

Theoretical Interpretation of Flavour Anomalies

Admir Greljo

<u>Abstract</u>: I will present our recent work on lepton flavor non-universal and anomaly-free U(1) gauge extensions of the SM. The phenomenological discussion will be centered around flavor anomalies in rare B-meson decays and muon g-2. This talk is based on 2103.13991 (AG, Stangl, and Thomsen) and 2107.07518 (AG, Soreq, Stangl, Thomsen, and Zupan).

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Part I: Introduction

\mathscr{L}_4 : Accidental symmetries

$$\mathscr{L}_4^{SM}$$
 sans Yukawa: $U(3)_q \times U(3)_U \times U(3)_D \times U(3)_l \times U(3)_E$

$$-\mathscr{L}_{Yuk} = \bar{q} V^{\dagger} \hat{Y}^{u} \tilde{H} U + \bar{q} \hat{Y}^{d} H D + \bar{l} \hat{Y}^{e} H E$$

 $[U(3)^5$ transformation and a singular value decomposition theorem]

$$\mathscr{L}_4^{SM}: \qquad U(1)_B \times U(1)_e \times U(1)_\mu \times U(1)_\tau$$

Prediction: No proton decay nor cLFV **Experiment:** $\tau_p \gtrsim 10^{34}$ years, $BR(\mu \rightarrow e\gamma) \lesssim 10^{-13}, \dots$

- Λ_{NP}^{-1} truncation at the $[\mathscr{L}^{\text{SMEFT}}] \leq 4 \implies \text{Exact}$ accidental symmetries
- Peculiar observed values of $Y^{u,d,e} \implies \text{Approximate} \text{ accidental symmetries}$ [Mass hierarchy & CKM alignment] [Quark flavour, CP, etc]





- Accidental symmetries (exact and approximate) are broken by the irrelevant couplings.
- Testing accidental symmetries is an opportunity \implies Efficient probe of high-energy dynamics.
- A viable BSM at the TeV-scale should have accidental symmetries similar to the SM.

Part II: Flavour anomalies

This talk: $b \rightarrow s\ell\ell$ and $(g-2)_{\mu}$

Footprints of a next layer?



LHCb, CERN, 2103.11769

+ other $b \rightarrow s \,\mu\mu$ observables

= 4.3σ conservative global significance

[Isidori, Lancierini, Owen, Serra, 2104.05631]



B. Capdevila, M. Fedele, S. Neshatpour, P. Stangl

New mass scale?

• IF $b \rightarrow s\ell^+\ell^-$ anomalies are genuine new physics effect \implies Major Revolution in HEP

$$\mathscr{L} \supset \frac{1}{(40 \text{ TeV})^2} \left(\bar{s}_L \gamma^\mu b_L \right) \left(\bar{\mu}_L \gamma_\mu \mu_L \right)$$



• Observational evidence!

(Argument stronger than EW naturalness)

• The scale indicated from the perturbative unitary tends to be <u>overly pessimistic</u> Weak interactions : $G_F \implies \Lambda \lesssim 1 \text{ TeV}$, $m_W \approx 80 \text{ GeV}$

New mass scale?



- A <u>consistent</u> theory should have a well-defined flavour symmetry and a symmetry breaking pattern (e.g. MFV, U(2), partial compositeness, etc).
- Thus, $3_q \rightarrow 2_q$ transition should carry a corresponding flavour spurion suppression. $\mathscr{L}_6 \supset \frac{V_{cb}}{(8 \text{ TeV})^2} (\bar{s}_L \gamma^{\mu} b_L) (\bar{\mu}_L \gamma_{\mu} \mu_L)$

