

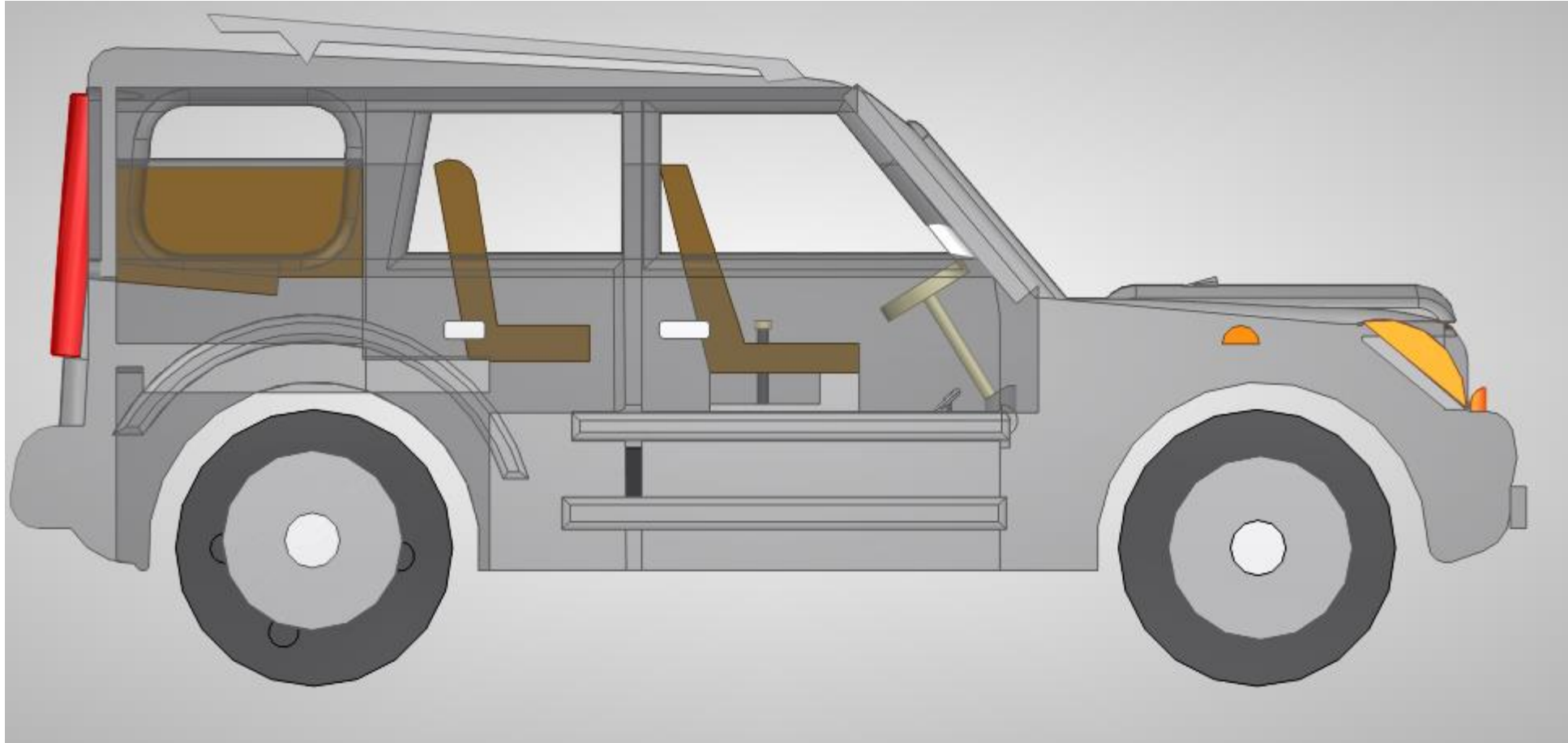
Driver model

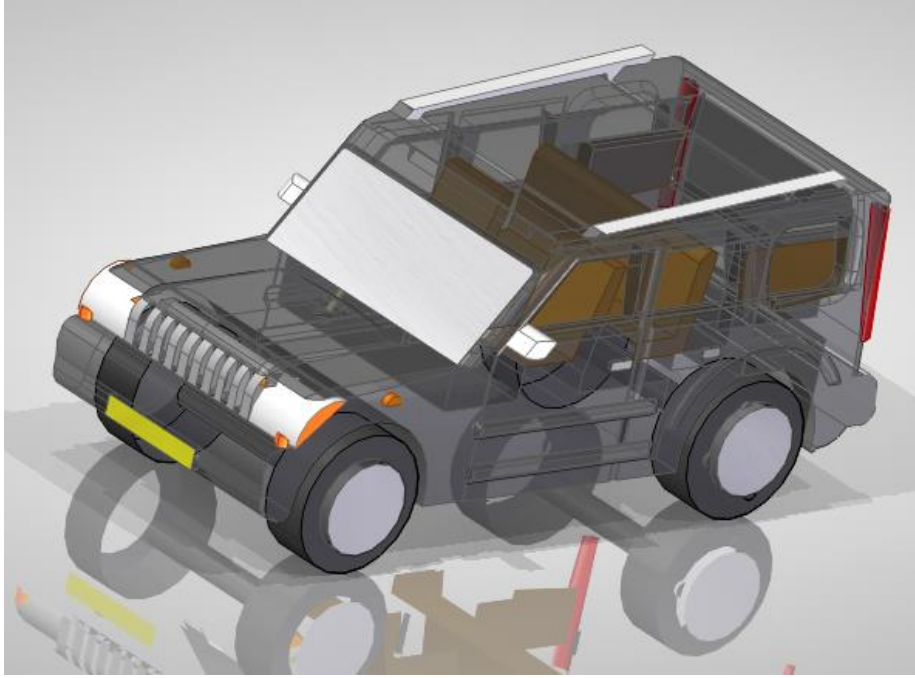
BIBIN S	ME13M1004
SAMUKHAM SURYA	ME13M1012
SANTHOSH KUMAR	ME13M1007
VINU V	ME13M1016
ANWAR SADATH	ME12M14P0 00001
RAGHAVENDRA ADITYA	ME10B007
MADHAVA RAMESH	ME11B038

