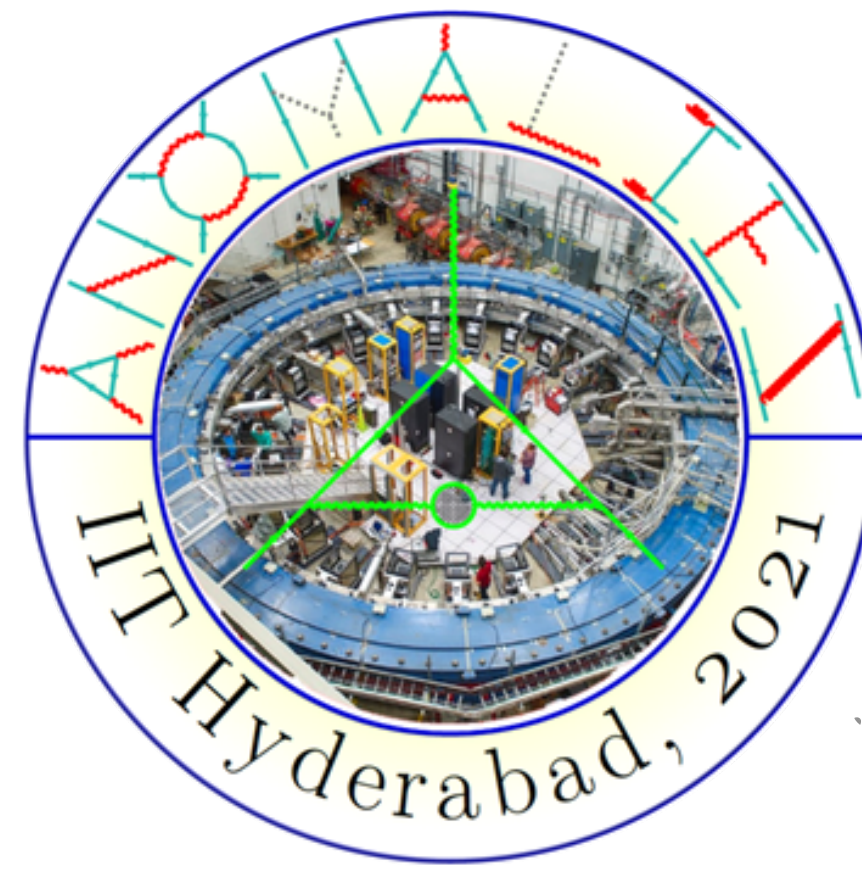


10.11.21



12.11.21

# What's in a hidden $U(1)$ ?

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RECAPP



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# Overview

- An abelian symmetry.
- $U(1)$  is among us and unbroken  $\sim$  massless photon.

Global  $U(1)_B$ ,  $U(1)_L$

- Appears as a remnant in most gauge extensions of the SM.

GUTs, Left-Right symmetry, etc.

- Very useful in model building  $\sim$  simplicity and applications

SUSY, Extradimensions, Neutrino mass,  $g-2$  anomaly, Flavour anomalies, etc.

- Straight forward experimental signatures

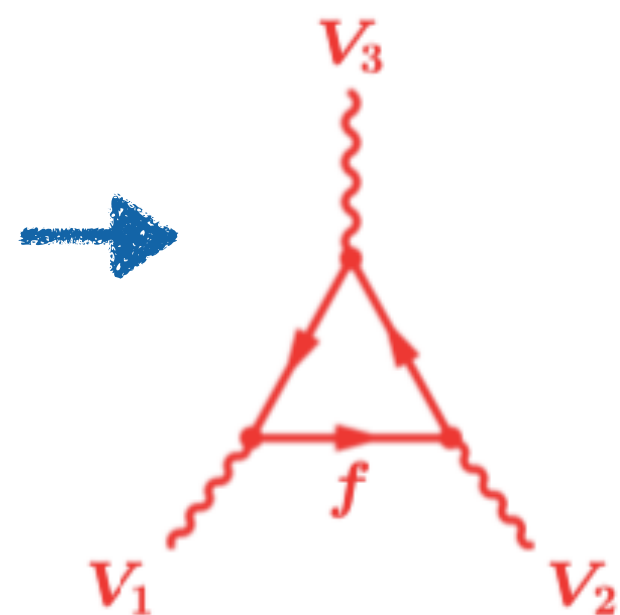
*The Physics of Heavy  $Z'$  Gauge Bosons, RMP 81, 1199 (0801.1345)*

- Charge assignment is easier to decipher through observables

# $Z'$

- Simple extension to SM:  $\mathcal{G}_{SM} \times U(1)'$
- $Z'$  couplings to SM fields start depending on the matter content added

- Anomalies



new fields  $f$  (vector-like)

Most of  $U(1)'$  constructions need additional fermions to cancel the triangle anomalies.

- Numerous possibilities with no fixed rule: lepton specific, hadrophobic, etc.
- Signal for the commonly studied scenario at colliders involves only the associated neutral current with simple assumptions  $\sim \mathcal{L} \subset g' J^\mu Z'_\mu$

$$J^\mu = f (q_L^f, q_R^f)$$

Quasi-Chiral : vector-like under SM but chiral under  $U(1)'$ .




## SM as an example:

$$\text{Neutral current : } \mathcal{L}_Z = \frac{g}{\cos \theta_w} J_Z^\mu Z_\mu$$

- SM quarks :  $J_Z^\mu = \bar{u}_L \gamma^\mu \left( \frac{1}{2} - Q \sin^2 \theta_w \right) u_L + \bar{u}_R \gamma^\mu \left( 0 - Q \sin^2 \theta_w \right) u_R$

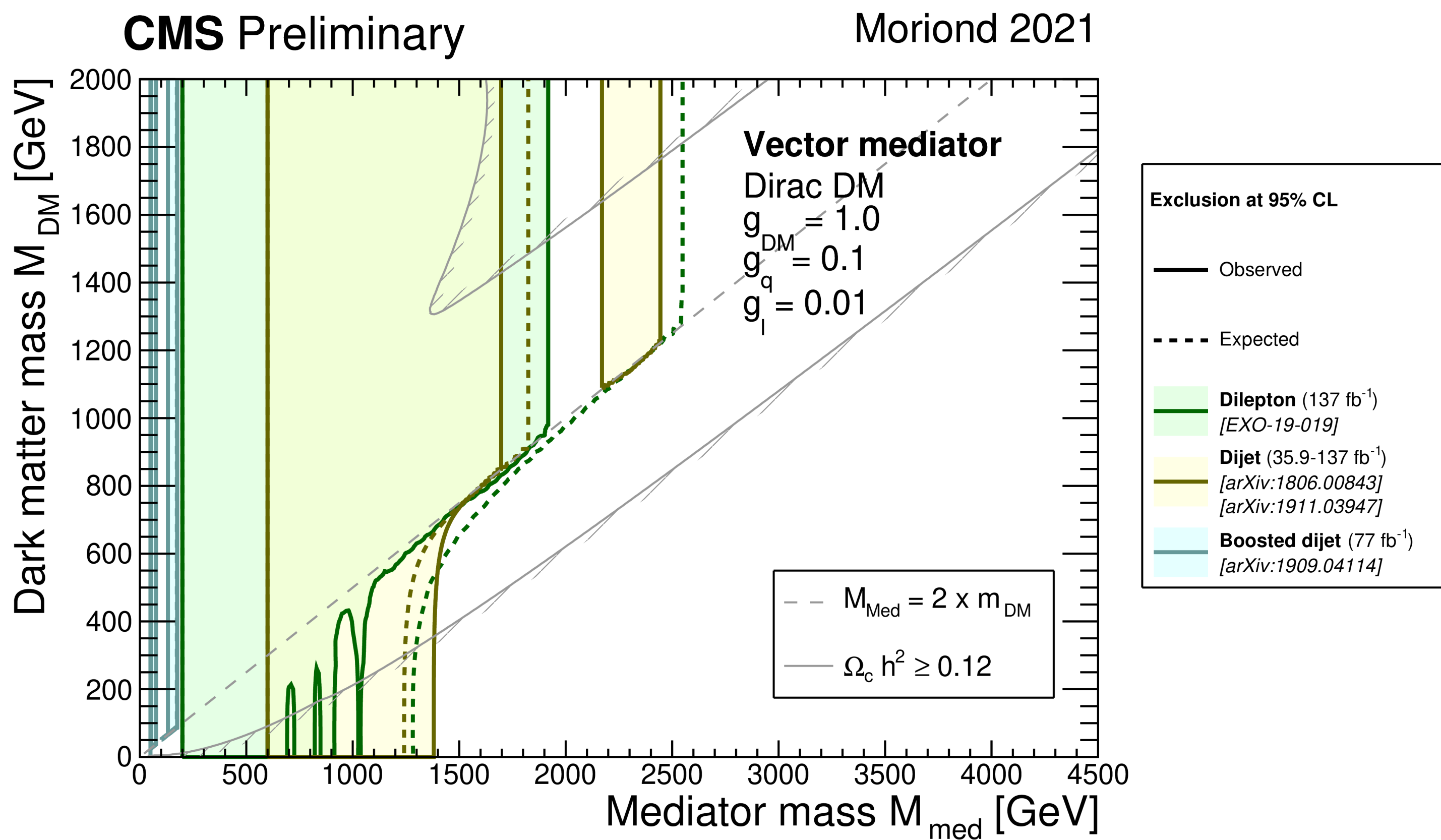
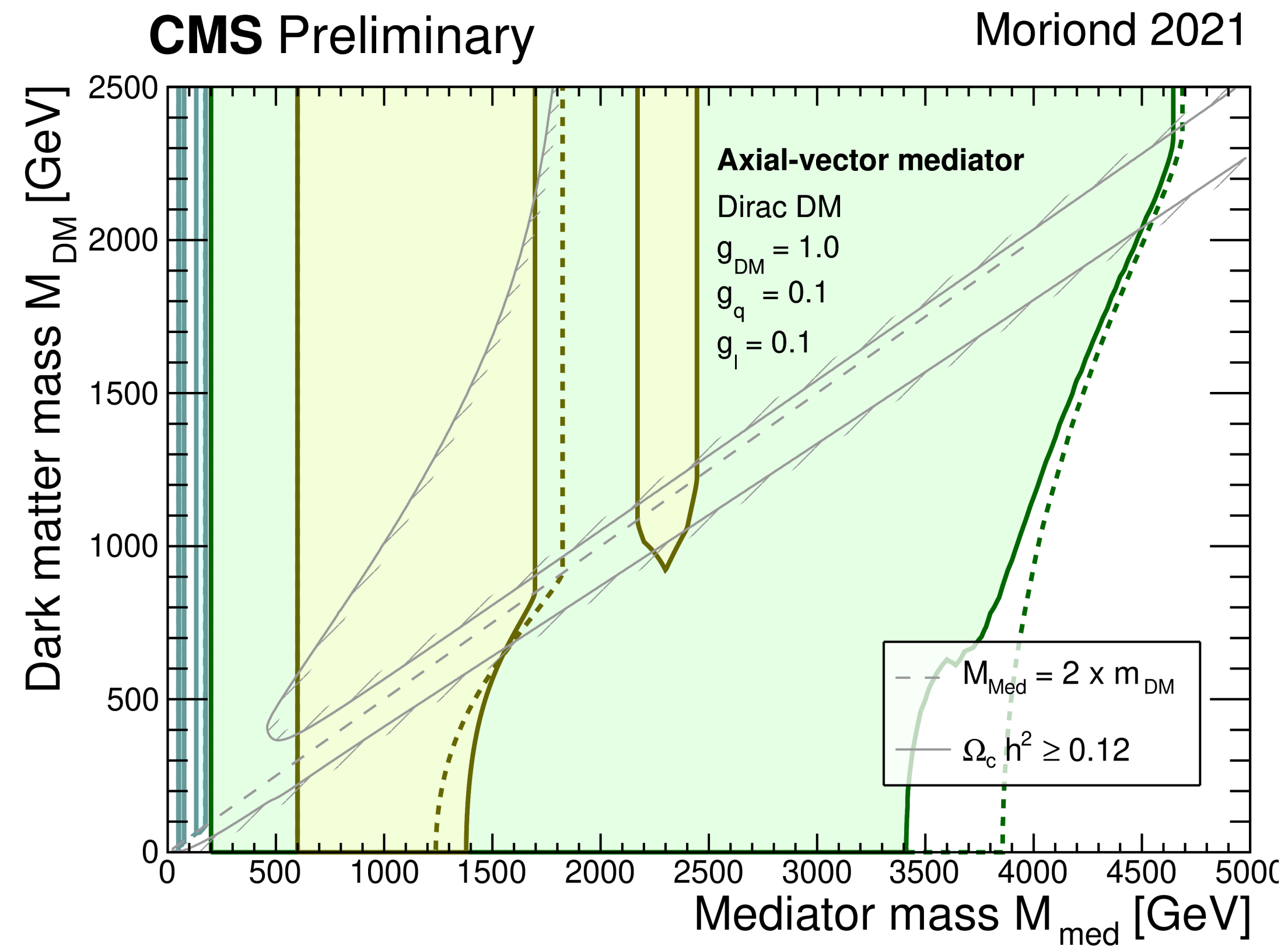
- Vector-like quarks :

