



[Strong] first order phase transitions and gravitational wave signatures

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This talk: saoghal.net/slides/anomalies2021

Anomalies 2021, IIT Hyderabad

The background of the slide is a complex, abstract pattern of colors ranging from light blue to dark red, representing a temperature slice from a phase transition simulation. The pattern consists of irregular, interconnected shapes and regions, with some areas being more uniform in color and others showing more variation. The overall appearance is that of a textured, organic surface.

Temperature slice from a phase transition simulation by Daniel Cutting



Hot, red areas are shrinking droplets



- How do droplets form?
- What are the consequences for gravitational waves?

Particle physics model

$\Downarrow \mathcal{L}_{4d}$

Dimensional reduction

$\Downarrow \mathcal{L}_{3d}$

Phase transition parameters from lattice simulations

$\Downarrow \alpha, \beta, T_N, \dots$

Real time cosmological simulations

$\Downarrow \Omega_{\text{gw}}(f)$

Cosmological GW background

Key parameters bridge the gap

Including:

- α , the phase transition strength
- β , the inverse phase transition duration
- T_N , the nucleation temperature

A long pipeline of large concrete pipes, supported by concrete blocks, stretching across a grassy field towards distant mountains under a cloudy sky. The pipes are arranged in a single line, receding into the distance. The surrounding landscape is a mix of green and yellowish grass, with rolling hills and mountains in the background. The sky is filled with soft, grey clouds.

A "pipeline"

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Real time cosmological simulations

⇓ $\Omega_{gw}(f)$

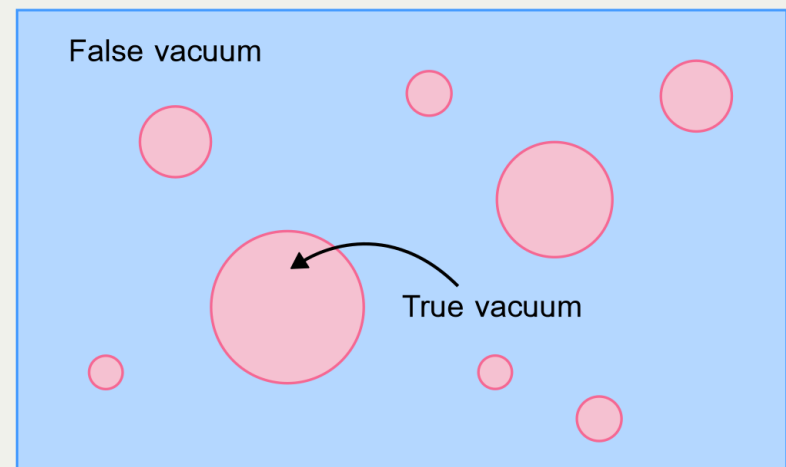
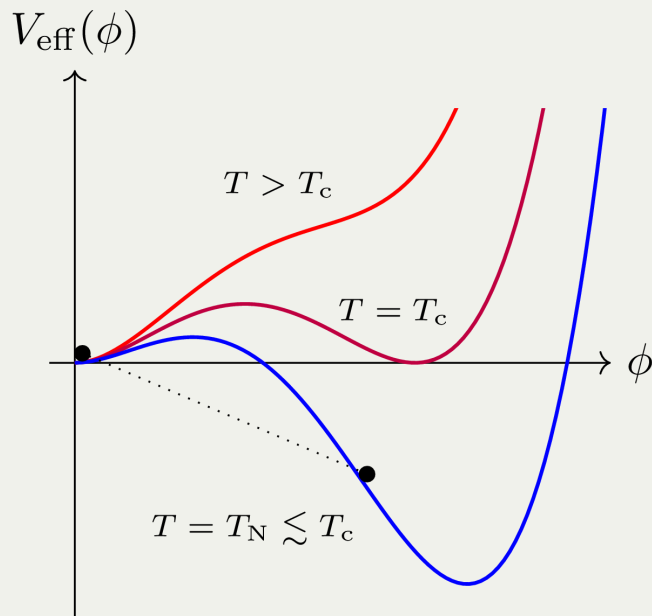
Cosmological GW background

My focus: extensions of the Standard Model

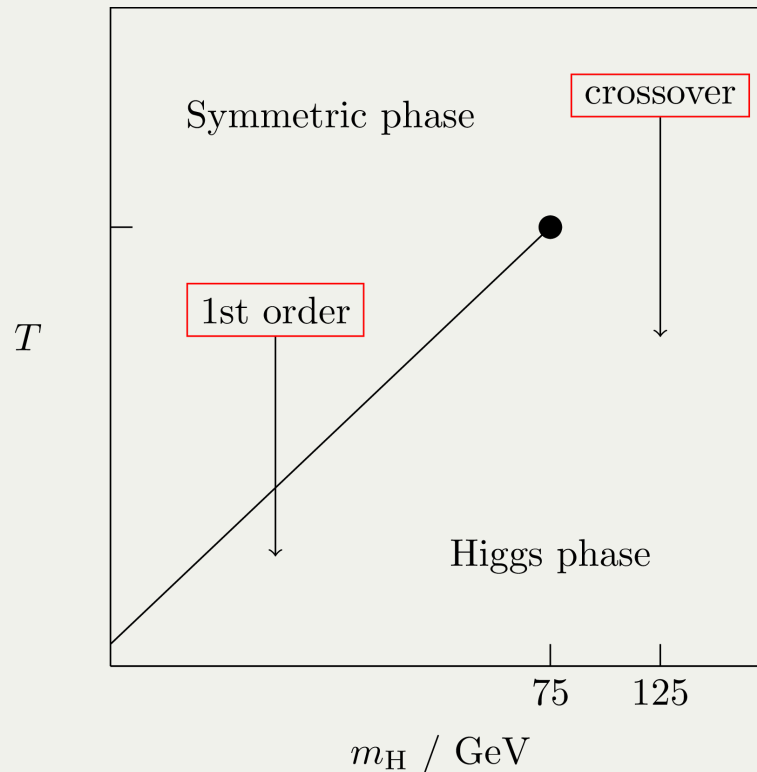
$$\mathcal{L}_{4d} = \mathcal{L}_{\text{SM}}[\text{SM fields}] + \mathcal{L}_{\text{BSM}}[\text{SM fields}, \dots?]$$

SM electroweak phase transition

- Process by which the Higgs 'switched on'
- In the Standard Model it is a crossover
- Possible in extensions that it would be first order
 - ↳ colliding bubbles then make gravitational waves