3D CAD Model Of Mahindra Scorpio



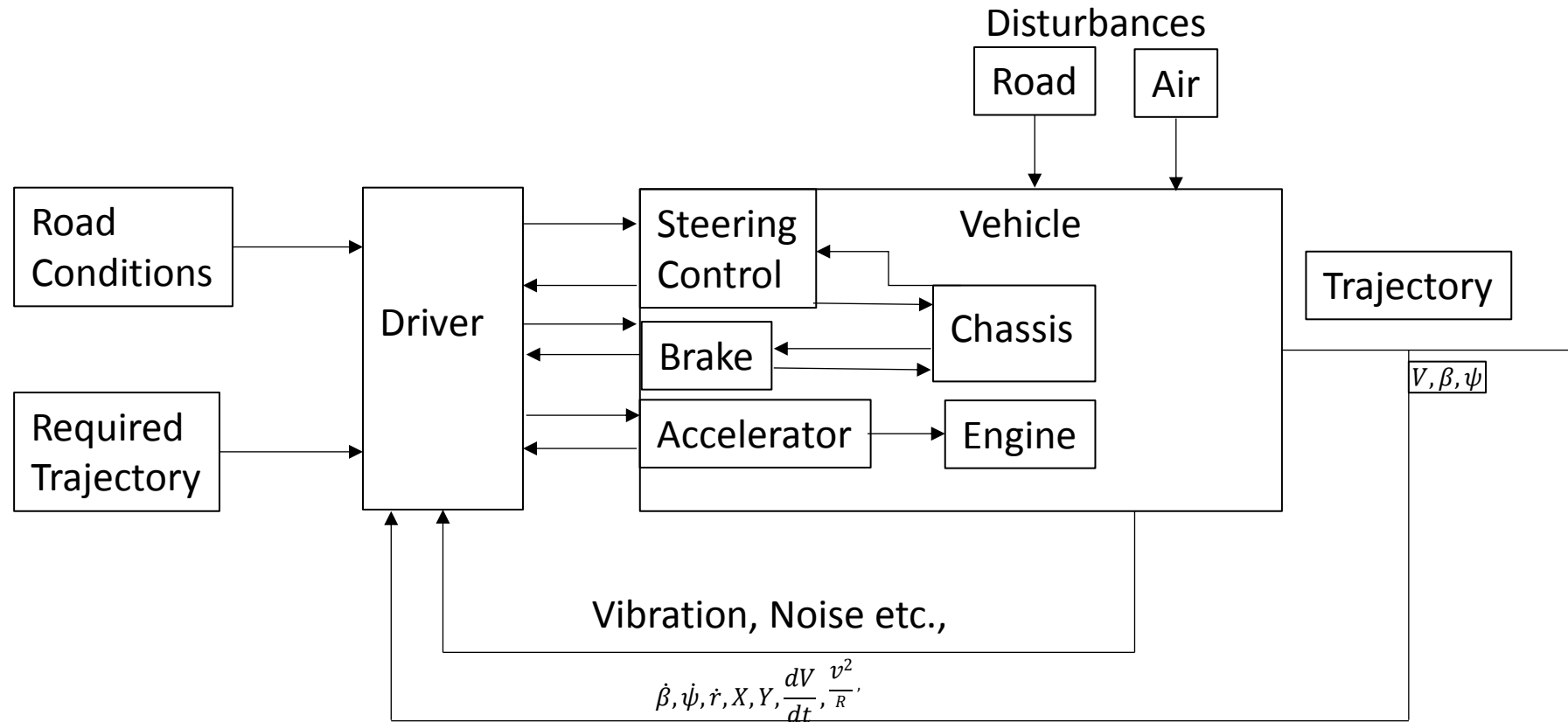
3D CAD Model Of Mahindra Scorpio





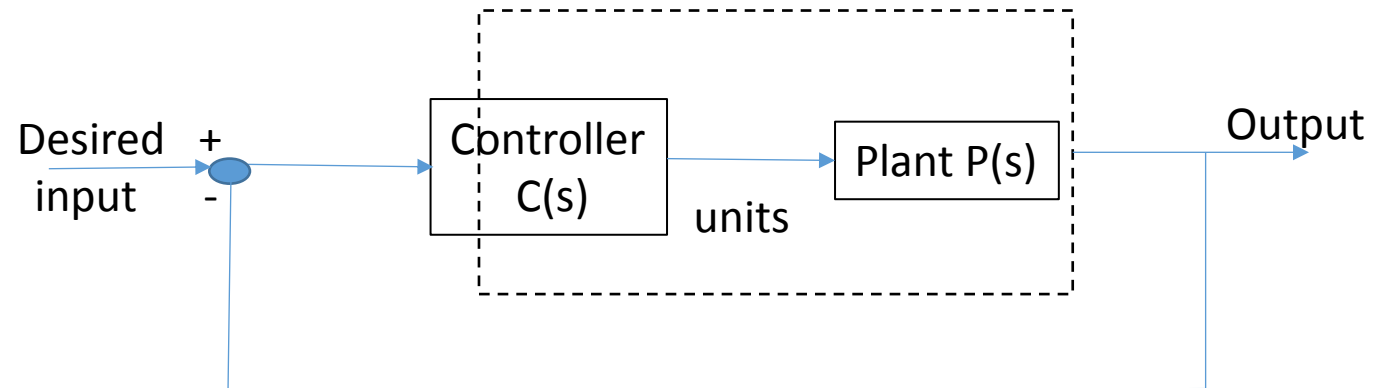
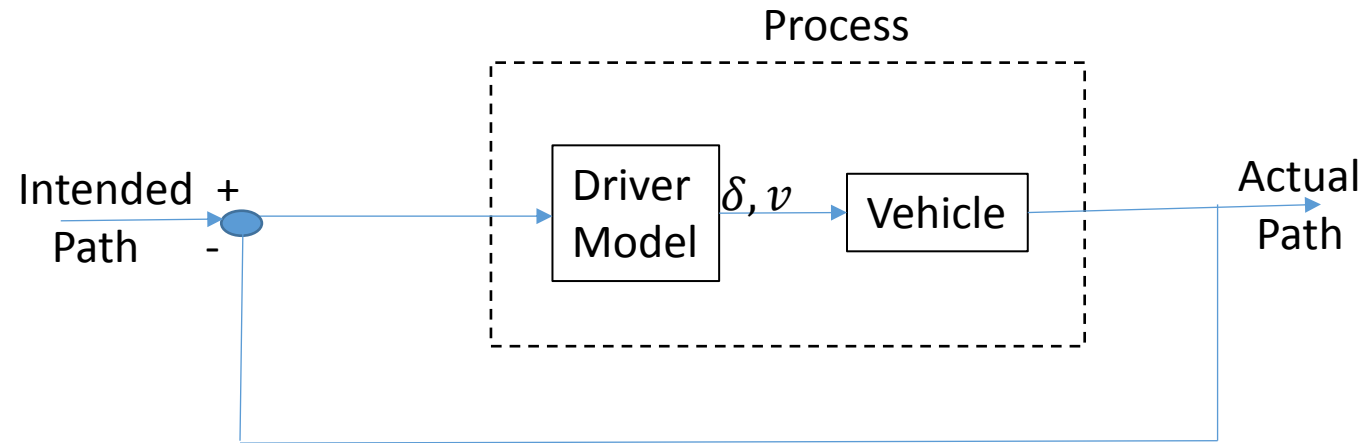
Introduction