- Doublet :

$$J_Z^\mu = \bar{xu}_L \gamma^\mu \left( \frac{1}{2} - Q \sin^2 \theta_w \right) xu_L + \bar{xu}_R \gamma^\mu \left( \frac{1}{2} - Q \sin^2 \theta_w \right) xu_R$$
$$= \left( \frac{1}{2} - Q \sin^2 \theta_w \right) \bar{xu} \gamma^\mu xu \equiv V$$


- In most models, the SM fermions and the Electroweak Higgs boson carry non-trivial charges under the U(1), e.g. remnants from GUTs
- Other variations of the extra U(1) symmetry: hadro-phobic U(1), lepto-phobic U(1), extra U(1) coupling only to the third family of fermions, etc.

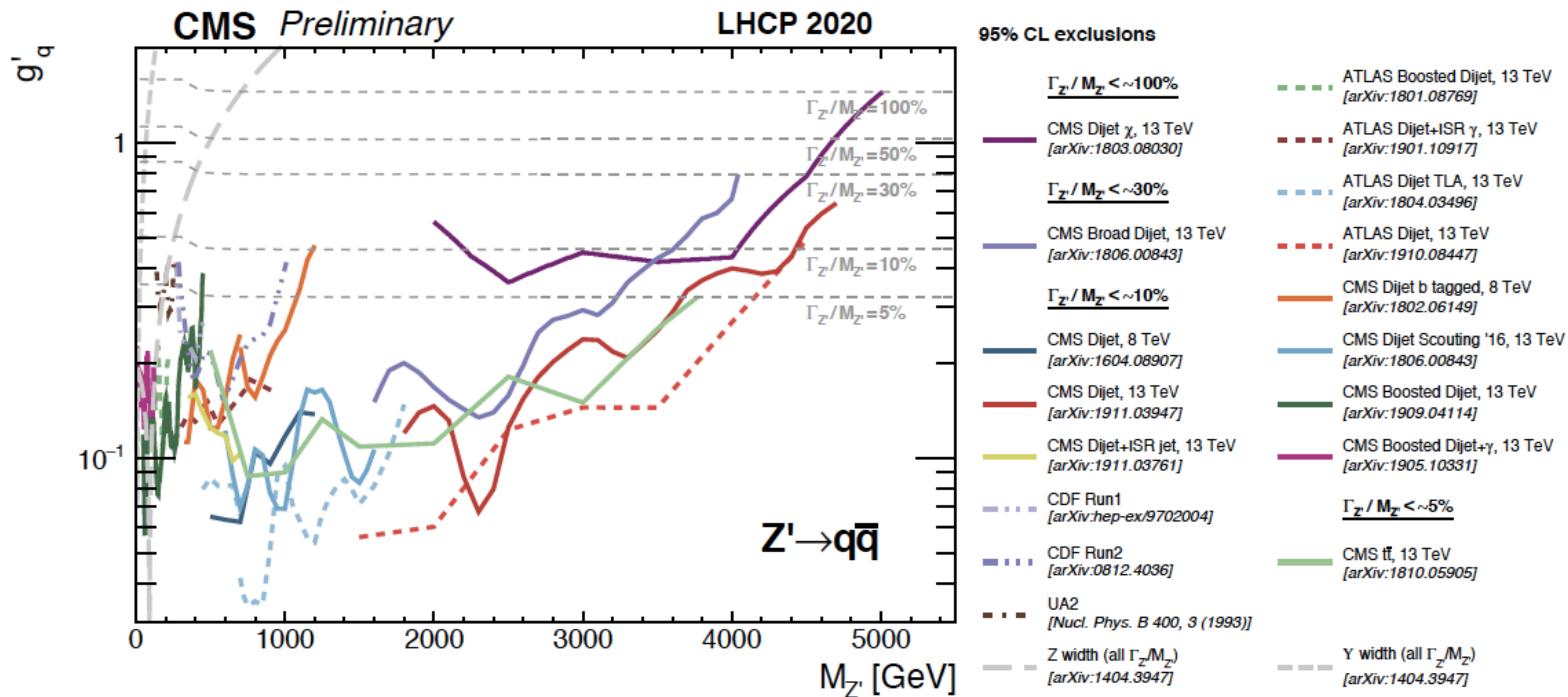
# Z' exclusions





# Z' exclusions

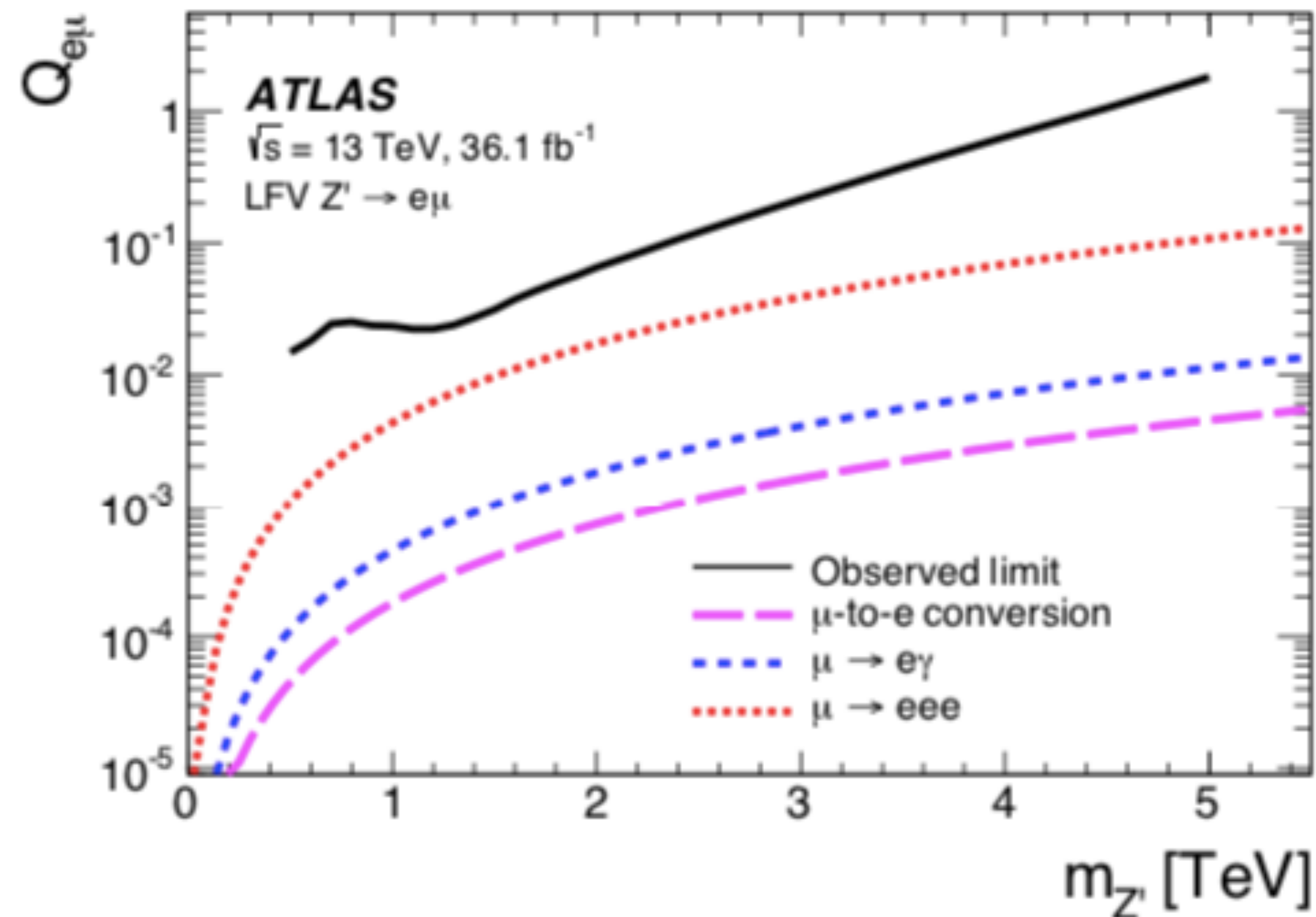
## Leptophobic Z'