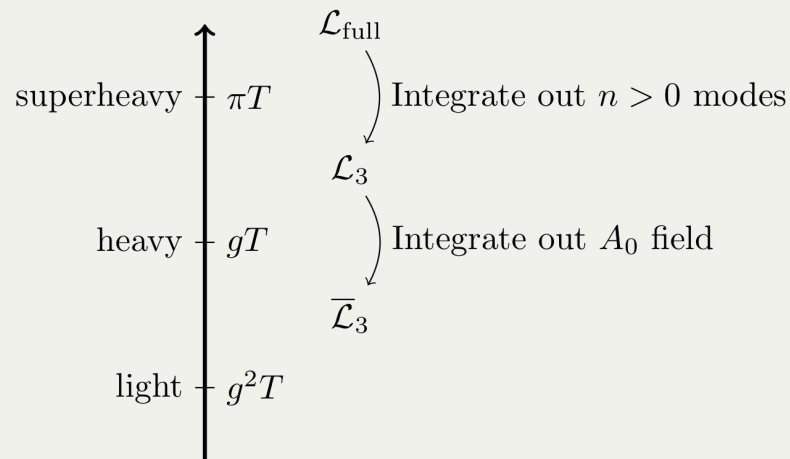
SM electroweak phase diagram



[arXiv:hep-ph/9605288](https://arxiv.org/abs/hep-ph/9605288) ; [arXiv:hep-lat/9704013](https://arxiv.org/abs/hep-lat/9704013); [arXiv:hep-ph/9809291](https://arxiv.org/abs/hep-ph/9809291)

How? Dimensional reduction

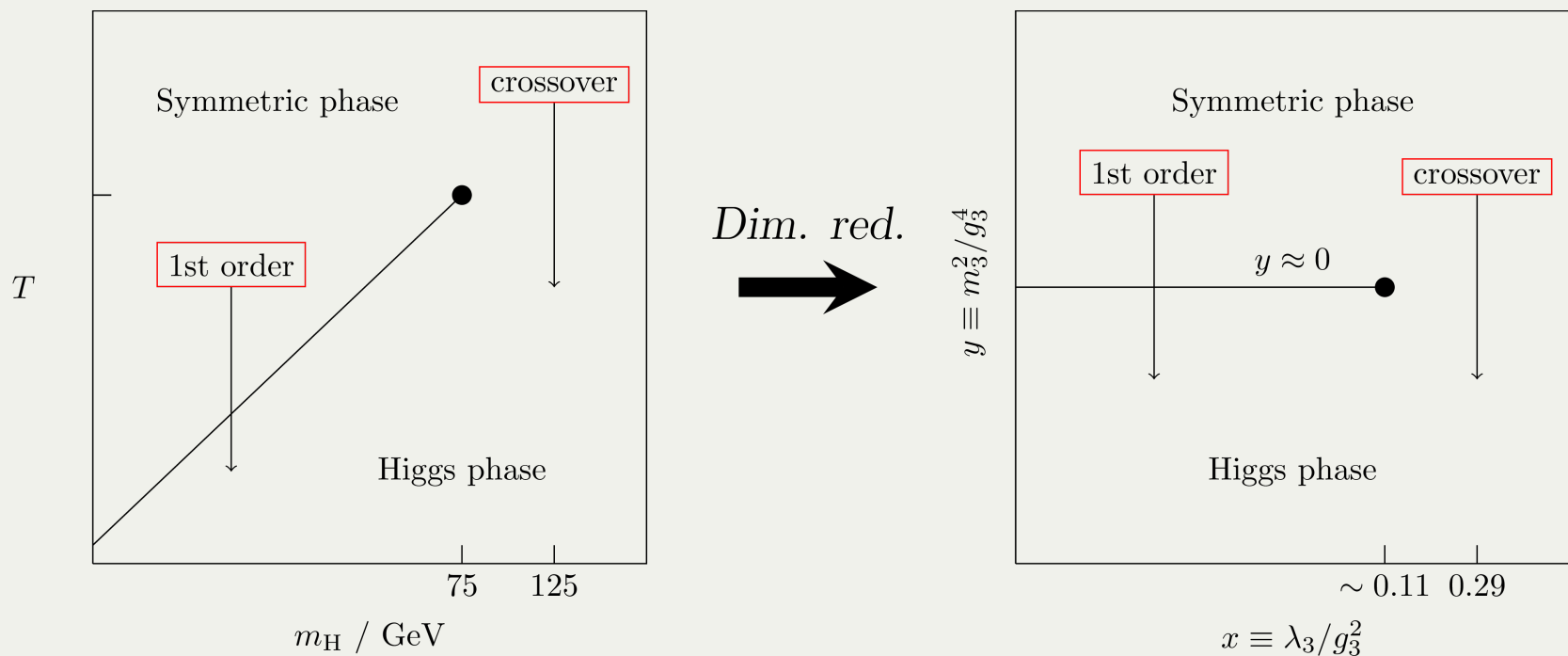
- At high T , system looks 3D at distances $\Delta x \gg 1/T$



- Each step involves matching Green's functions in the effective and full theories to the desired order.
- Handles the infrared problem, light fields can be studied on lattice. [arXiv:hep-ph/9508379](https://arxiv.org/abs/hep-ph/9508379)