- A driver model is a mathematical model which replicates the functionality of a driver(controlling , monitoring and stabilizing a vehicle)during various maneuvers .



Simplified scheme of the simplified vehicle-Driver System

Driver – vehicle 1-D model



Proposed driver models

- Driver model(PID controller):
 - Simple linearized driver model with and without delay
 - Path following driver model.
 - Path following driver model which minimizes lateral deviation and heading error according to a previewed path function and improves stability by regulating yaw and lateral disturbances during maneuvers.
- Vehicle Model
 - Rigid body model under neutral steering condition.

- Simple linearized driver model with out delay

$$\delta(t + \tau) = -K_g[\varphi(t) - \varphi(t)]$$

$$\tau\dot{\delta}(t) + \delta(t) = -K_g[\varphi(t) - \varphi(t)]$$

$$J_z\dot{r} = N_r r + N_\delta \delta + M_{z_e}$$

$$J_z\ddot{\varphi} - N_r\dot{\varphi} + N_\varphi K_g = N_\delta K_g \varphi_o(t) + M_{z_e}$$

$$|N_r| > 2\sqrt{J_z K_g N_\delta}$$

$$K_g < \frac{N_r^2}{4J_z N_\delta}$$

- Simple linearized driver model with delay

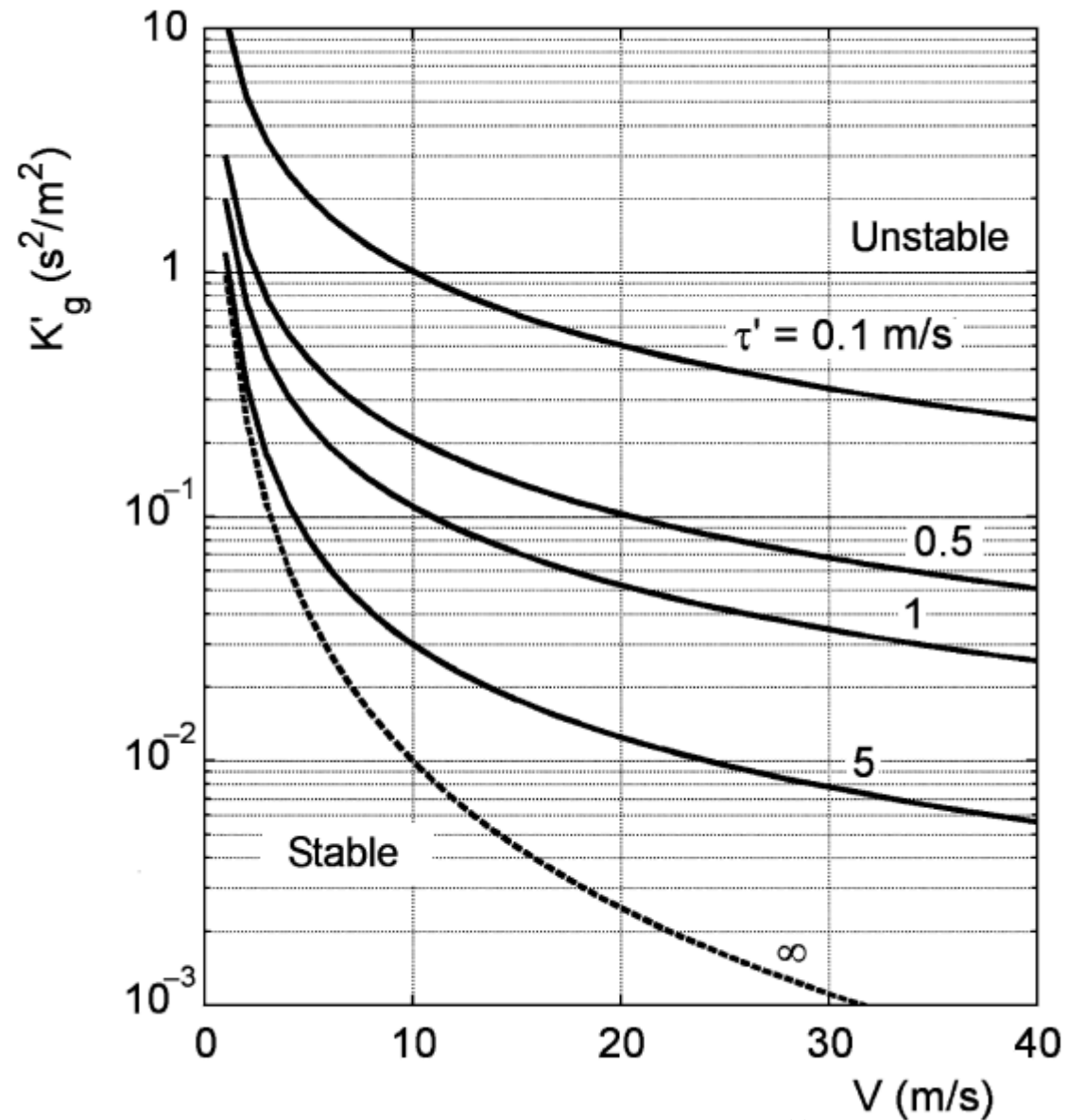
$$\begin{Bmatrix} \dot{r} \\ \dot{\delta} \\ \dot{\phi} \end{Bmatrix} = A \begin{Bmatrix} r \\ \delta \\ \phi \end{Bmatrix} + B_c \varphi_o + B_d M_{ze}$$

$$A = \begin{pmatrix} N_r/J_z & N_\delta/J_z & 0 \\ 0 & -1/\tau & -K_g/\tau \\ 1 & 0 & 0 \end{pmatrix}, \quad B_d = \begin{pmatrix} 1/J_z \\ 0 \\ 0 \end{pmatrix}, \quad B_c = \begin{pmatrix} \dot{r} \\ \dot{\delta} \\ \dot{\phi} \end{pmatrix}$$