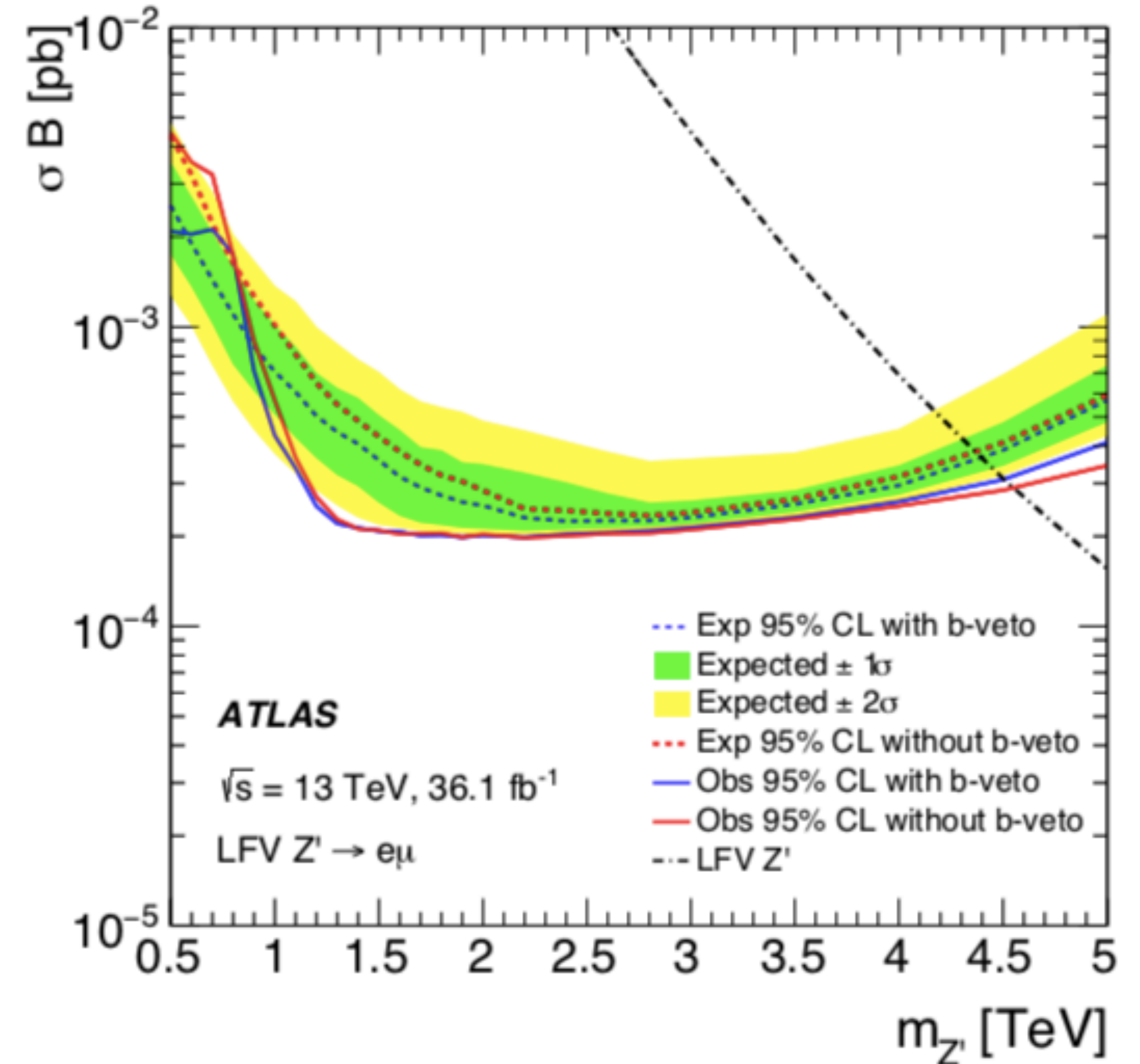
# $Z'$ exclusions

## LFV searches for $Z'$ at LHC

- Sequential  $Z_{SM}$
- $Z'$  couplings are SM like
- $Q_{ll'}$  represents the relative LFV strength



$$pp \rightarrow Z' \rightarrow \ell\ell'$$





TeV scale remnant  $U(1)'$  from :

$$E_6 \rightarrow SO(10) \times U(1)_\psi \rightarrow SU(5) \times U(1)_\chi \times U(1)_\psi$$

The unbroken symmetry at TeV scale:

$$SU(3)_C \times SU(2)_L \times U(1)_Y \times U(1)'$$

The unbroken  $U(1)'$  at TeV scale:

$$Q' = \cos \theta Q_\chi + \sin \theta Q_\psi, \quad \tan \theta = \sqrt{5/3}.$$

$$\tan \theta = \sqrt{5/3} \Rightarrow SN_i^c N_i^c \text{ term possible. (Neutrino Mass)}$$

Divide  $U(1)'$  charges by  $4\sqrt{15}$

$$-\mathcal{L}_y = y_{ij}^U Q_i U_j^c H_u + y_{ij}^D Q_i D_j^c H_d + y_{ij}^E L_i E_j^c H_d + y_{ij}^N L_i N_j^c H_u \\ + y_{ij}^{XNd} X L_i^c X N_j H_d + y_{ij}^{XNu} X L_i X N_j H_u + y_{ij}^{TD} D_i^c X D_j T \\ + y_{ij}^{TL} X L_i^c L_j T + y_{ij}^{SD} X D_i^c X D_j S + y_{ij}^{SL} X L_i^c X L_j S \\ + y_{ij}^{SN} S N_i^c N_j^c + y_{ij}^{TXNN} T X N_i^c N_j^c + \text{H.C.}$$

| $SO(10)$ | $SU(5)$   | Fields        | $SU(3)_C \times SU(2)_L \times U(1)_Y \times U(1)'$ |
|----------|-----------|---------------|---|
|          |           | $Q_i$         | $(3, 2, 1/6, 1)$                                    |
|          |           | $U_i^c$       | $(\bar{3}, 1, -2/3, 1)$                             |
|          |           | $E_i^c$       | $(1, 1, 1, 1)$                                      |
|          |           | $D_i^c$       | $(3, 1, 1/3, 7)$                                    |
|          |           | $L_i$         | $(1, 2, -1/2, 7)$                                   |
|          |           | $N_i^c / T$   | $(1, 1, 0, -5)$                                     |
| 10       | 5         | $XD_i$        | $(3, 1, -1/3, -2)$                                  |
|          |           | $XL_i^c, H_u$ | $(1, 2, 1/2, -2)$                                   |
|          | $\bar{5}$ | $XD_i^c$      | $(\bar{3}, 1, 1/3, -8)$                             |
|          |           | $XL_i, H_d$   | $(1, 2, -1/2, -8)$                                  |
| 1        | 1         | $XN_i, S$     | $(1, 1, 0, 10)$                                     |



- No direct hint of a  $U(1)$  extension yet. If present how can it hide?
- Very weakly coupled  $\longrightarrow$  very narrow resonance
- Many new exotic decay modes  $\longrightarrow$  very broad resonances

Cascade decays, dominant invisible decay to DM ?

- So what if it does not couple to SM directly?

Difficult to produce directly which is likely to keep it hidden

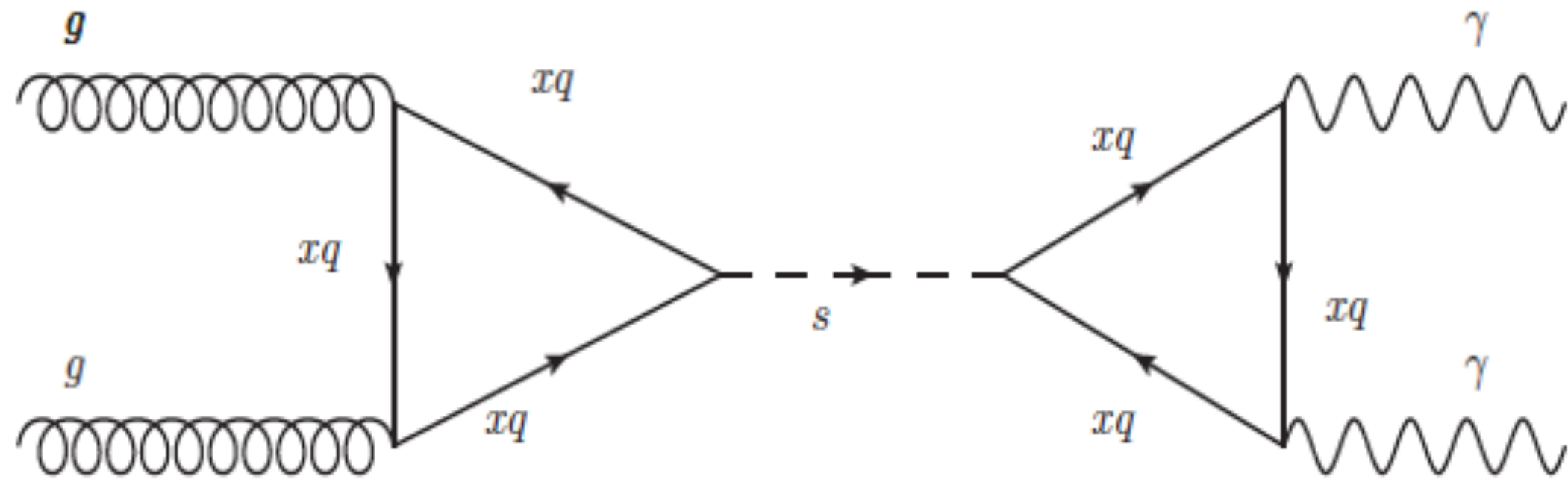
Rely on mixing, associated production, observation as a decay product ?

