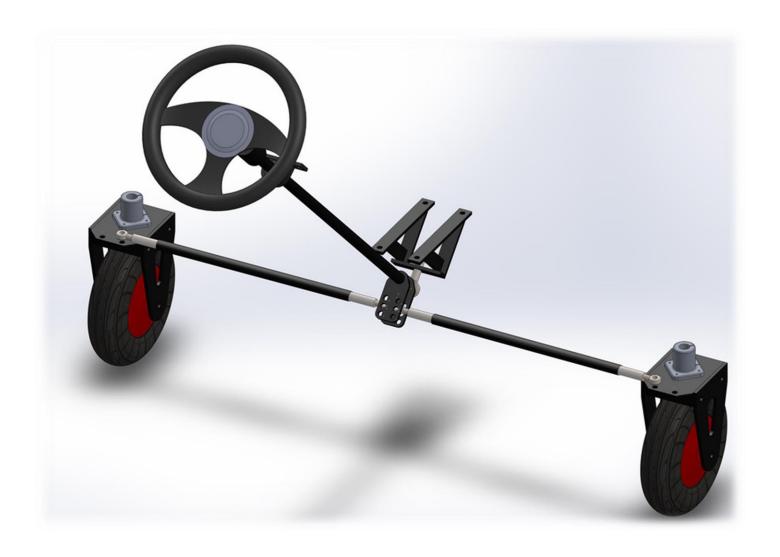


Oblique View of Solid part after and before rendering in preview mode





#### **Steering Assembly**



#### Overview

- Controllability of the vehicle.
  - Disturbances
  - Dynamic responses.

- Consequences as a output.
  - Environmental input
  - Feedback from the automobile system
  - Driver motive

### Bicycle model

- Simplified model
  - Basic representation
- Neglecting minor effects
  - Longitudinal and lateral load transfer
  - Rolling and pitching motion
  - Aerodynamic and suspension compliance effect.
- Degree of freedom
  - Lateral velocity (v)
  - Yaw velocity (r)

# Very slow speed cornering

- Governing parameters
  - Slip angles
  - Lateral accelerations
- Ackermann steering angle

$$-\delta = \frac{L}{R}$$

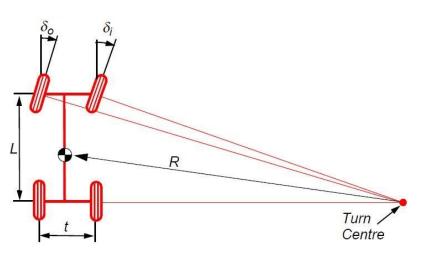


Figure: Slow Speed Cornering [1]

# High speed cornering

- Governing parameters
  - Slip angles
  - Lateral accelerations

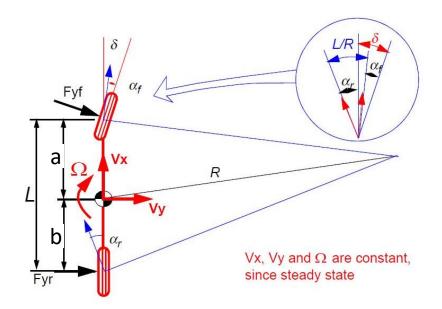


Figure: High Speed Cornering [1]

# High speed cornering

- Other dynamic parameters
  - Slip angles for body ,front and rear axle

• 
$$\beta = \frac{v}{V}$$
;  $\alpha_F = \frac{v + ar}{V} - \delta$ ;  $\alpha_R = \frac{v - br}{V}$ .

Cornering stiffness

• 
$$C_{\alpha} = \frac{F_{y}}{\alpha}$$
.

Load on front and rear axle

• 
$$W_f = \frac{Wb}{L}$$
;  $W_r = \frac{Wa}{L}$ .

### High speed cornering

- Moment equilibrium gives
  - $\bullet \ F_{yf}a F_{yr}b = 0.$
- Tire forces

• 
$$F_{yf} = \frac{W_f V^2}{gR}$$
;  $F_{yr} = \frac{W_r V^2}{gR}$ .

Understeer gradient

• 
$$K = \frac{W_f}{gC_{af}} - \frac{W_r}{gC_{ar}}$$
.