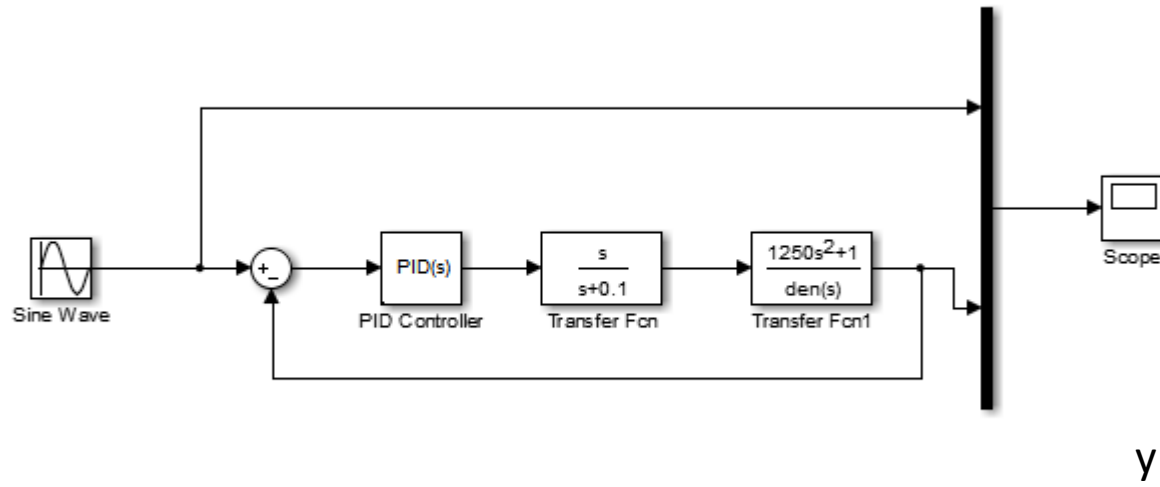
$$s^3 + P \left(\frac{1}{\tau} - \frac{N_r}{J_z} \right) s^2 - \frac{N_r}{\tau J_z} s + \frac{N_\delta K_g}{\tau J_z} = 0$$

$$K_g < \frac{N_r^2}{J_z N_\delta}$$

$$\tau < \frac{J_z N_r^2}{N_r^2 - J_z N_\delta K_g}$$



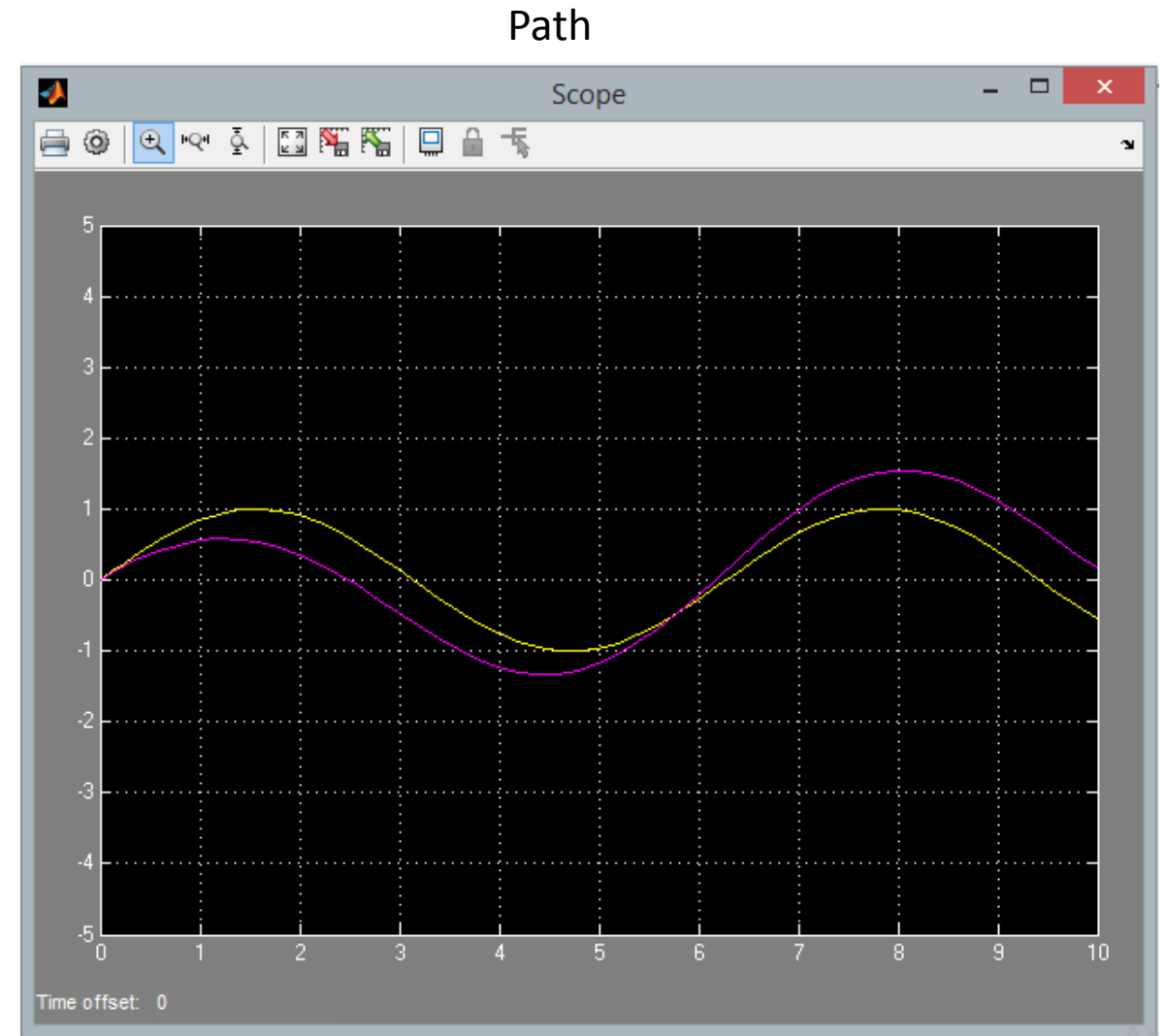
Proportional Constant Vs Velocity @ different time delays