# Vector-like quarks in a hidden $U(1)$ extension.

Hidden  $U(1)$  : Standard Model fields are neutral under  $U(1)'$ .

|        |   |
|--------|---|
| $S_1$  | $(1, 1, 0, q')$                         |
| $S_2$  | $(1, 1, 0, 0)$                          |
| $xq_L$ | $(3, 1, -1/3, q')$ or $(3, 1, 2/3, q')$ |
| $xq_R$ | $(3, 1, -1/3, q')$ or $(3, 1, 2/3, q')$ |

•  $-\mathcal{L}_{\text{Yukawa}} \supset M_x \bar{xq}_L xq_R + Y_{xa} \bar{xq}_L q_R S_1 + f_X \bar{xq}_L xq_R S_2 + \text{H.C}$



750 GeV diphoton excess in a  $U(1)$  hidden symmetry model.

Phys. Rev. D 93 095007 (2016), K. Das, S.K. Rai

- $Z'$  connects to the SM sector through  $\langle S_1 \rangle$
- Direct production via  $q - xq$  or  $Z - Z'$  mixing
- Pair production via  $S - H_{SM}$  mixing
- Production from the decay of heavy  $xq, S$



## Observable effects of vector-like quarks :

- Indirect observations
  - Rare top decays :  $t \rightarrow Zq$  (FCNC)
  - Meson mixings and decay. (Tree level FCNC and VLQ in the loop).
  - Modifications to CKM matrix.
  - Modification of  $Zc\bar{c}$ ,  $Zb\bar{b}$ ,  $Zu\bar{u}$ ,  $Zd\bar{d}$  couplings.
  - $S$ ,  $T$ ,  $U$  parameters (VLQ in the loop.)
  - Higgs coupling with gluons and photons.

Production cross section via  $Z'$   
Hints of  $Z - Z'$  mixing  
as well as its mass ?

Not much information on  $Z'$   
Hints of  $Z - Z'$  mixing?

### Direct observations at LHC :

- As Colored particles they will be pair produced.
- Mixing with SM quarks opens up decay modes for VLQ :  
Example:  $+\frac{2}{3}$  charge:  $xt \rightarrow W b, Z t, h t$   
 $-\frac{1}{3}$  charge:  $xb \rightarrow W t, Z b, h b$ .

# Neutrinophilic $U(1)$ model

$$\begin{aligned} \mathcal{L} \supset & (D_\mu H_1)^\dagger D_\mu H_1 + (D_\mu H_2)^\dagger D_\mu H_2 + (D_\mu S)^\dagger D_\mu S - \mu_1 H_1^\dagger H_1 - \mu_2 H_2^\dagger H_2 - \mu_s S^\dagger S \\ & + i \bar{N}_L \gamma^\mu D_\mu N_L + i \bar{N}_R \gamma^\mu D_\mu N_R - \hat{M}_N (\bar{N}_L N_R + \bar{N}_R N_L) - \{Y_\nu \bar{l}_L H_2 N_R + h.c.\} \\ & - \lambda_1 (H_1^\dagger H_1)^2 - \lambda_2 (H_2^\dagger H_2)^2 - \lambda_{12} H_1^\dagger H_1 H_2^\dagger H_2 - \lambda'_{12} |H_1^\dagger H_2|^2 \\ & - \lambda_s (S^\dagger S)^2 - \lambda_{1s} H_1^\dagger H_1 S^\dagger S - \lambda_{2s} H_2^\dagger H_2 S^\dagger S - \{Y_R S \bar{N}_R N_R^C + Y_L S \bar{N}_L N_L^C + h.c.\} \\ & + \left\{ \mu_{12} H_1^\dagger H_2 + h.c. \right\}. \end{aligned}$$

| Fields  | $SU(3)_C$ | $SU(2)_L$ | $U(1)_Y$ | $U(1)_X$ | Spin |
|---------|-----------|-----------|----------|----------|------|
| $H_1$   | 1         | 2         | -1/2     | 0        | 0    |
| $H_2$   | 1         | 2         | -1/2     | $-q_x$   | 0    |
| $S$     | 1         | 1         | 0        | $2q_x$   | 0    |
| $N_L^i$ | 1         | 1         | 0        | $q_x$    | 1/2  |
| $N_R^i$ | 1         | 1         | 0        | $q_x$    | 1/2  |

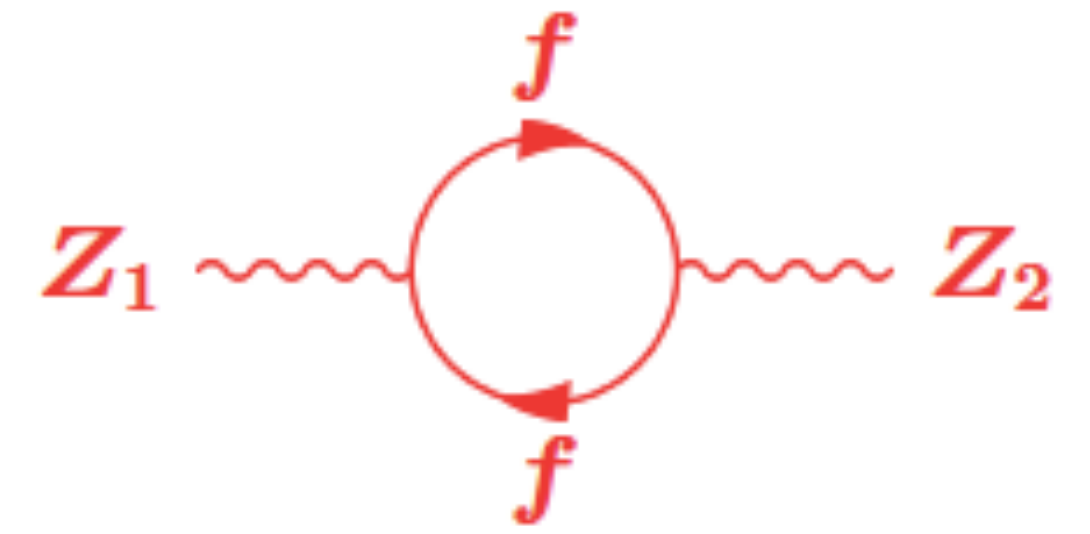
- Neutrino mass via inverse seesaw
- $Z'$  again connects to the SM through  $\langle S_1 \rangle$  but now only to the charge neutral fermions
- Direct production via  $Z - Z'$  mixing
- Pair production via  $S - H_{SM}$  mixing
- Production from the decay of heavy neutrinos

$$\langle H_1 \rangle = \begin{pmatrix} \frac{v_1}{\sqrt{2}} \\ 0 \end{pmatrix}, \quad \langle H_2 \rangle = \begin{pmatrix} \frac{v_2}{\sqrt{2}} \\ 0 \end{pmatrix}, \quad \langle S \rangle = \frac{v_s}{\sqrt{2}}$$



## Gauge kinetic mixing and masses of gauge bosons

$$\mathcal{L} \supset -\frac{1}{4}G^{a,\mu\nu}G_{\mu\nu}^a - \frac{1}{4}W^{b,\mu\nu}W_{\mu\nu}^b - \frac{1}{4}B^{\mu\nu}B_{\mu\nu} - \frac{1}{4}C^{\mu\nu}C_{\mu\nu} + \frac{1}{2}\tilde{g}B^{\mu\nu}C_{\mu\nu},$$



$$M^2 = \frac{1}{4} \begin{pmatrix} g_1^2 v^2 & -g_1 g_2 v^2 & g_1 (g'_x v^2 + 2g_x v_2^2) \\ -g_1 g_2 v^2 & g_2^2 v^2 & -g_2 (g'_x v^2 + 2g_x v_2^2) \\ g_1 (g'_x v^2 + 2g_x v_2^2) & -g_2 (g'_x v^2 + 2g_x v_2^2) & g_x'^2 v^2 + 4g_x g'_x v_2^2 + 4g_x^2 (v_2^2 + 4v_s^2) \end{pmatrix}$$

Mass matrix for single  $Z'$

$$M_{Z-Z'}^2 = \begin{pmatrix} M_{Z^0}^2 & \Delta^2 \\ \Delta^2 & M_{Z'}^2 \end{pmatrix}$$

$$\tan^2 \theta = \frac{M_{Z^0}^2 - M_1^2}{M_2^2 - M_{Z^0}^2}$$

• Eigenvalues  $M_{1,2}^2$ , mixing angle  $\theta$

**constraints:** Measurements at the  $Z$ -pole,  $Z$  width and decays

four-fermi operator interfering with  $\gamma, Z$

Resonance in  $pp, \bar{p}p \rightarrow e^+e^-, \mu^+\mu^-, \dots$

**Search for high-mass dilepton resonances using  
139 fb<sup>-1</sup> of *pp* collision data collected at  
 $\sqrt{s} = 13$  TeV with the ATLAS detector**

Table 3: Observed and expected 95% CL lower limits on  $m_{Z'}$  for three  $Z'$  gauge boson models, quoted to the nearest 100 GeV in the  $ee$  and  $\mu\mu$  channels as well as their combination ( $\ell\ell$ ).

| Model      | Lower limits on $m_{Z'}$ [TeV] |     |          |     |            |     |
|------------|--------------------------------|-----|----------|-----|------------|-----|
|            | $ee$                           |     | $\mu\mu$ |     | $\ell\ell$ |     |
|            | obs                            | exp | obs      | exp | obs        | exp |
| $Z'_\psi$  | 4.1                            | 4.3 | 4.0      | 4.0 | 4.5        | 4.5 |
| $Z'_\chi$  | 4.6                            | 4.6 | 4.2      | 4.2 | 4.8        | 4.8 |
| $Z'_{SSM}$ | 4.9                            | 4.9 | 4.5      | 4.5 | 5.1        | 5.1 |

Upper limits on mixing parameters  $\xi_{Z-Z'}$  at 95% C.L.