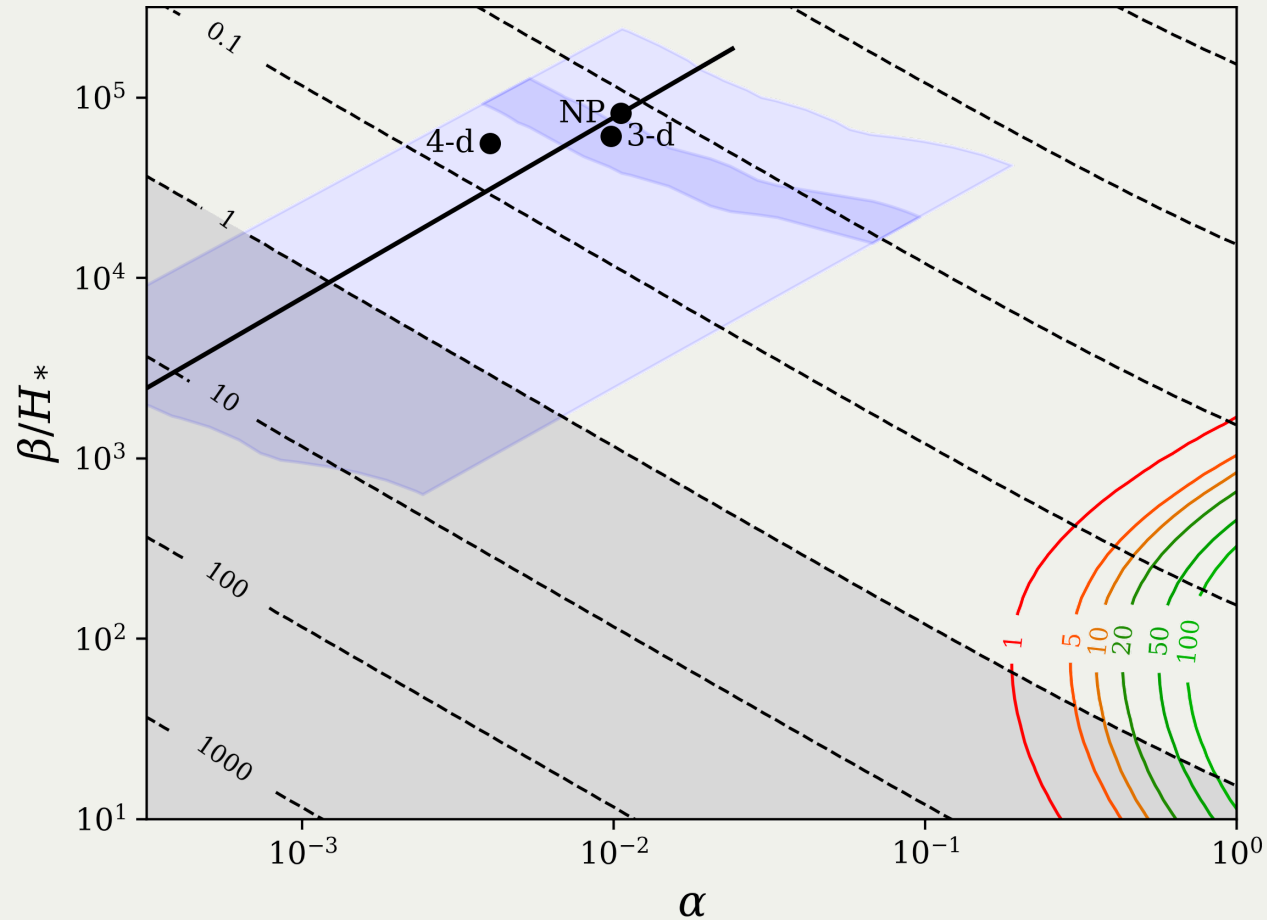
Using the dimensional reduction

- Simulate DR'ed 3D theory on lattice arXiv:hep-lat/9510020



- With DR, integrate out heavy new physics and recycle

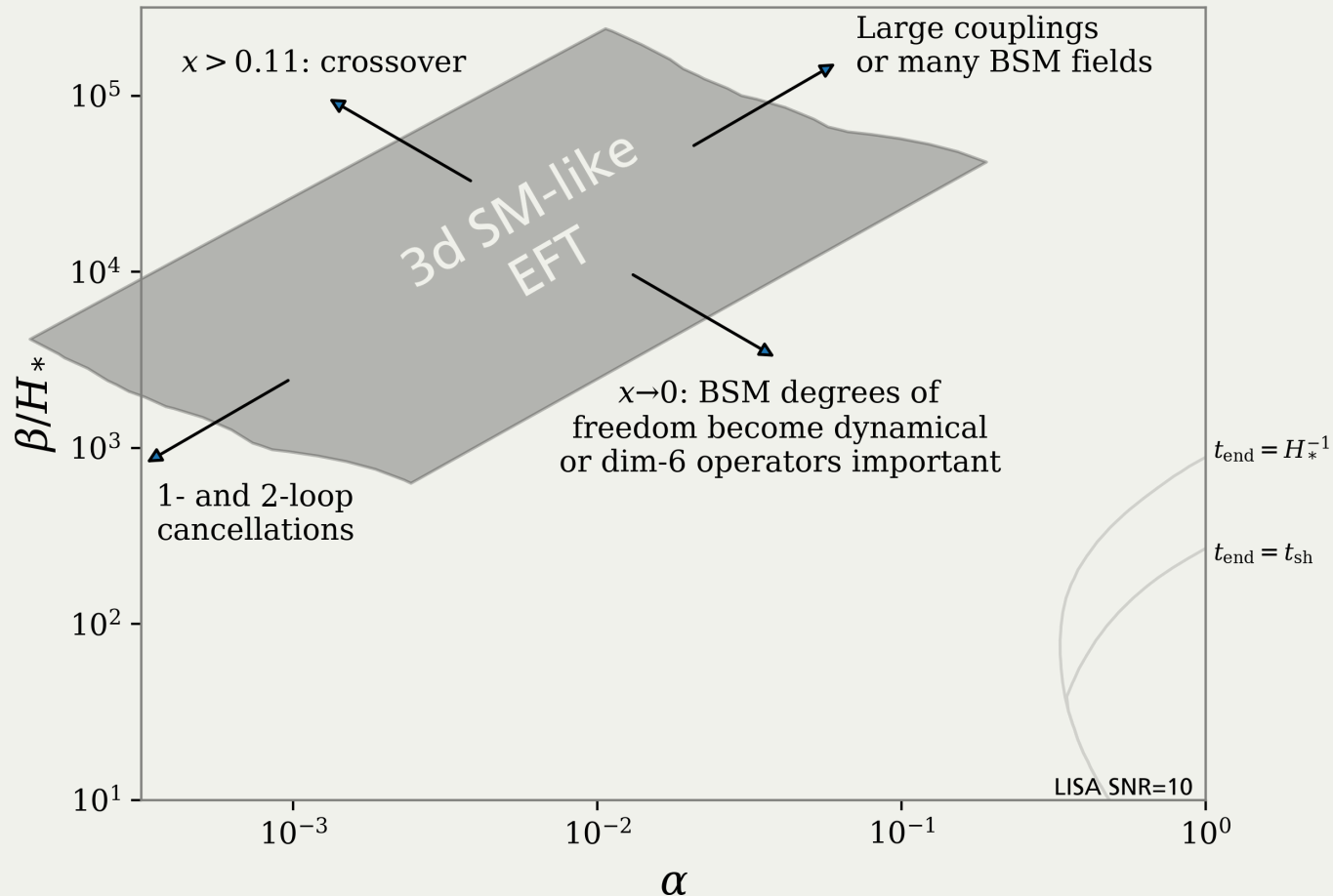
♻️ When new physics is heavy



Benchmark: • 4d PT vs • 3d PT vs • lattice

arXiv:1903.11604

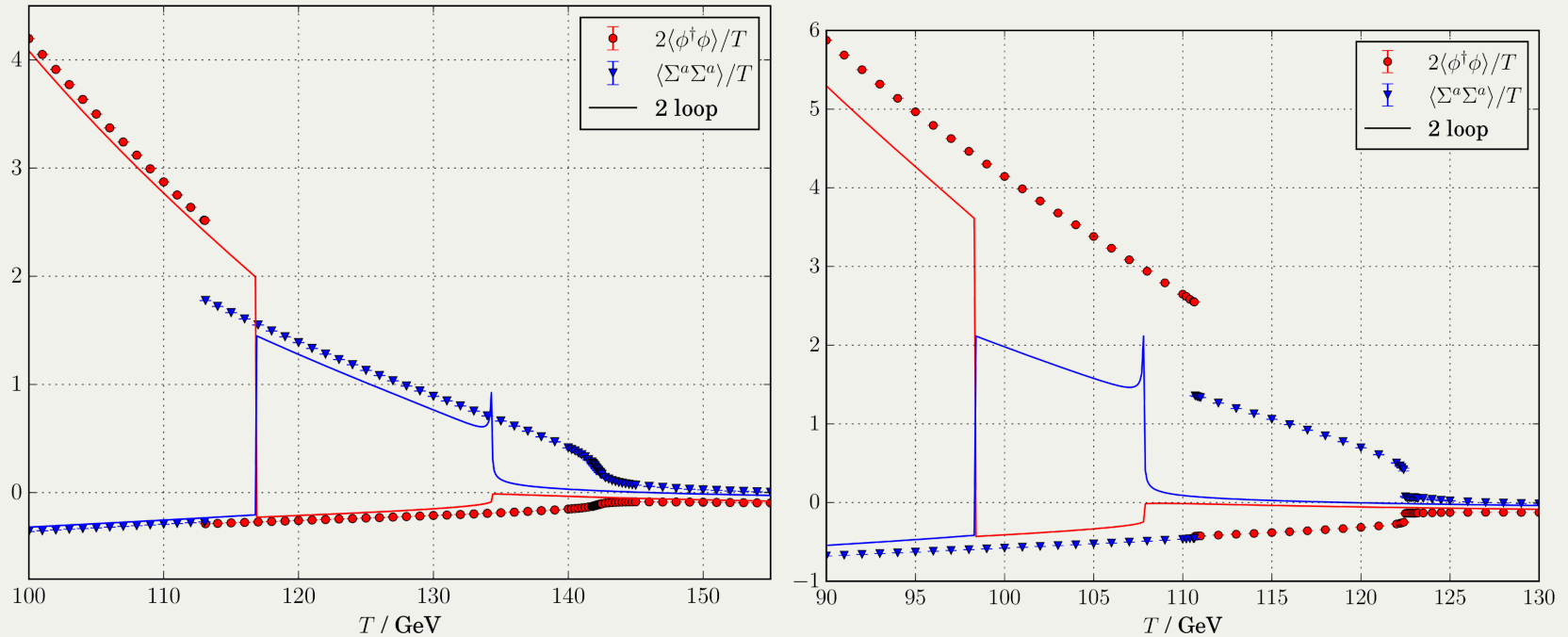
How to get strong transitions?



Need light physics or dim-6 operators

arXiv:1903.11604

DR: Σ SM (triplet) example



Perturbation theory doesn't see the phase transition!

arXiv:2005.11332

Key points so far

- Dimensional reduction + lattice simulations a well-proven method for studying BSM theories
- Higher dimensional operators or **light** new physics needed for a strong phase transition
- Should benchmark perturbation theory with DR + lattice, particularly for strong transitions