Simple linearized Driver model with Delay

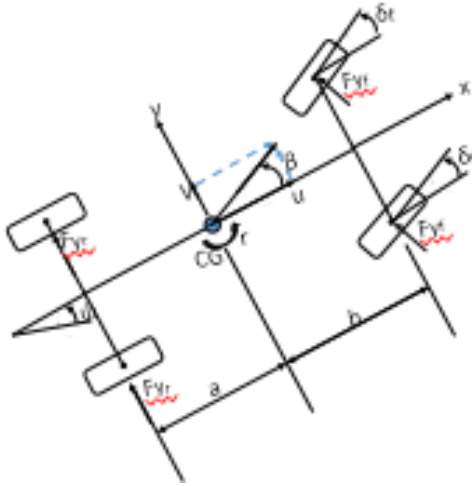
→ Yellow is the desired path

→ Violet is the Actual path

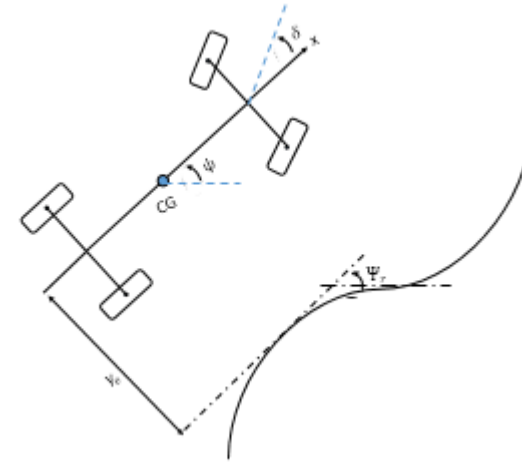


x

Path following driver model.



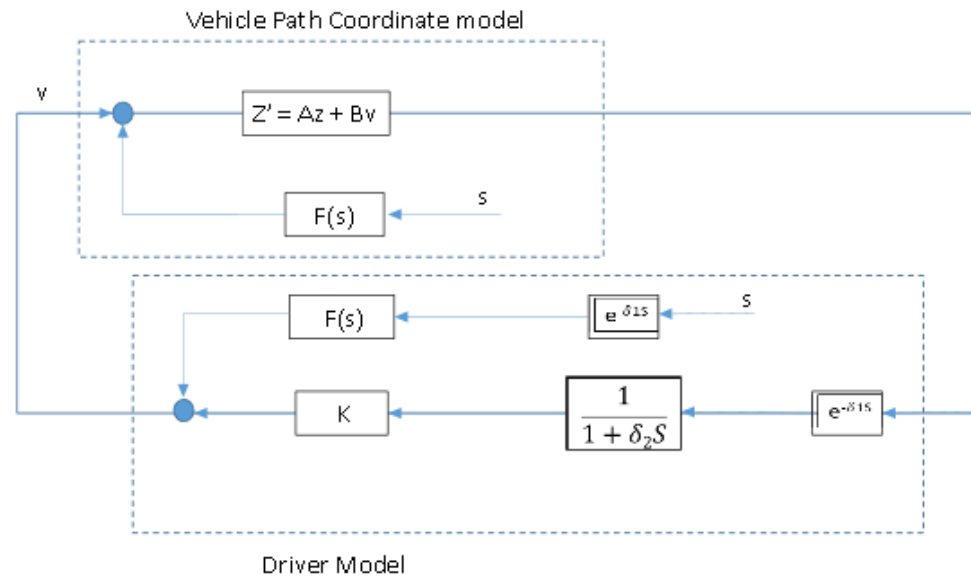
$$\begin{bmatrix} \dot{x} \\ \dot{y} \\ \dot{\theta} \\ \dot{\phi} \end{bmatrix} = \begin{bmatrix} \cos(\theta) \\ \sin(\theta) \\ \tan(\theta)/l \\ 0 \end{bmatrix} v_1 + \begin{bmatrix} 0 \\ 0 \\ 0 \\ 1 \end{bmatrix} v_2$$



$$\begin{aligned} \dot{s} &= \frac{v_1 \cos(\bar{\theta})}{1 - dc(s)} \\ \dot{d} &= v_1 \sin(\bar{\theta}) \\ \dot{\bar{\theta}} &= v_1 \left(\frac{\tan(\phi)}{l} - \frac{c(s) \cos(\bar{\theta})}{1 - dc(s)} \right) \\ c(s) &= \frac{d\theta_t}{ds} \end{aligned}$$

$$Z' = Az + Bv \quad z = \begin{bmatrix} d \\ \bar{\theta} \end{bmatrix},$$

$$Z' = \frac{\partial z}{\partial s} A = \begin{bmatrix} 0 & 1 \\ 0 & 0 \end{bmatrix} B = \begin{bmatrix} 0 \\ 1 \end{bmatrix}$$