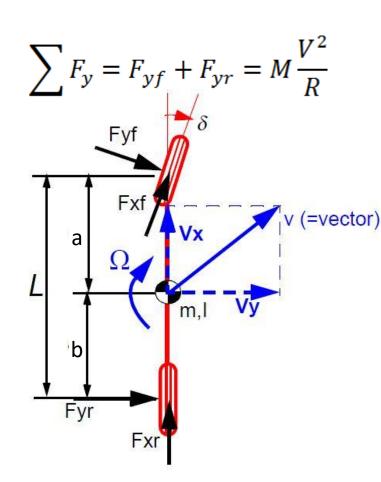


Figure: High Speed Cornering [1]

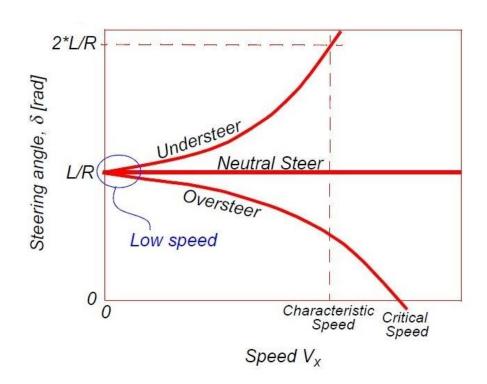
#### Understeer gradient

- Conditions for understeer gradient
  - Positive
  - Zero
  - Negetive
- Characteristic speed

$$- V = \sqrt{\frac{57.3Lg}{K}}.$$

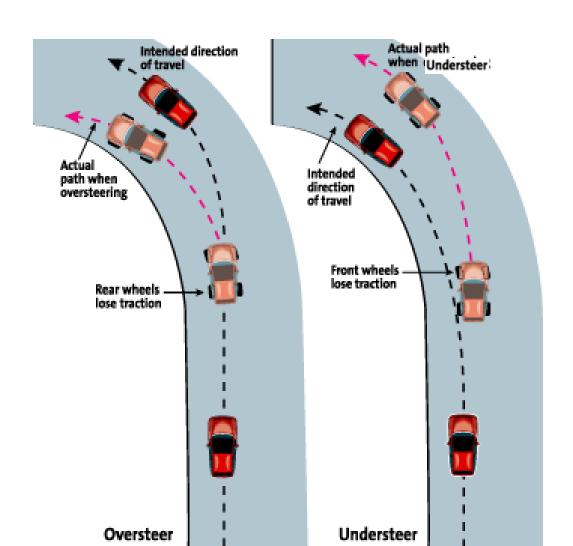
Critical speed

$$-V = \sqrt{-\frac{57.3Lg}{K}}.$$



K=0 Neutral Steer K>0 Under Steer K<0 Over Steer

#### Understeer, Over steer and Neutral steer



#### Stability analysis with Graphs using CARSIM

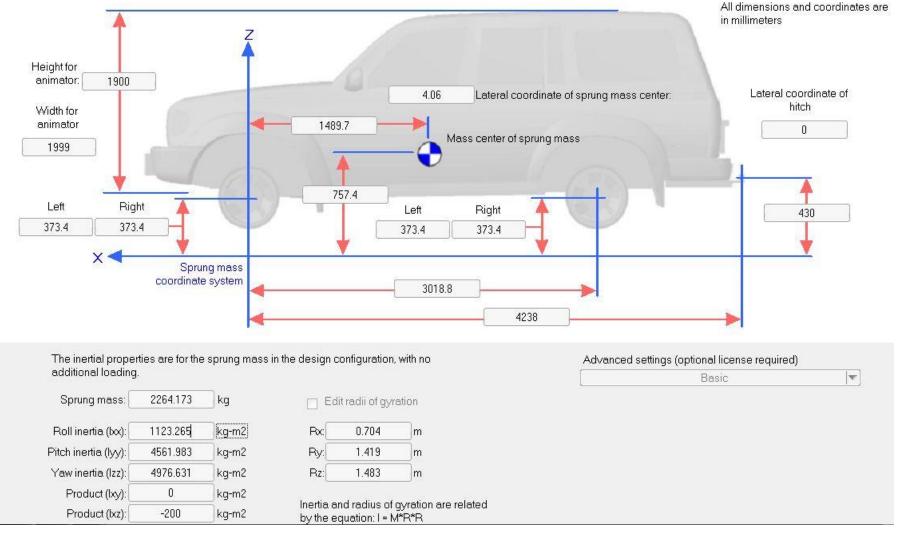
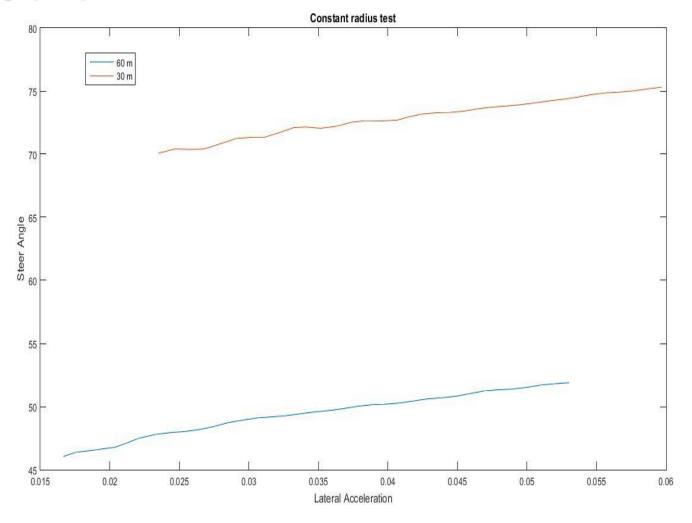
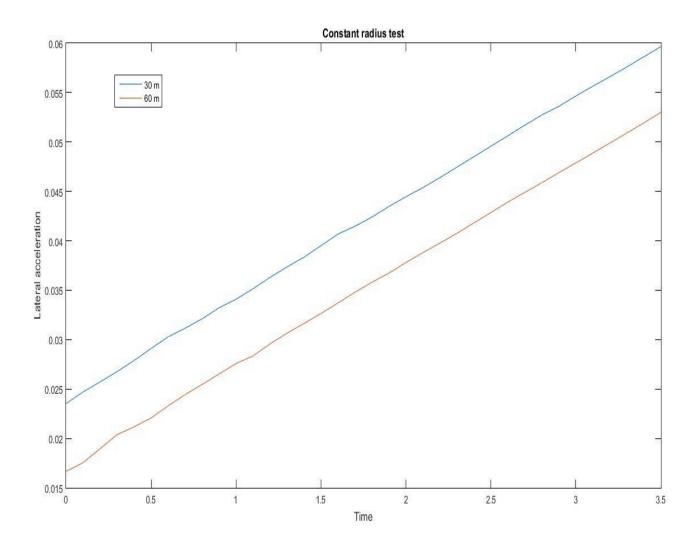