Particle physics model ✓

⇓ \mathcal{L}_{4d}

Dimensional reduction ✓

⇓ \mathcal{L}_{3d}

Phase transition parameters from lattice simulations ✓

⇓ $\alpha, \beta, T_N, \dots$

Real time cosmological simulations

⇓ $\Omega_{\text{gw}}(f)$

Cosmological GW background

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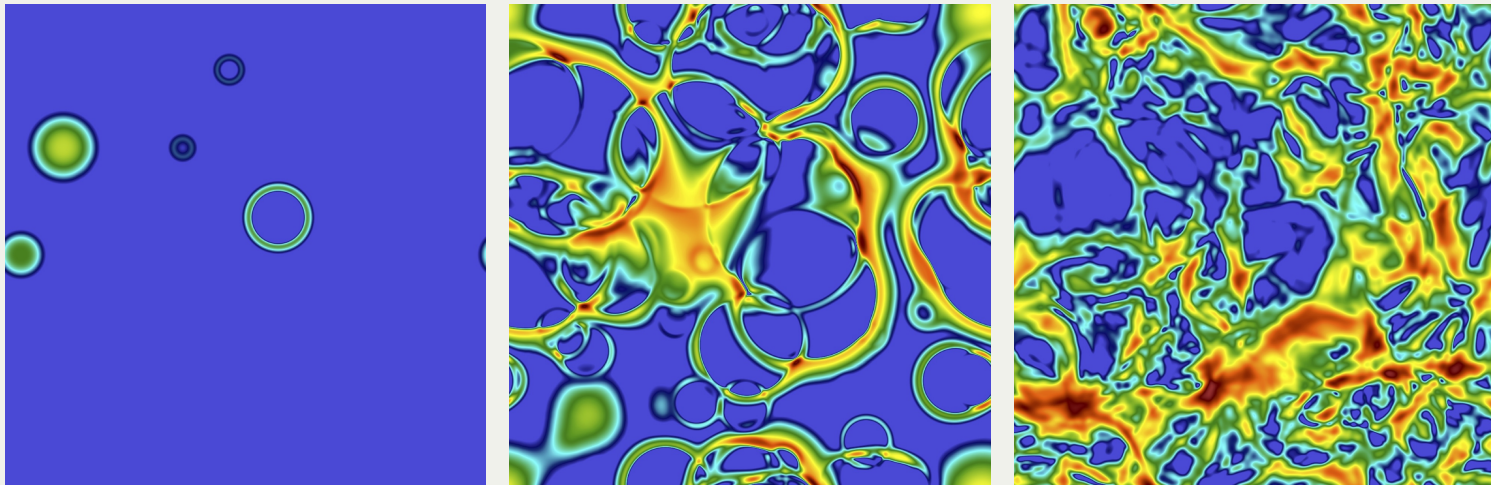
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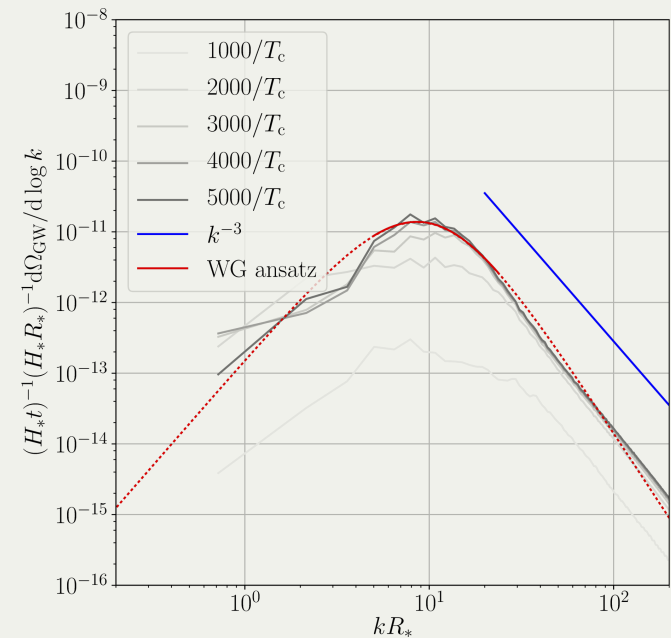
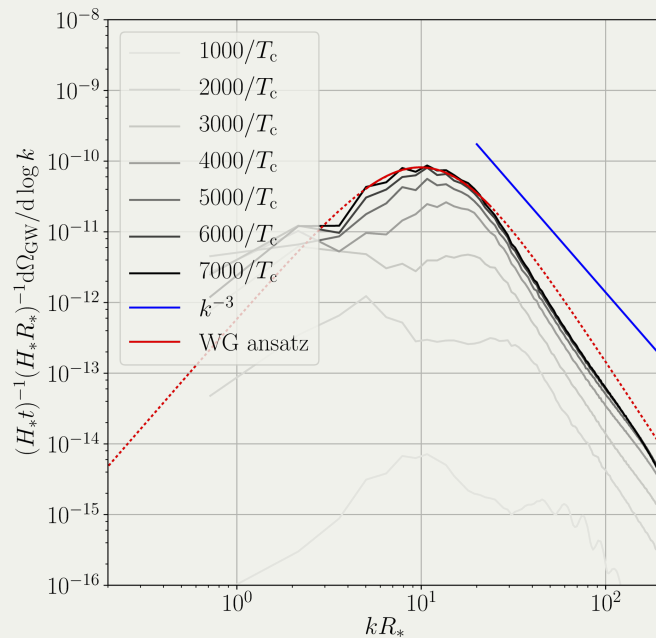
Out of equilibrium physics

1. Bubbles nucleate and grow
2. Expand in a plasma - create reaction fronts
3. Bubbles + fronts collide •)) $\Omega_{\text{col}}(f)$
4. **Sound waves** left behind in plasma •)) $\Omega_{\text{sw}}(f)$
5. Shocks [\rightarrow turbulence] \rightarrow damping •)) $\Omega_{\text{turb}}(f)$



Simulating weak transitions: $\alpha \ll 1$

- Focusing on GWs from sound waves... arXiv:1704.05871

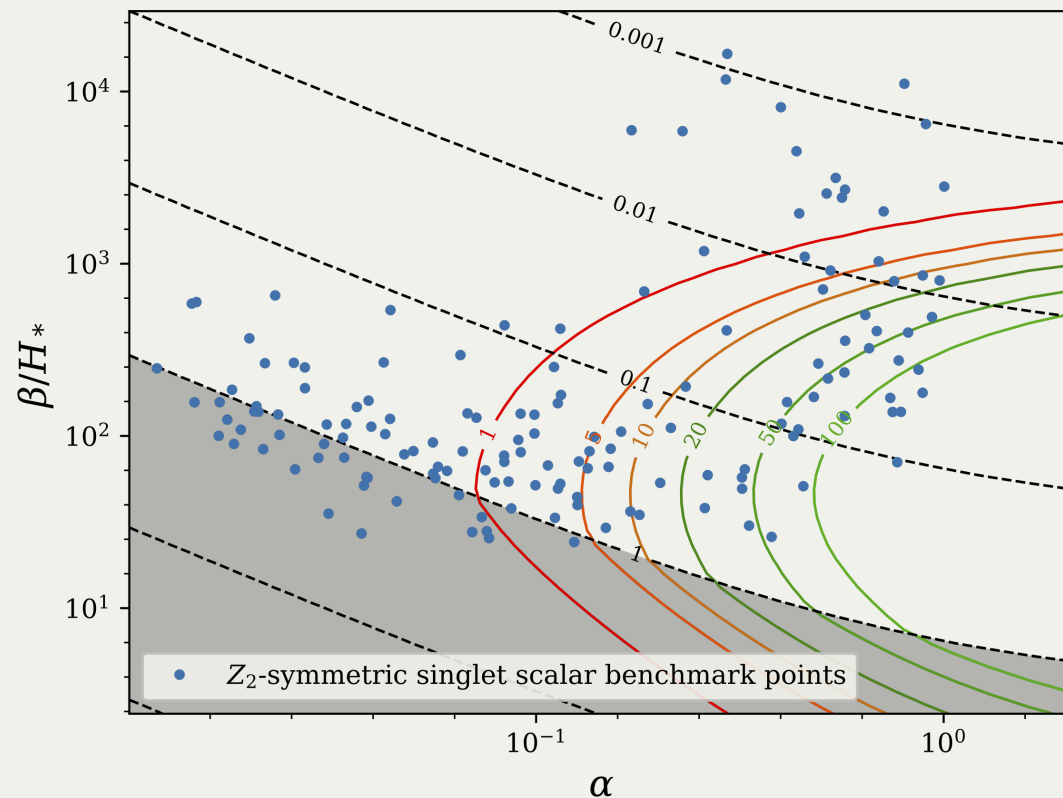


- ... $\Omega_{\text{SW}}(f)$ fairly close to broken power law arXiv:1512.06239
- ...and the linear sound shell model arXiv:1608.04735