$$\int_0^{\infty} (z^T Q z + r v^2) e^{2\lambda s} ds$$

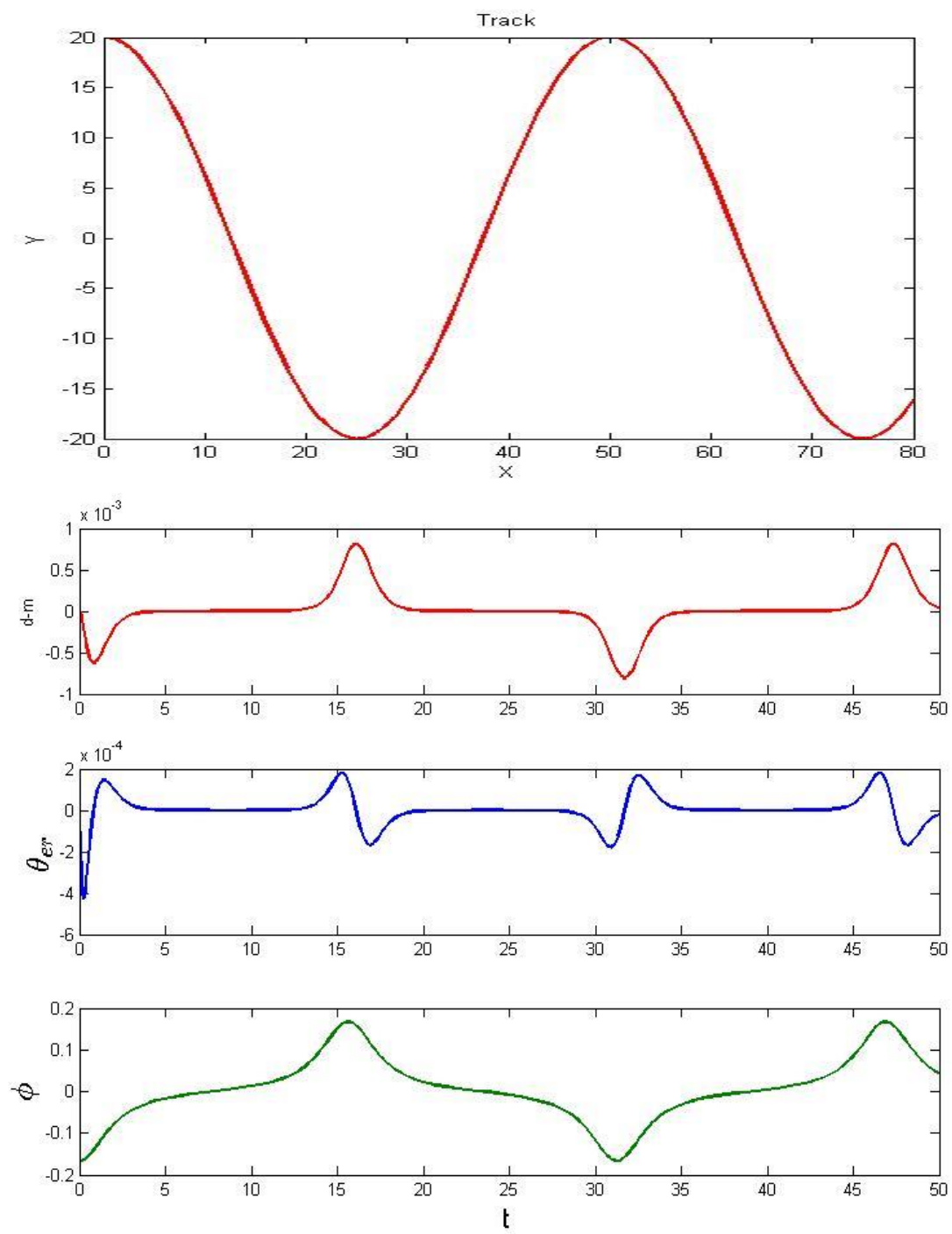
$$P(A + \lambda I) + (A^T + \lambda I)P - 1/r P B B^T P + Q = 0$$

$$Q = \begin{bmatrix} |v_1| & 0 \\ 0 & |v_1| \end{bmatrix}$$

$$V = -Kz$$

$$\phi = l(f(s) - Kz)$$

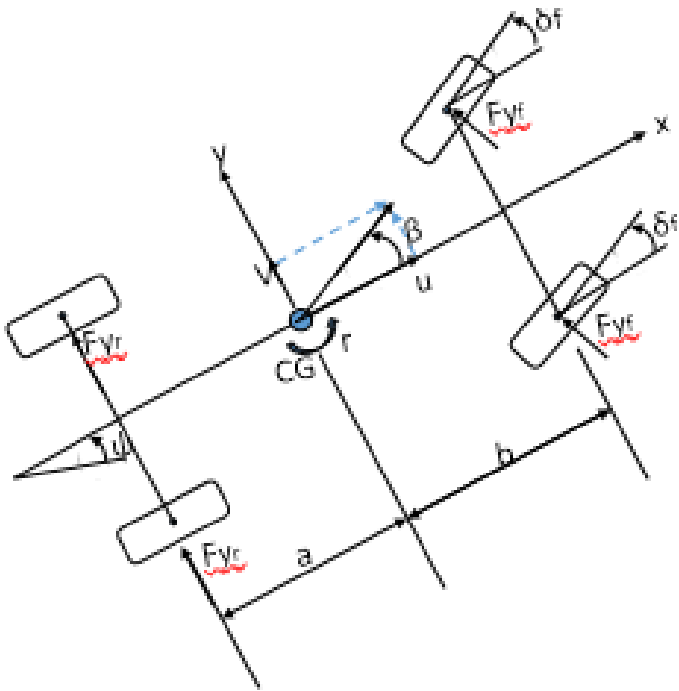
Results



Implementation of delay into driver model

- A vehicle path following analysis and improvement of vehicle handling process
- Introduce control system to ensure the vehicle follows desired path
- Desired yaw rate and slip angle to get desired path
- Delay associated with driver , Neural response delay
- Sensor delay
- Consider preview distance