$pp \rightarrow W'/Z' \rightarrow WZ/WW (\rightarrow qq\bar{q}\bar{q}), \mathcal{L}_{\text{int}} = 139 \text{ fb}^{-1}$

|              |                     |
|--------------|---------------------|
| $\xi_{Z-Z'}$ | @ $M_{V'}$<br>(TeV) |
|--------------|---------------------|

|                     |         |
|---------------------|---------|
| $3.1 \cdot 10^{-4}$ | 1.3–5.0 |
|---------------------|---------|



Redefining fields:

$$\begin{aligned} B^\mu &= B'^\mu + \frac{\tilde{g}}{\sqrt{1-\tilde{g}^2}} C'^\mu, \\ C^\mu &= \frac{1}{\sqrt{1-\tilde{g}^2}} C'^\mu. \end{aligned} \quad \longrightarrow \quad \begin{pmatrix} Z_\mu \\ Z'_\mu \end{pmatrix} = \begin{pmatrix} \cos \theta' & \sin \theta' \\ -\sin \theta' & \cos \theta' \end{pmatrix} \begin{pmatrix} X_\mu \\ C'_\mu \end{pmatrix},$$

$g_x$  :  $U(1)'$  gauge coupling,  $g'_x$  : gauge-kinetic mixing

$Z - Z'$  mixing angle

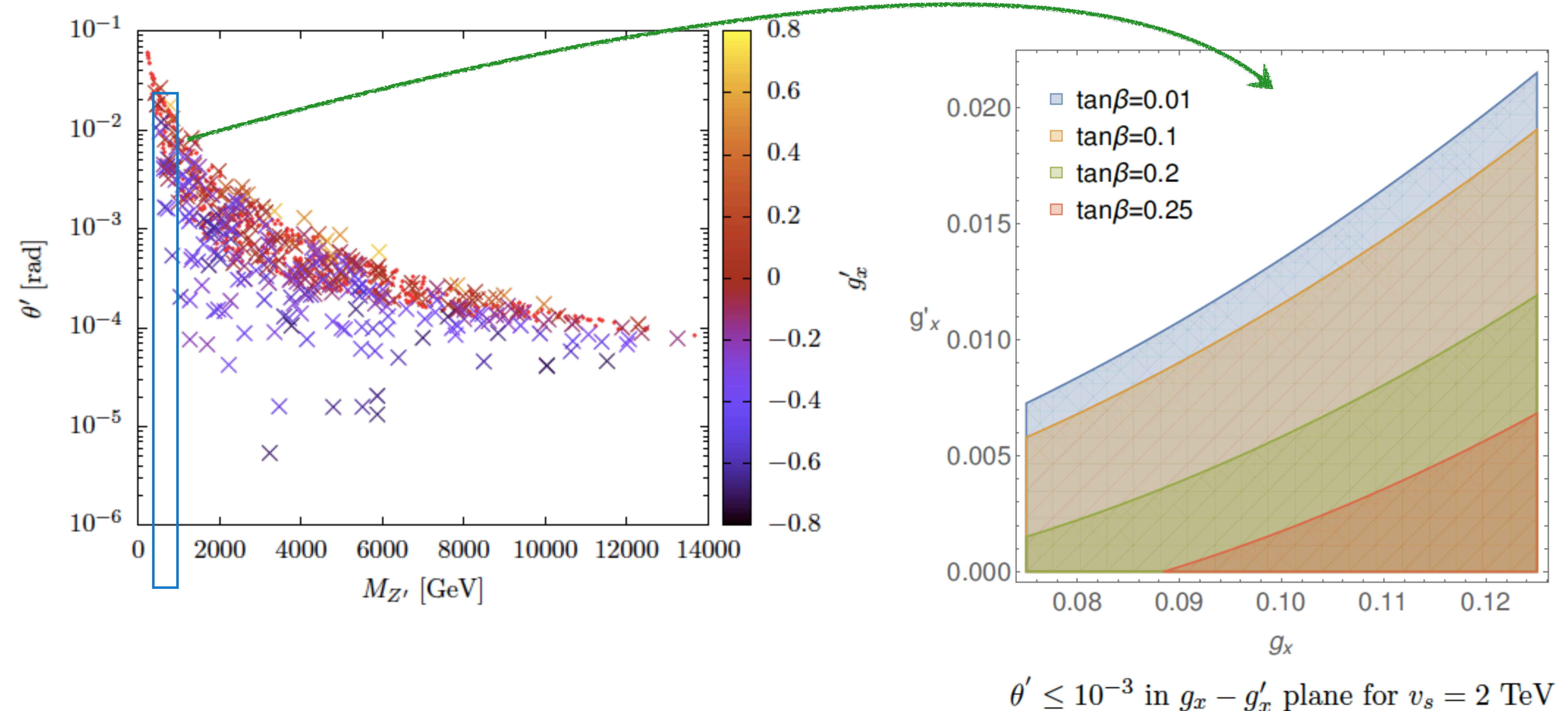
$$\tan 2\theta' = \frac{2g_z (g'_x v^2 + 2g_x v_2^2)}{g_x'^2 v^2 + 4g_x g'_x v_2^2 + 4g_x^2 (v_2^2 + 4v_s^2) - g_z^2 v^2}.$$

Non-zero  $\theta'$  for  $g'_x = 0$

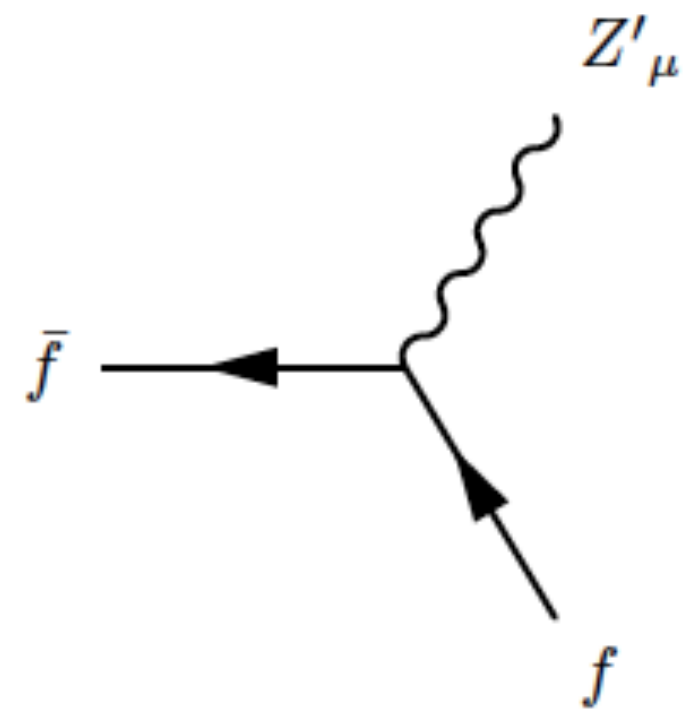
Numerator  $\propto (2g_x + g'_x)$  ;  $v_1 \ll v_2 \sim v \longrightarrow$  cancelation leads to small mixing  
Found to be disfavoured by Higgs data

We note that  $g'_x \lesssim 10^{-2}$  is sufficient to keep  $\theta' < 10^{-3}$ .

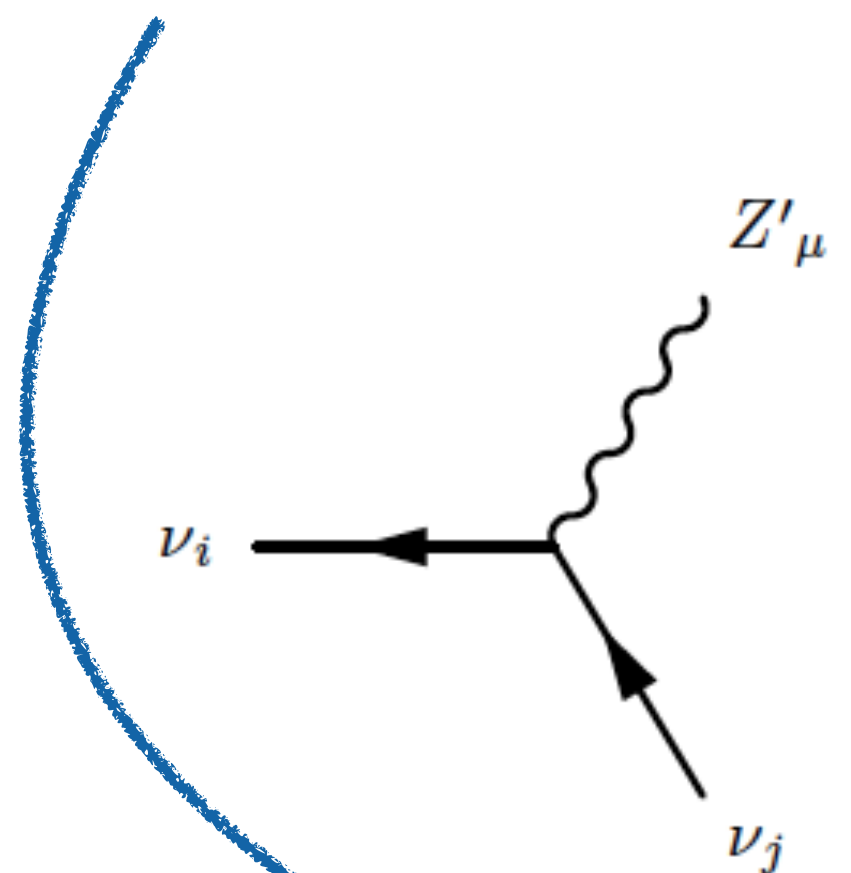
# $Z - Z'$ mixing angle dictated parameter space







$$i \left( \frac{e s_{\theta'}}{s_W c_W} (T^3 - Q_f s_W^2) + g'_x c_{\theta'} (T^3 - Q_f) \right) \gamma^\mu P_L - i \left( \frac{e s_{\theta'}}{s_W c_W} Q_f s_W^2 + g'_x c_{\theta'} Q_f \right) \gamma^\mu P_R$$



$$\frac{i}{2} \left( \left( \frac{e s_{\theta'}}{2 s_W c_W} + \frac{g'_x}{2} c_{\theta'} \right) \sum_{k=1}^3 \mathcal{N}_{ik} \mathcal{N}_{jk}^* - g_x c_{\theta'} \left( - \sum_{k=6}^9 \mathcal{N}_{ik} \mathcal{N}_{jk}^* + \sum_{k=4}^6 \mathcal{N}_{ik} \mathcal{N}_{jk}^* \right) \right) \gamma^\mu P_L$$

$$- \frac{i}{2} \left( \left( \frac{e s_{\theta'}}{2 s_W c_W} + \frac{g'_x}{2} c_{\theta'} \right) \sum_{k=1}^3 \mathcal{N}_{ik}^* \mathcal{N}_{jk} - g_x c_{\theta'} \left( - \sum_{k=6}^9 \mathcal{N}_{ik}^* \mathcal{N}_{jk} + \sum_{k=4}^6 \mathcal{N}_{ik}^* \mathcal{N}_{jk} \right) \right) \gamma^\mu P_R$$

$\mathcal{N}$  is the neutrino mixing matrix

Signal:

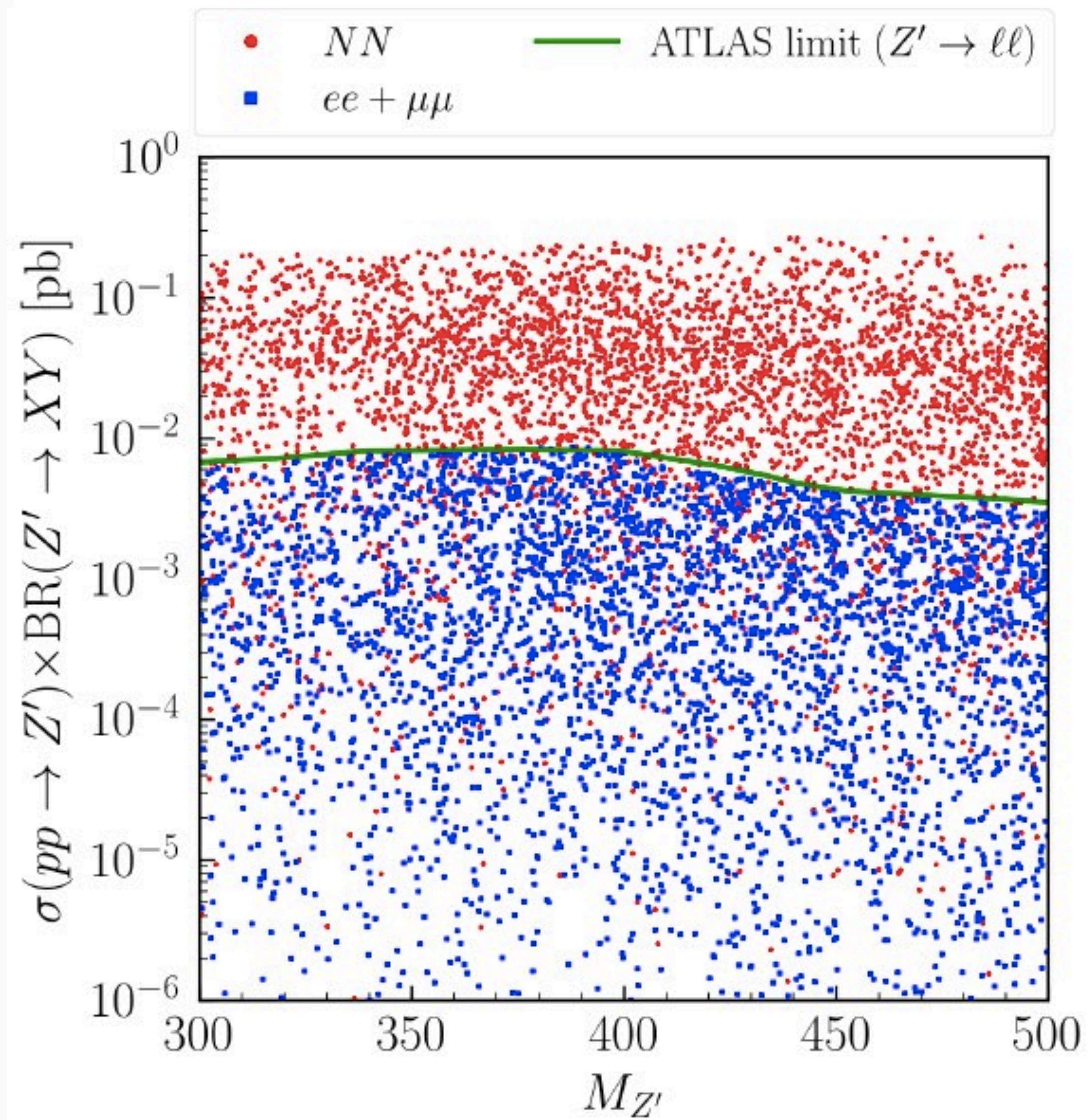
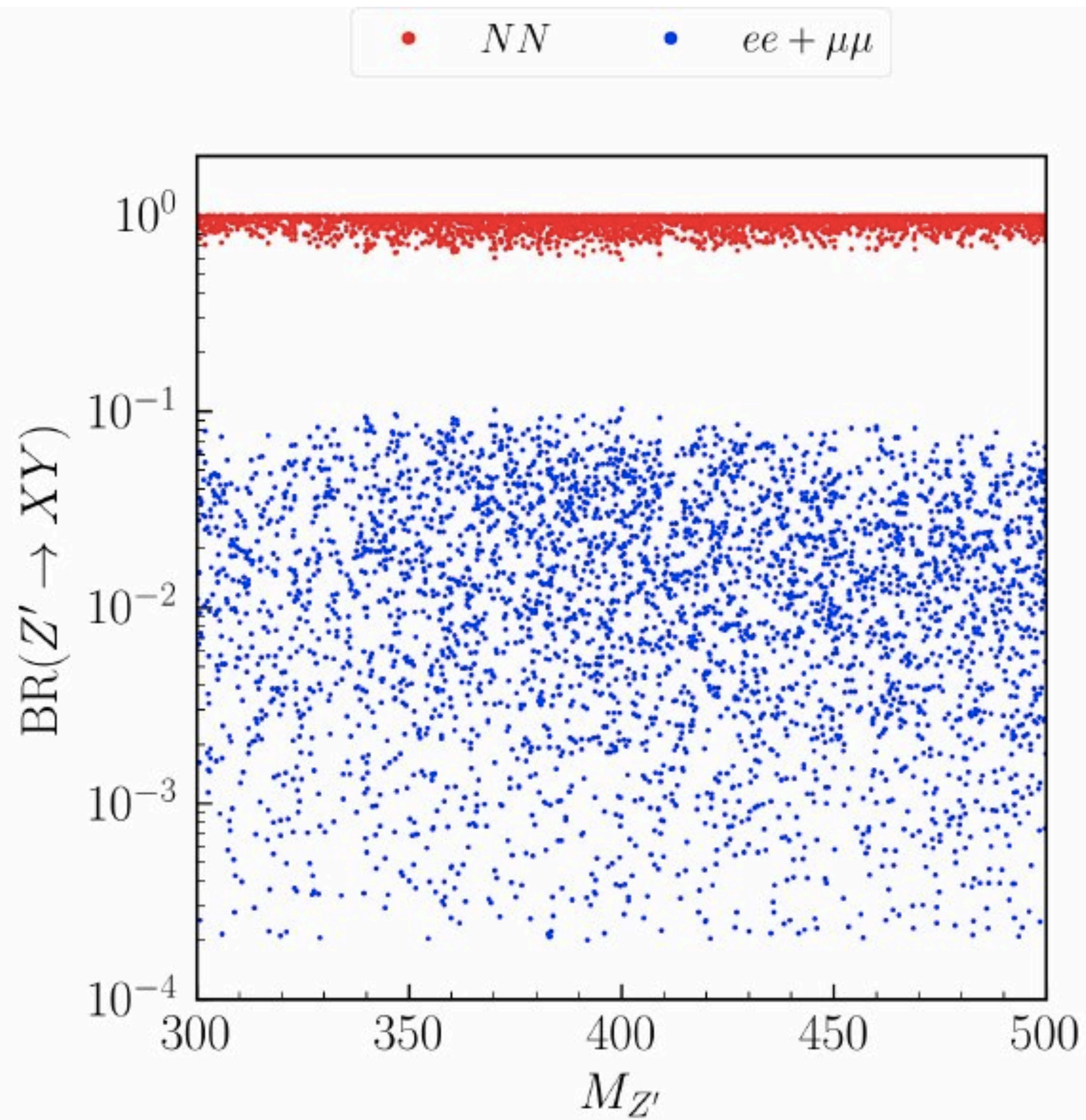
$$pp \rightarrow Z' \rightarrow NN$$