Mediators

See for example: Arcadi, Calibbi, Fedele, Mescia, 2104.03228

Scalar leptoquark example

- Tree-level
$$J_q \times J_\ell$$
 , while $J_q \times J_q$ and $J_\ell \times J_\ell$ loop-suppressed

$$\mathscr{L} \supset \eta_{ij} \mathcal{Q}_L^i L_L^j S_3$$

$$\uparrow$$

$$S_3 = (\bar{\mathbf{3}}, \mathbf{3}, 1/3)$$

• V-A structure

Hiller, Schmaltz, 1408.1627, Dorsner, Fajfer, AG, Kamenik, Kosnik; 1603.04993, Buttazzo, AG, Isidori, Marzocca; 1706.07808, Gherardi, Marzocca, Venturini; 2008.09548 + many more

$$\Rightarrow \frac{\eta_{b\mu}\eta_{s\mu}}{M_{LQ}^2} \sim \frac{V_{cb}}{(8 \text{ TeV})^2}$$

Direct LHC searches LQ pair production: $m_{LQ} \gtrsim 1.5 \text{ TeV}$

$$Leptoquarks$$

$$\mathcal{L}_{4} \neq = \bigcup_{i} \bigcap_{j} \bigcup_{k=1}^{i} S_{j} + z_{ij} \bigcap_{k=1}^{i} \bigcap_{j=1}^{i} S_{j}^{\dagger} + z_{ij} \bigcap_{k=1}^{i} \bigcap_{k=1}^{i} S_{k}^{\dagger} + z_{ij} \bigcap_{k=1}^{i} \bigcap_{k=1}^{i} S_{k}^{\dagger} + z_{ij} \bigcap_{k=1}^{i} \bigcap_{k=1}^{i} S_{k}^{\dagger} + z_{ij} \bigcap_{k=1}^{i} \sum_{k=1}^{i} \sum_{k=1$$

$$Muon (g - 2)$$

The Muon g-2, Fermilab, 2104.03281

A word of caution:

More EXP/TH work is needed to prove NP is behind these effects.

*BMW lattice only 1.6σ [2002.12347]

cLFUV but no cLFV

$$\frac{Br(\mu \to e\gamma)}{3 \times 10^{-13}} \approx \left(\frac{\Delta a_{\mu}}{3 \times 10^{-9}}\right)^2 \left(\frac{\theta_{12}}{10^{-5}}\right)^2$$
$$\frac{Br(\tau \to \mu\gamma)}{4 \times 10^{-8}} \approx \left(\frac{\Delta a_{\mu}}{3 \times 10^{-9}}\right)^2 \left(\frac{\theta_{23}}{10^{-2}}\right)^2$$
Naive BSM expectation is wrong!

$$\begin{aligned} \theta_{12} &\sim \sqrt{m_e/m_\mu} \sim \mathcal{O}(10^{-1}) \\ \theta_{23} &\sim \sqrt{m_\mu/m_\tau} \sim \mathcal{O}(10^{-1}) \end{aligned}$$

Nearly exact $U(1)_e \times U(1)_\mu \times U(1)_\tau$?

Part III: Muonic forces

AG, Stangl, Thomsen; 2103.13991

AG, Soreq, Stangl, Thomsen, Zupan; 2107.07518

Gauged lepton flavor

Extend the SM gauge group with the lepton flavour non-universal $U(1)_X$.

Gauged U(1)_X $\sim \sim e^{\mu}$ χ

- Natural framework for cLFUV without cLFV.
- $U(1)_X$ gauge boson is a potential mediator behind flavour anomalies.

Altmannshofer, Gori, Pospelov, Yavin; 1403.1269, Crivellin, D'Ambrosio, Heeck; 1501.00993, Celis, Fuentes-Martin, Jung, Serodio; 1505.03079, Crivellin, Fuentes-Martin, AG, Isidori; 1611.02703, Alonso, Cox, Han, Yanagida; 1705.03858, Bonilla, Modak, Srivastava, Valle; 1705.00915, Ellis, Fairbairn, Tunney; 1705.03447; Allanach, Davighi; 1809.01158, Altmannshofer, Davighi, Nardecchia; 1909.02021, Allanach; 2009.02197, + many more ...