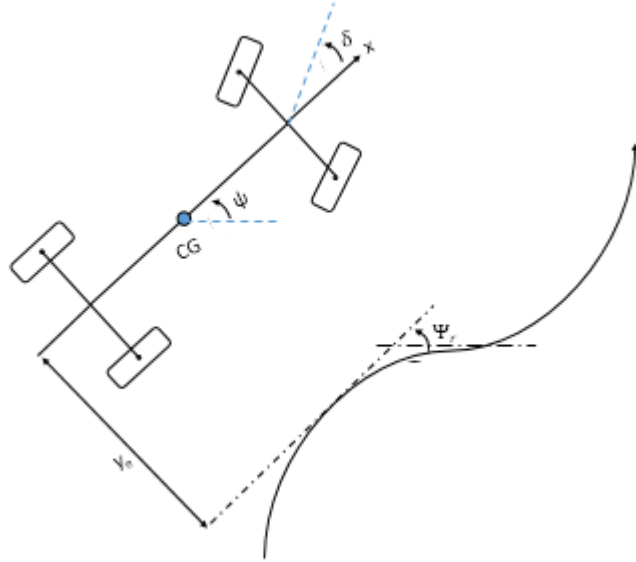
- The equations of vehicle dynamics are:
 - $M(\dot{V}y + Ur) = F_{yr} \cos\delta_r + F_{xr} \sin\delta + F_{yf} \cos\delta_f + F_{xf} \sin\delta_f$
 - $I_z \dot{r} = aF_{yf} \cos\delta_f + aF_{xf} \sin\delta_f - bF_{yr} \sin\delta_r - bF_{yr} \cos\delta_r$



$$\dot{y}_e = U \sin\psi + Vy \cos\psi$$

$$\dot{\psi} = \dot{\psi}_v - \dot{\psi}_r$$

Vehicle model



$$\dot{X}_1 = A_1 X_1 + E_1 \delta + B_1 M z + K \left(\frac{1}{R(t)} \right)$$

$$X_1 = \begin{bmatrix} y_e \\ V_y \\ \psi \\ r \end{bmatrix} \quad A_1 = \begin{bmatrix} 0 & 1 & U & 0 \\ 0 & a_{11} & 0 & a_{12} \\ 0 & 0 & 0 & 1 \\ 0 & a_{21} & 0 & a_{22} \end{bmatrix} \quad E_1 = \begin{bmatrix} 0 \\ e_1 \\ 0 \\ e_2 \end{bmatrix} \quad B_1 = \begin{bmatrix} 0 \\ 0 \\ 0 \\ b \end{bmatrix} \quad K = \begin{bmatrix} 0 \\ 0 \\ -U \\ 0 \end{bmatrix}$$

$$a_{11} = -2 \frac{C_{af} + C_{ar}}{MU} \quad a_{12} = -2 \frac{bC_{ar} + C_{af}}{MU} - U \quad a_{21} = 2 \frac{bC_{ar} - aC_{af}}{I_z U}$$

$$a_{22} = -2 \frac{a^2 C_{af} + b^2 C_{ar}}{I_z U} \quad e_1 = 2 \frac{C_{af}}{M} \quad e_2 = -2 \frac{aC_{af}}{I_z}$$

Driver model

- $H(s) = \frac{d(s)}{Ed(s)} = \frac{h}{N} \left[\frac{\tau_1 s + 1}{\tau_2 s + 1} \right] \frac{1}{\tau_r s + 1} e^{-\tau_d s}$ reff: Rosettes 2003
- Lead constant ,lag constant, reaction and delay time.
- $y_{ep} = y_e + L \psi$
- First order Pade polynomial approximation
- $e^{-\tau_d s} = \frac{1 - \frac{\tau_d}{2}s}{\left(1 + \frac{\tau_d}{2}s\right)}$

Human driver equation in time variant space.

- $\ddot{\delta} = W[-\ddot{y}_e + L\psi] + \frac{2\tau_1}{\tau_2} (\dot{y}_e + L\dot{\psi}) + \frac{1}{\tau_n \tau_2} [-(\tau_n + \tau_2) \dot{\delta} - \delta]$
- $W = \frac{h}{N} \cdot \frac{1}{\tau_n} \frac{1}{\tau_2}$

Closed Loop driver model

- $\dot{X} = AX + BMz + K \begin{bmatrix} 1 \\ R \end{bmatrix}$

$$X = \begin{bmatrix} ye \\ v \\ \psi \\ r \\ \delta \\ \dot{\delta} \end{bmatrix} \quad A = \begin{bmatrix} 0 & 1 & 0 & 0 & 0 & 0 \\ 0 & a_{11} & 0 & a_{21} & e_1 & 0 \\ 0 & 0 & 0 & 1 & 0 & 0 \\ 0 & a_{21} & 0 & a_{22} & e_2 & 0 \\ 0 & 0 & 0 & 0 & 0 & 1 \\ a_{16} & a_{62} & a_{63} & a_{64} & a_{65} & a_{66} \end{bmatrix} \quad B = \begin{bmatrix} 0 \\ 0 \\ 0 \\ b \\ 0 \\ Wb \end{bmatrix} \quad K = \begin{bmatrix} 0 \\ 0 \\ -U \\ 0 \\ 0 \\ -WU^2 - \frac{2W\tau_1}{\tau_d}LU \end{bmatrix}$$

curvature is taken as
sinusoidal path

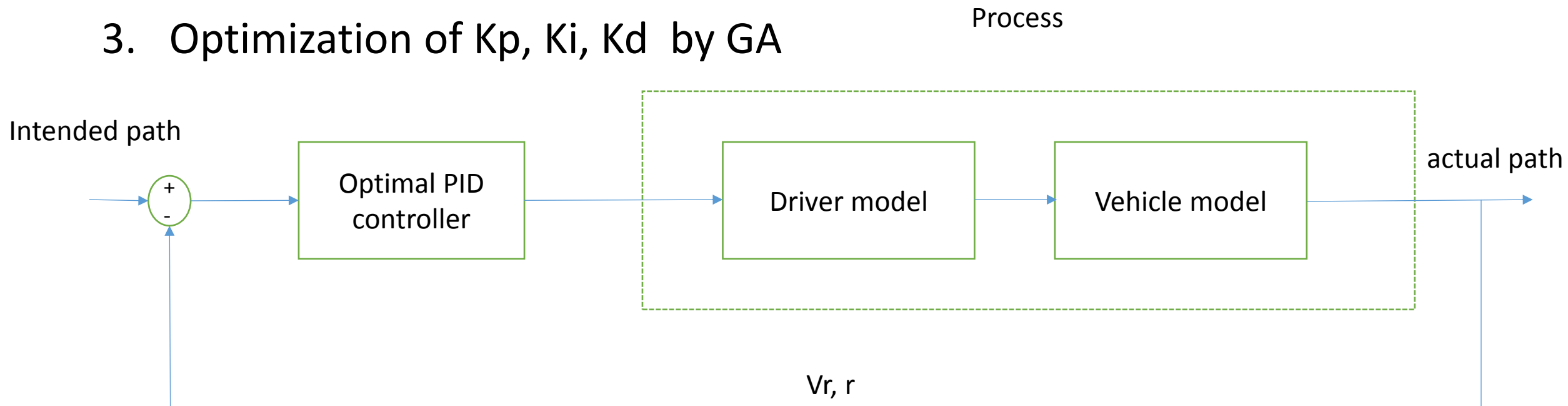
$$a_{61} = W \quad a_{62} = W(a_{11} + La_{21}) + \frac{2W\tau_1}{\tau_d}, \quad a_{63} = -\frac{2W\tau_1}{\tau_d}U + WL$$