Figure: Vehicle Sprung Mass Model [4]

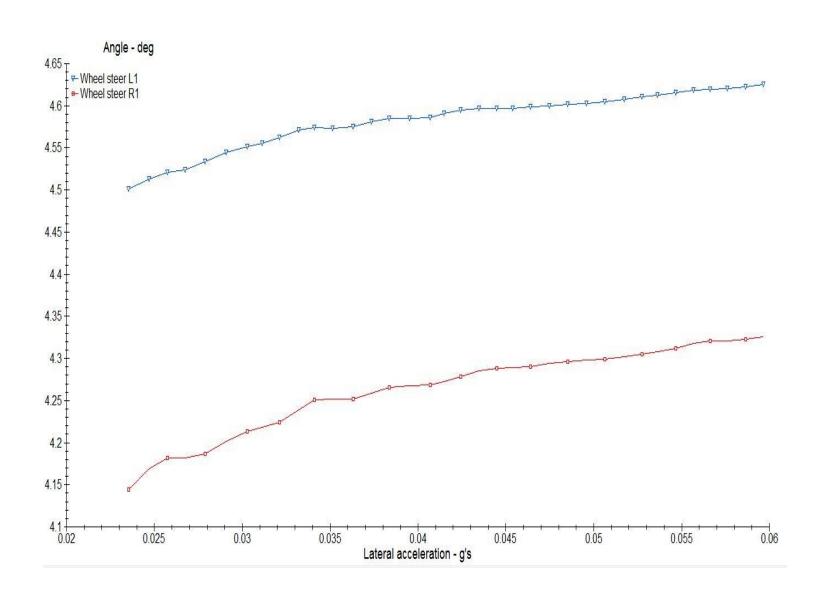
# Constant Radius Test: At 60 and 30m, Lateral Acceleration vs. Steer Angle[2&7]



# Constant Radius Test: At 60 and 30m, Lateral Acceleration vs. Time[2&7]



#### Front wheel steering angle vs. Lateral Acceleration[2&7]



#### Conclusion

- Figure discussed above shows the comparison of lateral acceleration versus time for different radius values. The rate of build up of lateral acceleration is observed to be higher for the smaller radius(30m).
- Lateral acceleration with respect to steer angel for front axle wheels has also been plotted for different radius values. Left wheel (inside one) steers most when we turn left
- The current procedure for executing the constant steer understeer test and the methodology used for calculation of understeer gradient does not take into account the change in the road wheel angles during the course of the test. Hence, there is a need for a better procedure to address this issue. The understeer gradient calculation techniques based on the bicycle model have simplifications and do not take into account the effects of the system compliance.

#### References

- 1. Gillespie T. D., Fundamentals of Vehicle Dynamics, Published by Society of automotive engineers
- Mechanical Simulation Corporation. CarSim mechanical simulation references and help files.
- MIT Open Access Article, On Steady-State Cornering Equilibria for Wheeled Vehicles with Drift
- 4. Evaluation of Vehicle Understeer Gradient Definitions, University of Ohio, and Loughborough University
- 5. Blue Prints for making Solid Surface Model of car <a href="http://carblueprints.info/rus/view/audi/audi-rs4-2005">http://carblueprints.info/rus/view/audi/audi-rs4-2005</a>
- 6. <a href="http://www.carsim.com/products/carsim/packages.php#Basicon/packages.php#Basicon/packages.p
- 7. Matlab Help Section