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Another potential mediator

• Charge a **leptoquark** under $U(1)_X$.

Hambye, Heeck; 1712.04871 Davighi, Kirk, Nardecchia, 2007.15016 AG, Stangl, Thomsen, 2103.13991 AG, Soreq, Stangl, Thomsen, Zupan; 2107.07518

• Gauge symmetry selection rules:

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Gauge symmetry selection rules: $q \mu S$ $q \mu S$ $q \rho S$, $q \tau S$, $q q S^{\dagger}$

The accidental symmetry of \mathscr{L}_4 is $U(1)_B \times U(1)_e \times U(1)_\mu \times U(1)_\tau$ and the LQ charge is (-1/3, 0, -1, 0)

"Muoquark"

The $U(1)_X$ atlas

- $\mathrm{SU}(3)_C \times \mathrm{SU}(2)_L \times \mathrm{U}(1)_Y \times \mathrm{U}(1)_X$ gauge group $Q_i \sim (\mathbf{3}, \mathbf{2}, \frac{1}{6}, X_{Q_i}), \qquad U_i \sim (\mathbf{3}, \mathbf{1}, \frac{2}{3}, X_{U_i}), \qquad D_i \sim (\mathbf{3}, \mathbf{1}, -\frac{1}{3}, X_{D_i}),$ $L_i \sim (\mathbf{1}, \mathbf{2}, -\frac{1}{2}, X_{L_i}), \qquad E_i \sim (\mathbf{1}, \mathbf{1}, -1, X_{E_i}), \qquad N_i \sim (\mathbf{1}, \mathbf{1}, 0, X_{N_i})$
- Six anomaly cancelation conditions:

$$\begin{split} &\mathrm{SU}(3)_C^2 \times \mathrm{U}(1)_X: \ \sum_{i=1}^3 (2X_{Q_i} - X_{U_i} - X_{D_i}) = 0 \ , \\ &\mathrm{SU}(2)_L^2 \times \mathrm{U}(1)_X: \ \sum_{i=1}^3 (3X_{Q_i} + X_{L_i}) = 0 \ , \\ &\mathrm{U}(1)_Y^2 \times \mathrm{U}(1)_X: \ \sum_{i=1}^3 (X_{Q_i} + 3X_{L_i} - 8X_{U_i} - 2X_{D_i} - 6X_{E_i}) = 0 \ , \\ &\mathrm{Gravity}^2 \times \mathrm{U}(1)_X: \ \sum_{i=1}^3 (6X_{Q_i} + 2X_{L_i} - 3X_{U_i} - 3X_{D_i} - X_{E_i} - X_{N_i}) = 0 \ , \\ &\mathrm{U}(1)_Y \times \mathrm{U}(1)_X^2: \ \sum_{i=1}^3 (X_{Q_i}^2 - X_{L_i}^2 - 2X_{U_i}^2 + X_{D_i}^2 + X_{E_i}^2) = 0 \ , \\ &\mathrm{U}(1)_X^3: \ \sum_{i=1}^3 (6X_{Q_i}^3 + 2X_{L_i}^3 - 3X_{U_i}^3 - 3X_{D_i}^3 - X_{E_i}^3 - X_{N_i}^3) = 0 \ . \end{split}$$

AG, Soreq, Stangl, Thomsen, Zupan; 2107.07518

$$X_{Q_i} = X_{U_j} = X_{D_k} \quad (X_H = 0)$$

 $-10 \le X_{F_i} \le 10$ [276 inequivalent solutions] (i.e. up to flavor permutation, etc)

<u>Muoquark requirement</u>

eg.
$$S_3 LQ: X_{L_2} \neq \{X_{L_{1,3}}, -3X_q\}$$

[273 inequivalent solutions]

vector category : $X_{L_i} = X_{E_i}$ chiral category : the rest.