$$a_{64} = W(a_{21} + La_{22} + U) + \frac{2W\tau_1}{\tau_d}L, \quad a_{65} = \frac{-1}{\tau_n \cdot \tau_1} + e_1 + Le_2, \quad a_{66} = \frac{(\tau_n + \tau_2)}{\tau_n \cdot \tau_2}$$

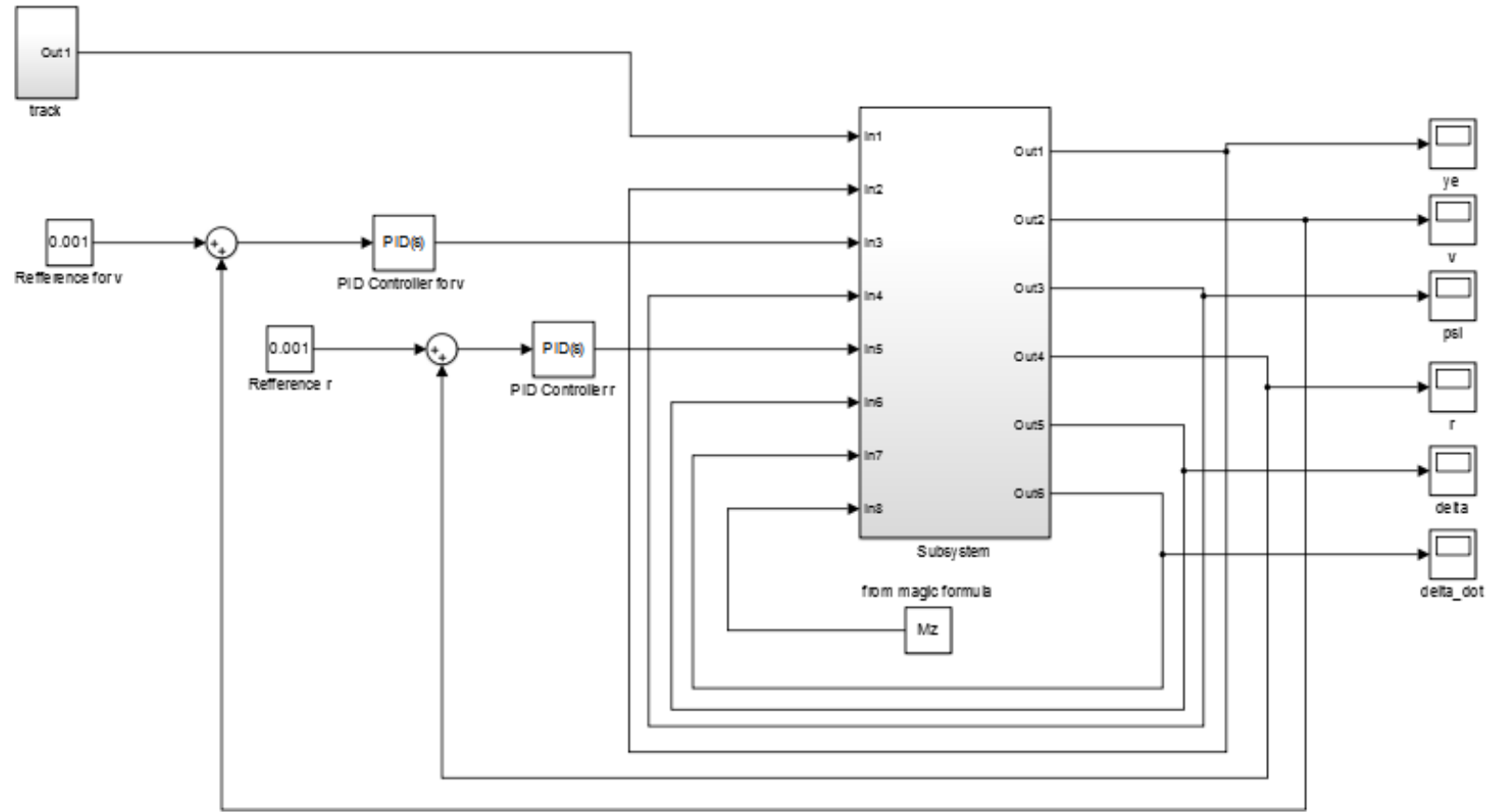
Controller

Introduce PID controller for

1. yaw rate
2. slip angle to get desired path
3. Optimization of K_p , K_i , K_d by GA



Matlab Simulink model



Conclusion

- Formulated driver model in order to make vehicle in desired path.
- 1- Simple model with delay case has been studied, and used PID controller
 - Modeled in Simulink
- 2- No delay case has been studied by considering preview distance
 - Optimized proportional controller has been used with the help of Riccati equation by minimizing cost function .
 - Modeled and solved using Matlab ODE solver
- 3- Introduced delays to driver model and
 - Modeled in Matlab Simulink along with mathematical modeling .

REFERENCE

- Giancarlo Genta, Lorenzo Morello 2009 “The Automotive Chassis – System Design”.
- Wenjuan Jiang, Carlos Canudas-de-Wit, Olivier Sename and Jonathan Dumon 2011 “A new mathematical model for car drivers with spatial preview”.
- Behrooz Mashadi, Mehdi Mahmoudi-Kaleybar, Pouyan Ahmadizadeh; Atta Oveisi 2014 “A path following driver/vehicle model with optimized lateral dynamic controller.”
- Rosettes, E.J , (2003) “A potential Field Framework for Active Vehicle Lane Keeping Assistance”.

THANK YOU