$$2M_N < M_{Z'}:$$

$$Z' \rightarrow NN \simeq 100\%:$$

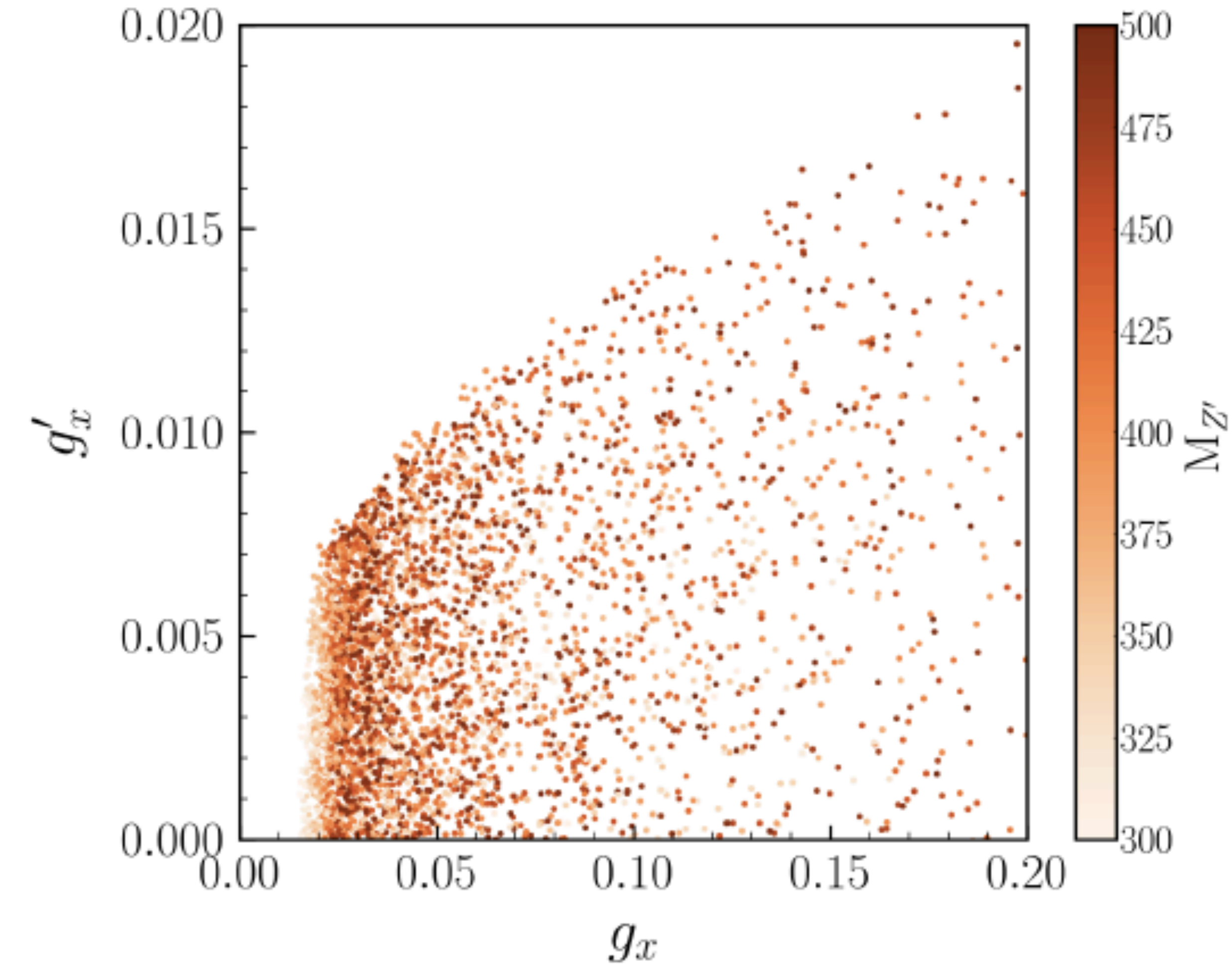


$$g'_x < 0.02$$





Scatter plot of points satisfying  
experimental constraints



Signal:  $N \rightarrow \ell W, \nu Z$

- $4\ell + \cancel{E}_T$

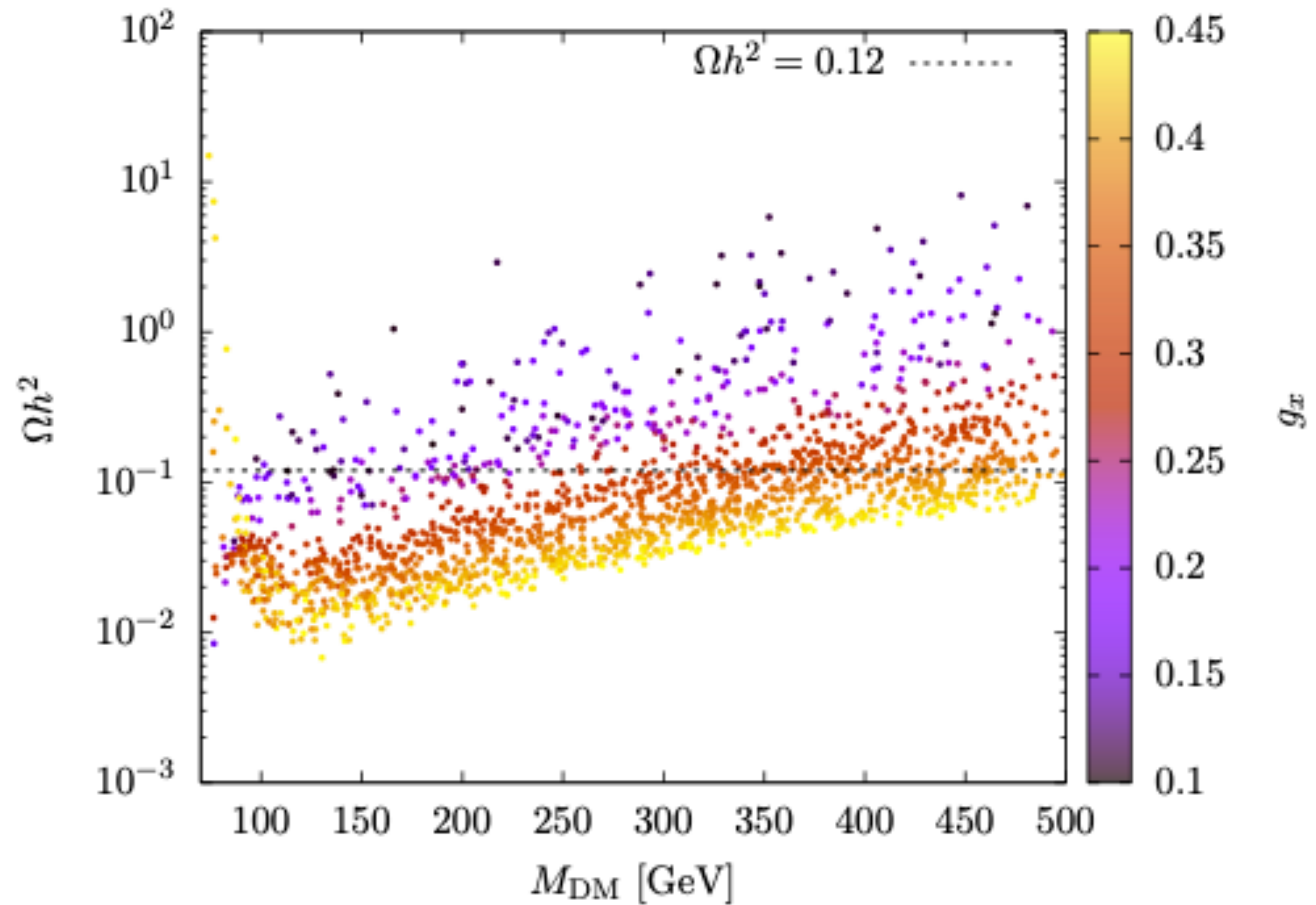
- $3\ell + 2j + \cancel{E}_T$

- $2\ell + 4j + \cancel{E}_T$

- $4j + \cancel{E}_T$  (when only  $N \rightarrow \nu Z$  decay is considered.)

$Z'$  phenomenology is only dependent on kinetic mixing and its coupling to exotic sector

- What if we now get rid of the  $Z$ - $Z'$  mixing too?
- Set  $\tan \beta = v_2/v_1 \simeq 10^{-5}$  and  $g'_x = 0$
- Makes the  $Z'$  practically invisible to SM fields
- In addition choose  $Y_{\nu_{11}} \lesssim 10^{-27}$ ,  $Y_{\nu_{1j}} = 0$  which makes the lightest  $N_k$  stable (DM candidate)



Dominant annihilation channels

$$N_k N_l \rightarrow Z' Z', H_s H_s, H_s Z' \quad (k, l = 4, 5)$$

Light  $Z'$  and/or  $H_s$



$$pp \rightarrow h_{1,2} \rightarrow Z' Z'.$$

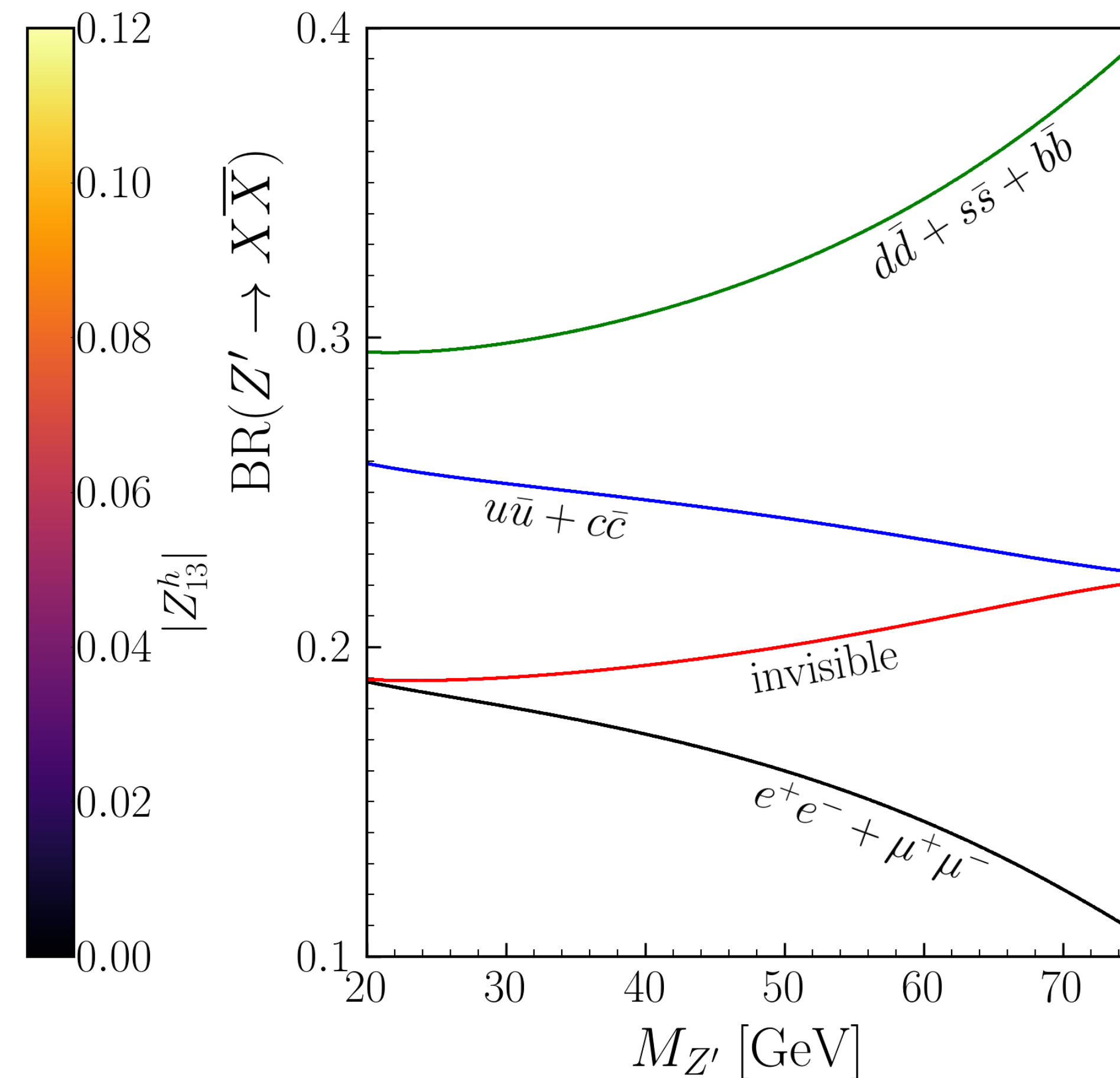
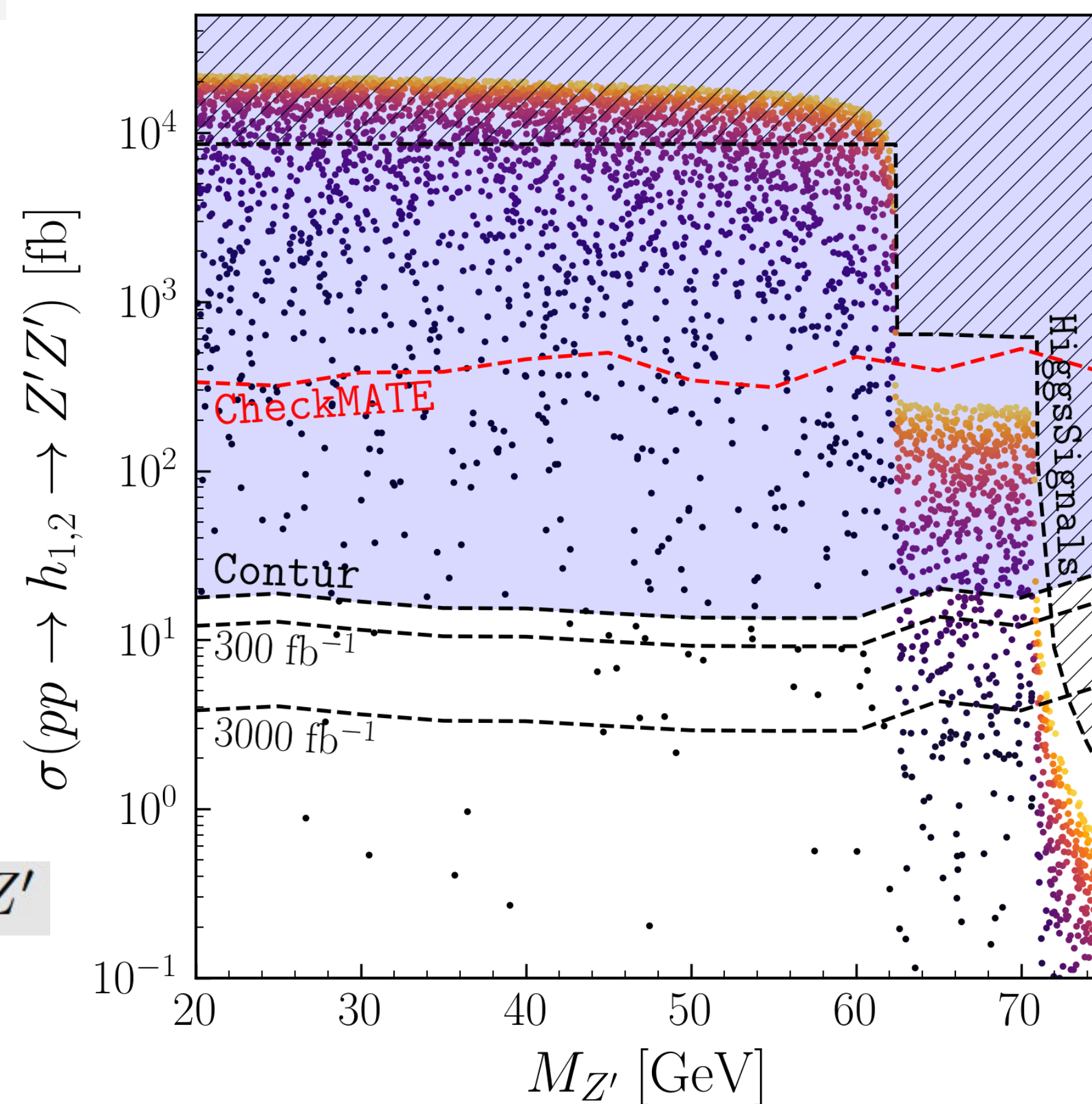
Abdallah, Barik, SKR, Samui; 2109.07980