• Third-family quark [The "2+1" charge assignment]

18

• Answer: NO AG, Soreq, Stangl, Thomsen, Zupan; 2107.07518

Model Example I

			AG, Stangl, Thomsen, 2103.13991	
Fields	SU(3) _c	$SU(2)_L$	$U(1)_Y$	$U(1)_{B-3L_{\mu}}$
$q_{ m L}$	3	2	$^{1}/_{6}$	1/3
$u_{\rm R}$	3		$^{2}/_{3}$	¹ /3
d_{R}	3		-1/3	¹ /3
$\ell_{ m L}$		2	$^{-1}/_{2}$	$\{0, -3, 0\}$
$e_{\rm R}$			-1	$\{0, -3, 0\}$
$\nu_{ m R}$			0	$\{0, -3, 0\}$
Н		2	$^{1}/_{2}$	0
S_3	3	3	1/3	8/3
S_1	3		1/3	8/3
Φ			0	3

- Resolves $b \rightarrow s\mu\mu$ and $(g-2)_{\mu}$ while satisfying all complementary data.
- Minimal type-I seesaw for the neutrino masses. Viable texture.
- No proton decay up to dim-6 nor sizeable cLFV.
- No Landau poles up to the Planck scale.
- Finite naturalness. No tuning.

Model Example I

* V-A structure

Hiller, Schmaltz, 1408.1627, Dorsner, Fajfer, AG, Kamenik, Kosnik; 1603.04993, Buttazzo, AG, Isidori, Marzocca; 1706.07808, Gherardi, Marzocca, Venturini; 2008.09548 + many more

- moments, neutral meson mixing, semileptonic and
- rare B, D, K decays, etc.

Model Example II

• S_3 is charged under $U(1)_X$ such that it becomes a **muoquark**.

AG, Stangl, Thomsen, 2103.13991

Model Example II

Model Example III : Radiative y_{μ}

- The dimension-4 muon Yukawa is forbidden by $U(1)_X$ $X_{L_2} \neq X_{E_2}$ $(X_H = 0)$
- Introduce two scalar muoquarks $S_{\pm} = (\mathbf{3}, \mathbf{2}, 7/6, X_{S_{\pm}})$ $\mathcal{L} \supset \eta_{\mathrm{L}} \, \overline{t}_{\mathrm{R}} \ell_{\mathrm{L}}^2 \, i \sigma_2 S_+ - \eta_{\mathrm{R}} \, \overline{q}_{\mathrm{L}}^3 \, \mu_{\mathrm{R}} \, S_-$
- Mix them via $U(1)_X$ breaking $\mathcal{L} \supset -A\phi S_+^\dagger S_-$

Model Example III : Radiative y_{μ}

 $\Delta a_{\mu} = \frac{m_{\mu}^2}{m_{\star}^2} \tilde{F}\left(\frac{m_{S_1}^2}{m_{\star}^2}, \frac{m_{S_2}^2}{m_{\star}^2}\right)$

- The dimension-4 muon Yukawa is forbidden by $U(1)_X$ $X_{L_2} \neq X_{E_2}$ $(X_H = 0)$
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Conclusions

- Testing accidental symmetries is an opportunity: Efficient probe of high-energy dynamics.
- Flavour anomalies might be footprints of physics beyond the SM.
- Gauged lepton flavor is an interesting direction.
- We have just scratched the surface of $U(1)_X$ phenomenology.

	Type A	Type B	Type C
$\left R_{K^{(*)}}, b \to s \mu \mu \right $	S_3	S_3	heavy X
$(g-2)_{\mu}$	S_{1}/R_{2}	light X	S_{1}/R_{2}

AG, Stangl, Thomsen, 2103.13991

Mediators

- Tree-level $b \to s\ell\ell$ models
- Targeted mass window:

• Comments on the difference: [Upper bound] Z' induces tree-level $B_s - \overline{B}_s$ oscillations. Vector LQ comes with the Z'. [Lower bound] LQs are coloured and copiously produced at the LHC.