Explore $\Omega_{\text{SW}}(f)$ with PTPlot.org

Model $\longrightarrow [T_*, \alpha_{T_*}, v_w, \beta] \longrightarrow$ this plot

[Here: Z_2 -symmetric xSM points from arXiv:1910.13125]



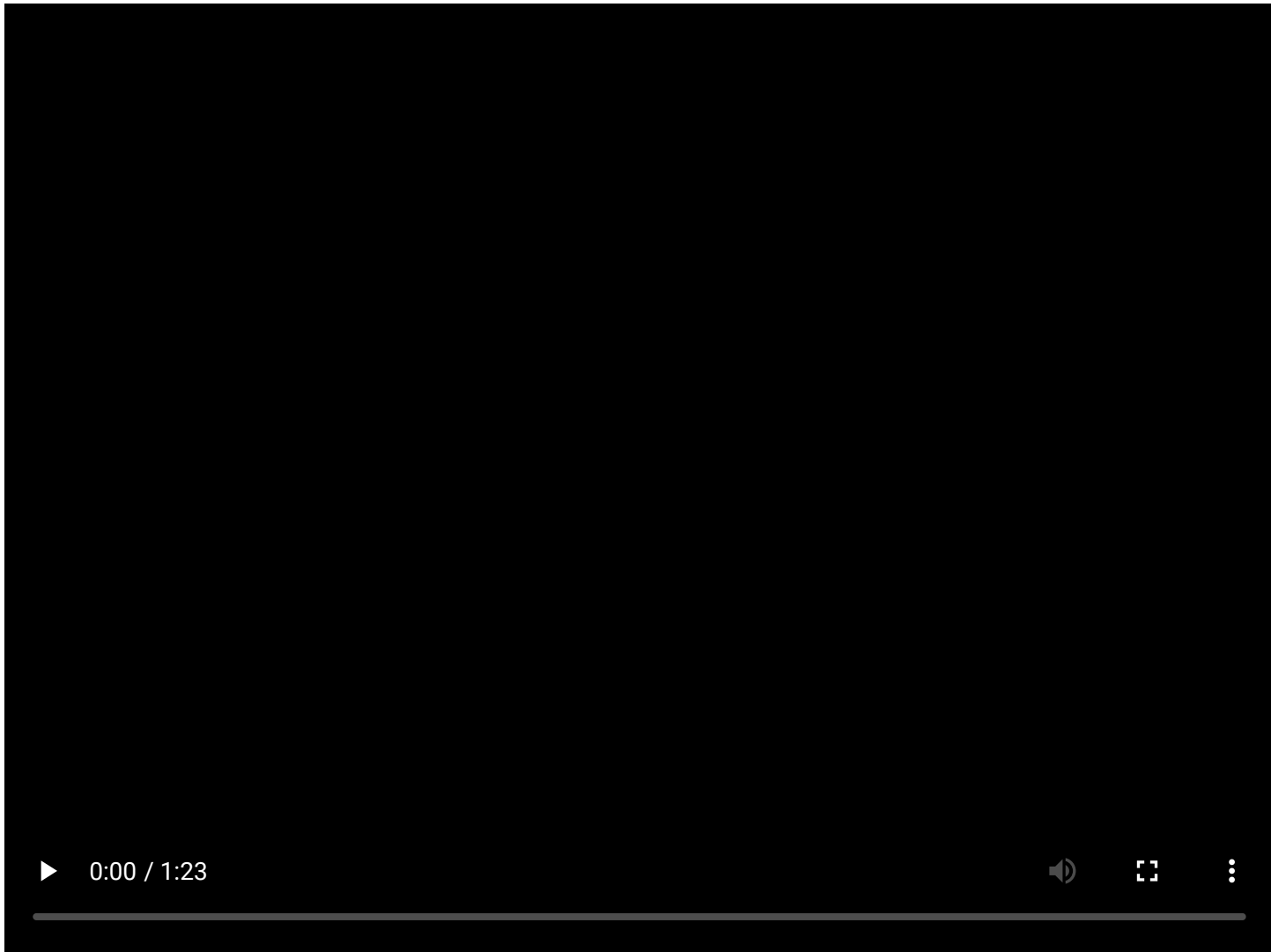
But what about strong transitions?

- Nonlinearities during the transition:
 - Generation of vorticity
 - Droplets
- Nonlinearities after the transition:
 - Shocks
 - turbulence