Accomando et.al. 1708.03650; Amrith et.al. 1811.11452

G. Aad *et al.* (ATLAS), **JHEP** **07**, 005 (2021),  
arXiv:2103.01918 [hep-ex].

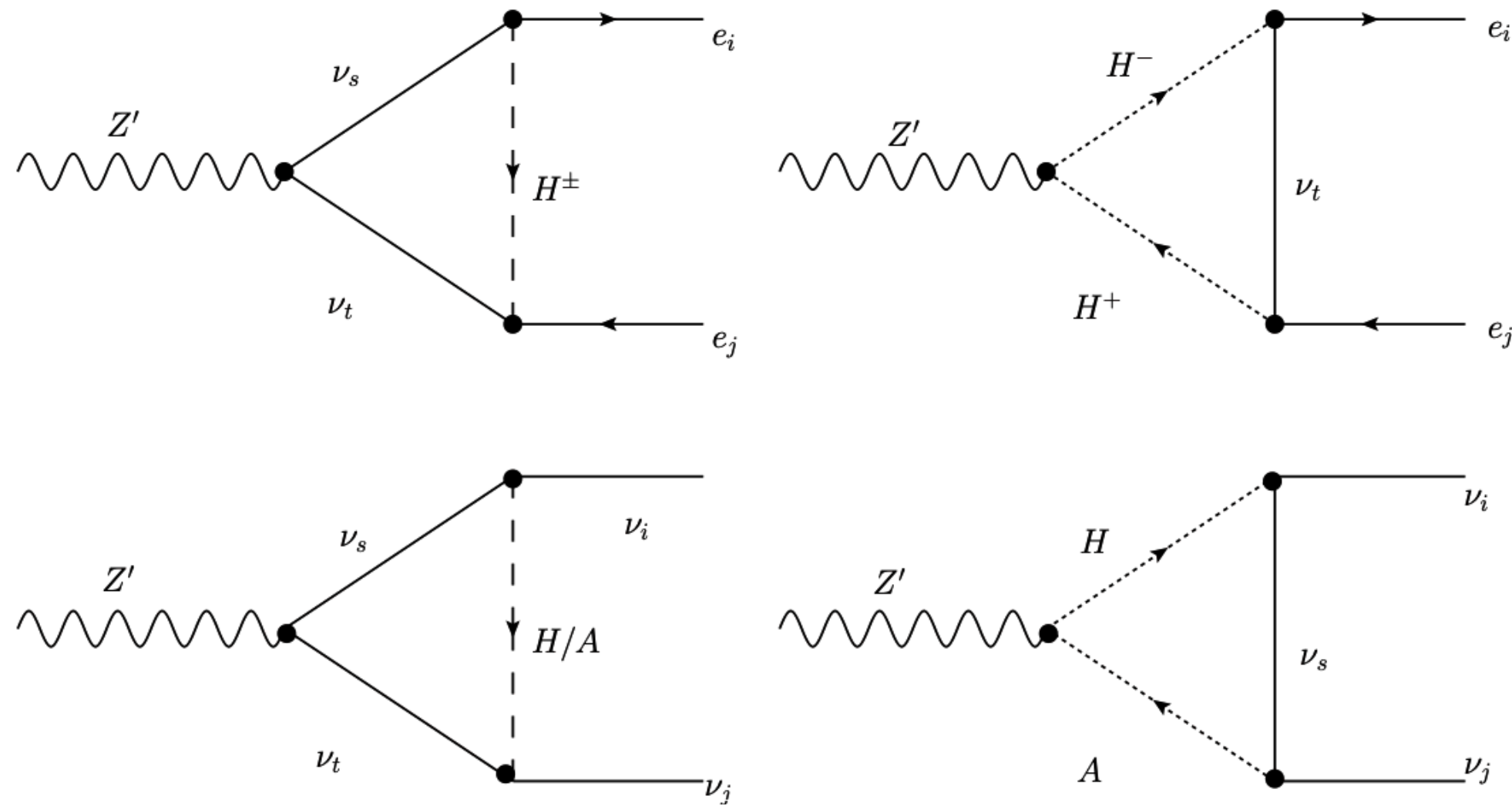
measurement of the  
4 lepton final state  
in the SM

discovery channel for our  $Z'$



Interplay of  $Z'$  coupling to the singlet scalar with coupling strength  $g_x$  while the scalars are produced via gluon-gluon fusion helps probe the light gauge boson at LHC via Higgs sector

- Another interesting possibility when  $Z'$  decays radiatively due to  $Y_{\nu_{ij}}$
- The  $Y_{\nu_{ij}} \bar{\ell}_i H_2 N_j$  in the Lagrangian determines how large the radiative decay is.
- $Y_\nu \sim 10^{-2}$  gives loop induced decays comparable to tree-level width for  $g'_x \sim 10^{-5}$ ,  $\theta' \sim 10^{-5}$  mixing and  $g_x \sim g_{EW}$ .



effective vertex of  $Z' l_k \bar{l}_n$

$$\mathcal{M}_{Z' l_k \bar{l}_n} = i f_{kn} \gamma^\mu P_L$$

The partial decay width for

$$\Gamma(Z' \rightarrow l_i \bar{l}_j) = \frac{M_{Z'}}{24\pi} |f_{ij}|^2$$

| $Z'$ decay  | $\sum \nu_a \nu_b$ | $\sum \ell_a^+ \ell_a^-$ | $\sum \ell_a^\pm \ell_b^\mp$ | $\sum j j$    | $\Gamma_{Z'} \text{ (GeV)}$ |
|---|--------------------|--------------------------|------------------------------|---------------|-----------------------------|
| $Y_{\nu_{ij}}^{i \neq j} \sim 0, Y_\nu^{ii} \sim 10^{-3}$ | 0.23 ( $10^{-3}$ ) | 0.16 ( $10^{-4}$ )       | 0 ( $10^{-4}$ )              | 0.61 (0)      | $2 \times 10^{-9}$          |
| $Y_{\nu_{ij}}^{i \neq j} \sim 0.08, Y_\nu^{ii} \sim 0.2$  | $10^{-5}$ (0.8)    | $10^{-5}$ (0.135)        | 0 (0.065)                    | $10^{-5}$ (0) | $3 \times 10^{-4}$          |



# Summary

- With no clear hints of BSM physics at LHC we must explore the possibility of hidden symmetries in the data.
- $U(1)$  is one of the simplest and well motivated scenarios to consider.
- I showed through a few examples how a light  $Z'$  can show itself at experiments even when not connected to the SM sector directly but with gauge coupling strength similar to  $g_{EW}$ .
- Experimental signatures change as the modes of interactions change.
- Role of very long-lived  $Z'$  in this scenario, LFV, ILC expectations, DM, (g-2) at 2-loop, etc. are things being looked at currently.
- A closer look for such symmetries in accumulated data could show the need for new search strategies at LHC and future colliders.