Single mediator?

The $U(1)_X$ at las

Quark flavor universal

•
$$Y^{u,d}$$
 are allowed => $X_{Q_i} = X_{U_j} = X_{D_k}$
($X_H = 0$)

$$-10 \le X_{F_i} \le 10$$

[276 inequivalent solutions]

• Muoquark requirement eg. $S_3 LQ: X_{L_2} \neq \{X_{L_{1,3}}, -3X_q\}$ [273 inequivalent solutions]

 Y^e allowed => vector category : $X_{L_i} = X_{E_i}$ [252 inequivalent solutions] chiral category : the rest. [21 inequivalent solutions]

The $U(1)_X$ atlas

Third-family-quark

• The "2+1" charge assignment

$$X_{Q_i} = X_{U_j} = X_{D_k} \equiv X_{q_{12}}$$
 for all $i, j, k = 1, 2$, and
 $X_{Q_3} = X_{U_3} = X_{D_3} \equiv X_{q_3}$. $(X_H = 0)$

• The CKM elements
$$(V_{td}, V_{ts})$$
 at dim-5:
 $\mathcal{L} \supset \frac{x_i^u}{\Lambda} \overline{Q}_i \tilde{H} \phi U_3 + \frac{x_i^d}{\Lambda} \overline{Q}_i H \phi D_3 + \text{H.c.}$

- The ACC conditions are satisfied provided $$^{*\rm Th}_{\rm solution}$$ $2X_{q_{12}}+X_{q_3}=3X_q$

*The quark flavor-universal solutions can immediately be extended to the 2 + 1 case.

• The muoquark conditions slightly change: $X_{q_{12}} = 0$ eg. $S_3 \perp Q$: $X_{L_2} \neq \{X_{L_{1,3}}, X_{L_{1,3}} - X_{q_3}, -X_{q_3}, -2X_{q_3}, -3X_{q_3}\}$ [171 inequivalent sol.] $-10 \leq X_{F_i} \leq 10$

Gauged $L_{\mu} - L_{\tau}$

Z' models: $L_{\mu} - L_{\tau}$

Constraints:

 $L_{\mu} - L_{\tau}$

Altmannshofer, Gori, Martin-Albo, Sousa, Wallbank 1902.06765

Fig. 5.1: Reach in new physics scale of present and future facilities, from generic dimension six operators. Colour coding of observables is: green for mesons, blue for leptons, yellow for EDMs, red for Higgs flavoured couplings and purple for the top quark. The grey columns illustrate the reach of direct flavour-blind searches and EW precision measurements. The operator coefficients are taken to be either ~ 1 (plain coloured columns) or suppressed by MFV factors (hatch filled surfaces). Light (dark) colours correspond to present data (mid-term prospects, including HL-LHC, Belle II, MEG II, Mu3e, Mu2e, COMET, ACME, PIK and SNS).

Neutrino masses

• The minimal type-I seesaw mechanism

$$m_{\nu} \simeq -v^2 y_{\nu} \left(M_{\rm R} + y_{\Phi} \langle \Phi \rangle \right)^{-1} y_{\nu}^{\rm T}$$

- The $U(1)_{B-3L_{\mu}}$ imposes a flavor structure for y_{ν}, M_R, y_{Φ} .
- The Dirac mass matrix splits into 2x2 $e\tau$ block and a diagonal μ .
- The Majorana mass matrix is entirely populated except (2,2) entry.
- There is enough parametric freedom to accommodate for:
 - Neutrino oscillations data,
 - The Planck limit on the sum of neutrino masses,
 - The absence of neutrinoless double beta decay.
- Not the case for all $U(1)_{X_{\mu}}$. Example is $U(1)_{L_{\mu}-L_{\tau}}$, see 1907.04042.