Let's take a look at droplets

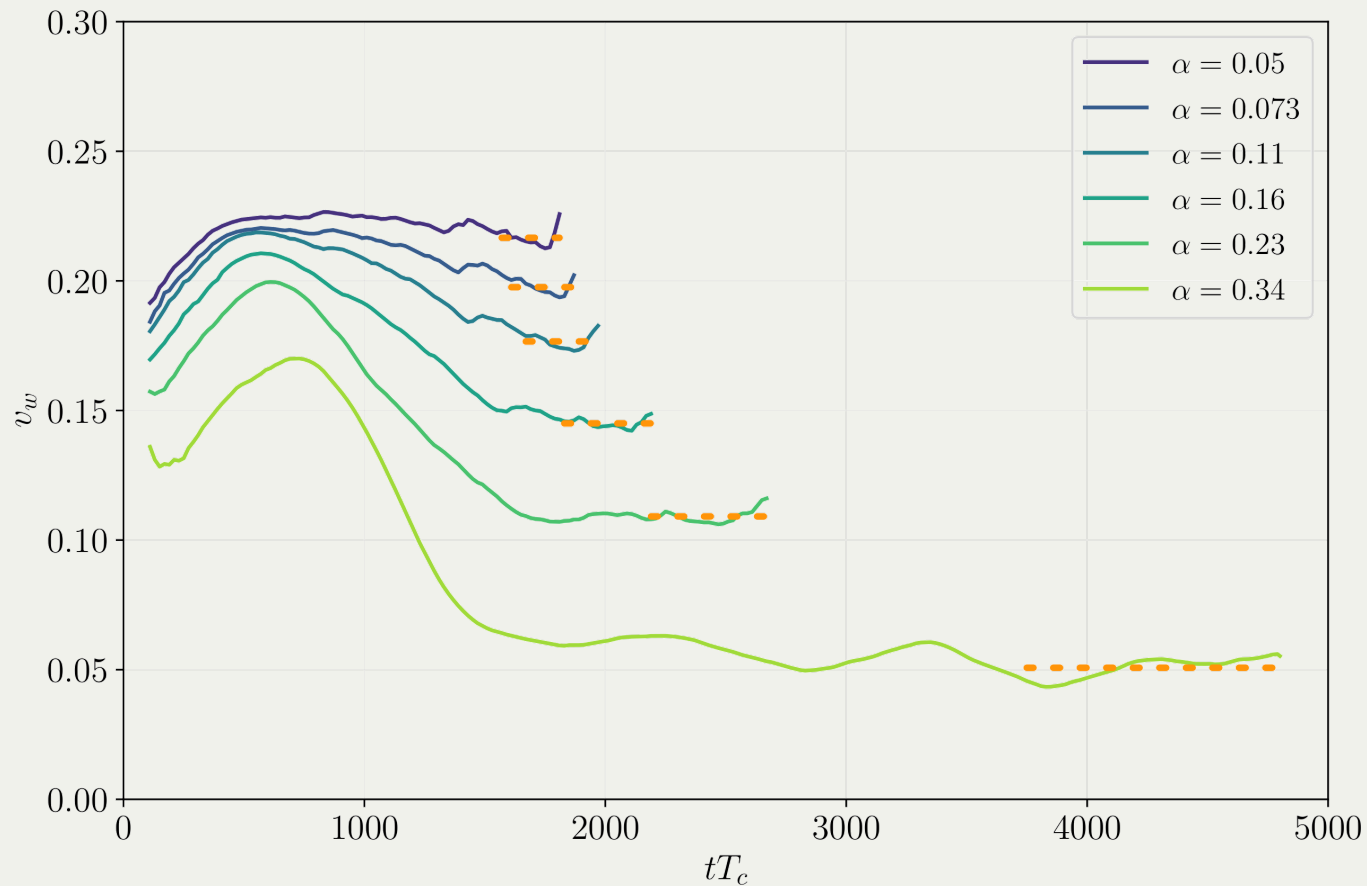
Strong simulation velocity slice

$[\alpha_{T_*} = 0.34, v_w = 0.24 \text{ [deflag.]}]$, velocity \mathbf{v}



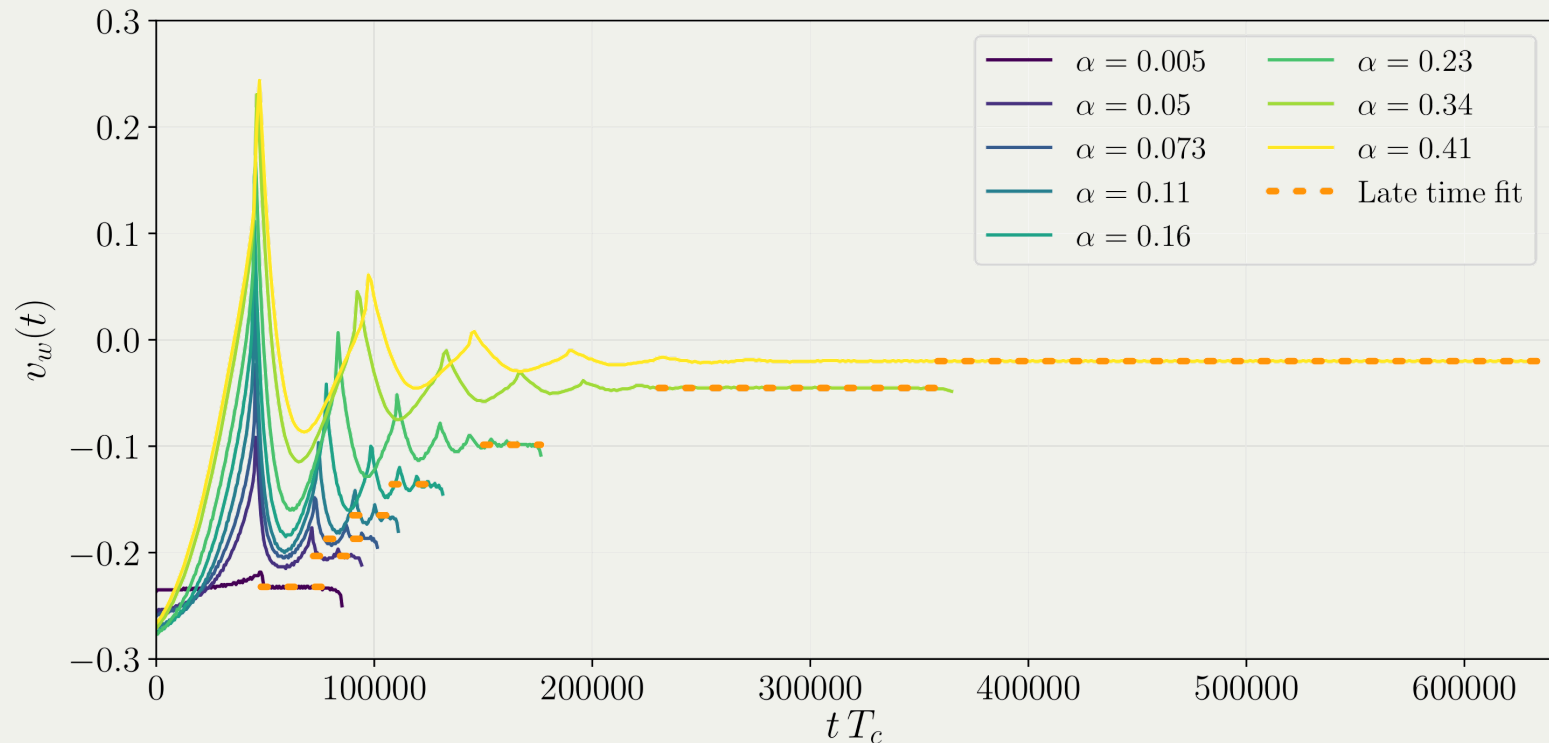
Walls slow, droplets form

At large α_{T^*} reheated droplets form in front of the walls



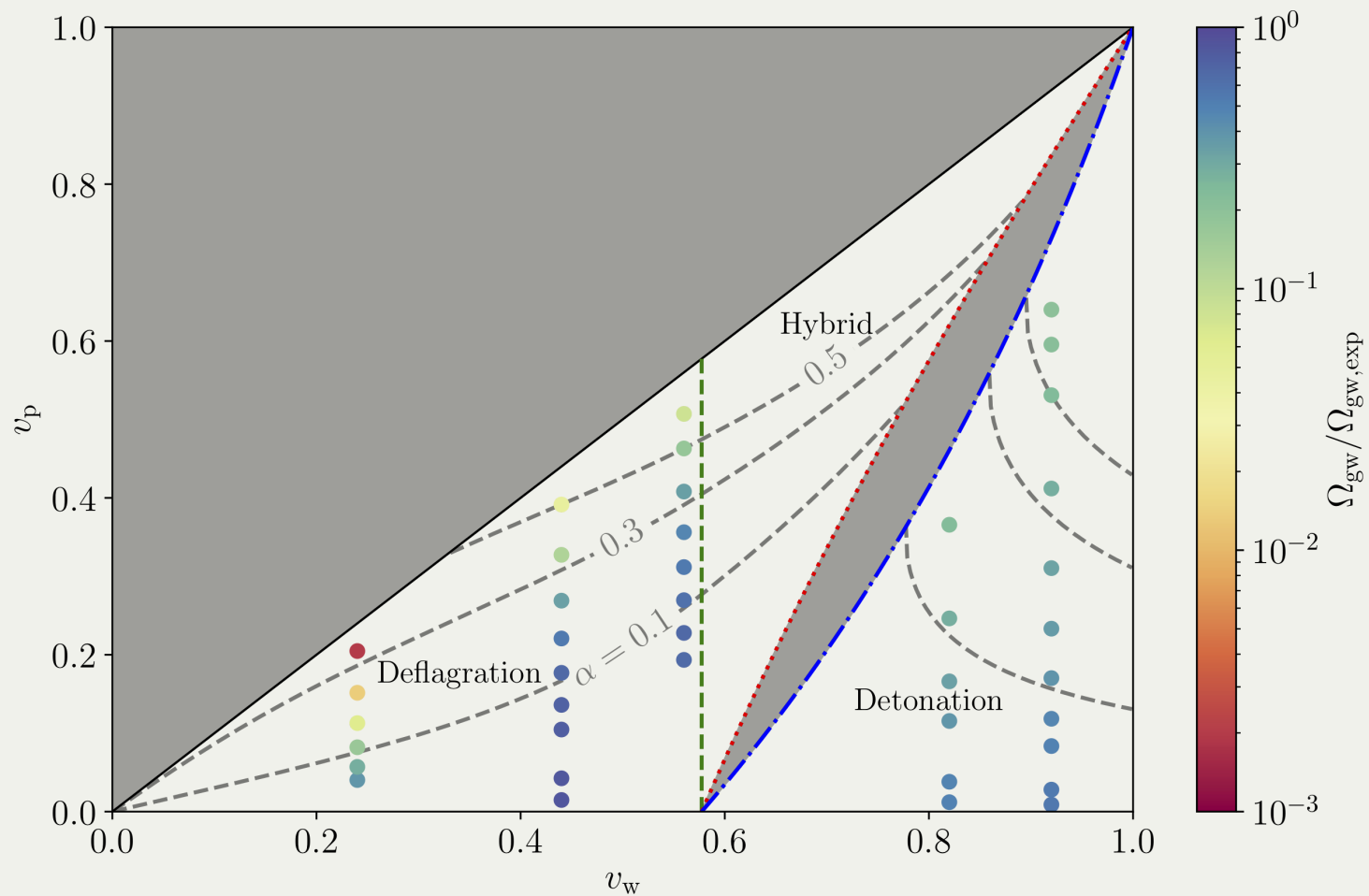
Isolated spherical droplets

In the spherical case, we can get a self-similar droplet.
We see the same wall velocity slowdown:



Droplets may suppress GWs

Suppression compared to sound waves [redder = worse]



arXiv:1906.00480

Thanks

- **Students:**

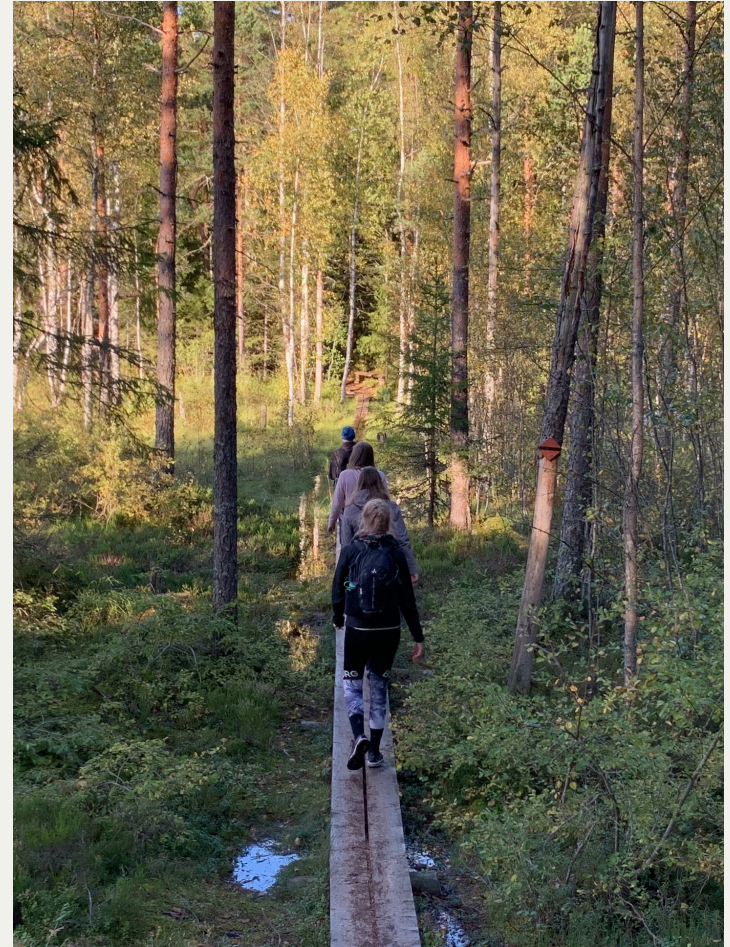
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Musolf, Kari Rummukainen,
Tuomas Tenkanen



What I want you to remember

- **Dimensional reduction**, a valuable field theory tool
⇒ test perturbative studies of phase transitions
 - Strong phase transitions: hot **droplets** slow completion
⇒ also suppress GW production
-

Questions you can ask me

- How accurate are bubble nucleation calculations?
- What about the onset of shocks and turbulence?
- What other physics could explain the GW suppression seen in strong transitions?