

Models for non-standard neutrino interactions

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Effects of NSI on neutrinos

Neutral current Non-Standard Interaction (**NSI**): propagation of neutrinos in matter

$$\mathcal{L}_{\text{NC-NSI}} = -2\sqrt{2}G_F \epsilon_{\alpha\beta}^{fX} (\bar{\nu}_\alpha \gamma^\mu P_L \nu_\beta) (\bar{f} \gamma_\mu P_X f)$$

Charged current Non-Standard Interaction (**NSI**): production and detection

$$\mathcal{L}_{\text{CC-NSI}} = -2\sqrt{2}G_F \epsilon_{\alpha\beta}^{ff'X} (\bar{\nu}_\alpha \gamma^\mu P_L \ell_\beta) (\bar{f}' \gamma_\mu P_X f)$$

Effects of NSI on neutrinos

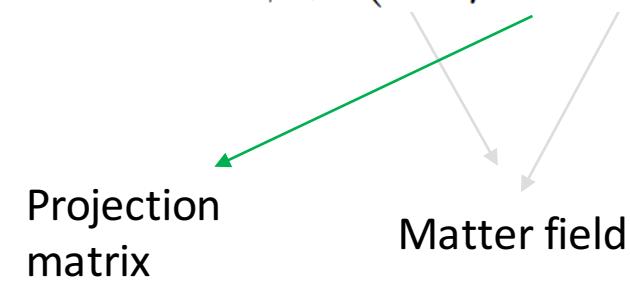
Neutral current Non-Standard Interaction (**NSI**): propagation of neutrinos in matter

$$\mathcal{L}_{\text{NC-NSI}} = -2\sqrt{2}G_F \epsilon_{\alpha\beta}^{fX} (\bar{\nu}_\alpha \gamma^\mu P_L \nu_\beta) (\bar{f} \gamma_\mu P_X f)$$

Focus of this talk

Non-standard **neutral current** interaction

$$\mathcal{L}_{\text{NC-NSI}} = -2\sqrt{2}G_F \epsilon_{\alpha\beta}^{fX} (\bar{\nu}_\alpha \gamma^\mu P_L \nu_\beta) (\bar{f} \gamma_\mu P_X f)$$



Neutrino propagation:

$$\epsilon_{\alpha\beta}^f \equiv \epsilon_{\alpha\beta}^{fL} + \epsilon_{\alpha\beta}^{fR}.$$

Hamiltonian of neutrinos

$$i \frac{d}{dx} \begin{pmatrix} \nu_e \\ \nu_\mu \\ \nu_\tau \end{pmatrix} = H^\nu \begin{pmatrix} \nu_e \\ \nu_\mu \\ \nu_\tau \end{pmatrix}$$
$$H^\nu = H_{\text{vac}} + H_{\text{mat}} \quad \text{and} \quad H^{\bar{\nu}} = (H_{\text{vac}} - H_{\text{mat}})^*$$

$$U = \begin{bmatrix} 1 & 0 & 0 \\ 0 & \cos \theta_{23} & \sin \theta_{23} \\ 0 & -\sin \theta_{23} & \cos \theta_{23} \end{bmatrix} \begin{bmatrix} \cos \theta_{13} & 0 & \sin \theta_{13} e^{i\delta} \\ 0 & 1 & 0 \\ -\sin \theta_{13} e^{-i\delta} & 0 & \cos \theta_{13} \end{bmatrix} \begin{bmatrix} \cos \theta_{12} & 0 \\ -\sin \theta_{12} & \cos \theta_{12} \\ 0 & 0 \end{bmatrix}$$

$$H_{\text{vac}} = U \cdot \text{Diag}(m_1^2/2E_\nu, m_2^2/2E_\nu, m_3^2/2E_\nu) \cdot U^\dagger$$

Matter effects in presence of NSI

$$i \frac{d}{dx} \begin{pmatrix} \nu_e \\ \nu_\mu \\ \nu_\tau \end{pmatrix} = H^\nu \begin{pmatrix} \nu_e \\ \nu_\mu \\ \nu_\tau \end{pmatrix} \quad H^\nu = H_{\text{vac}} + H_{\text{mat}} \quad \text{and} \quad H^{\bar{\nu}} = (H_{\text{vac}} - H_{\text{mat}})^*$$

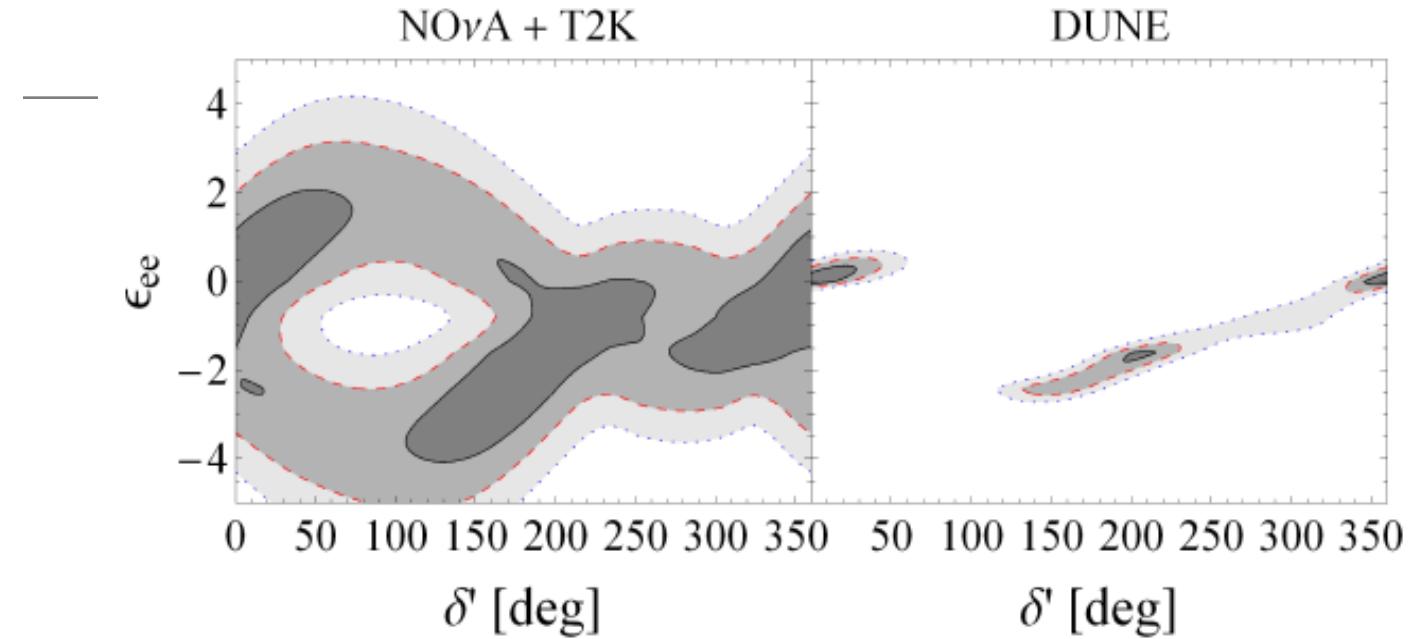
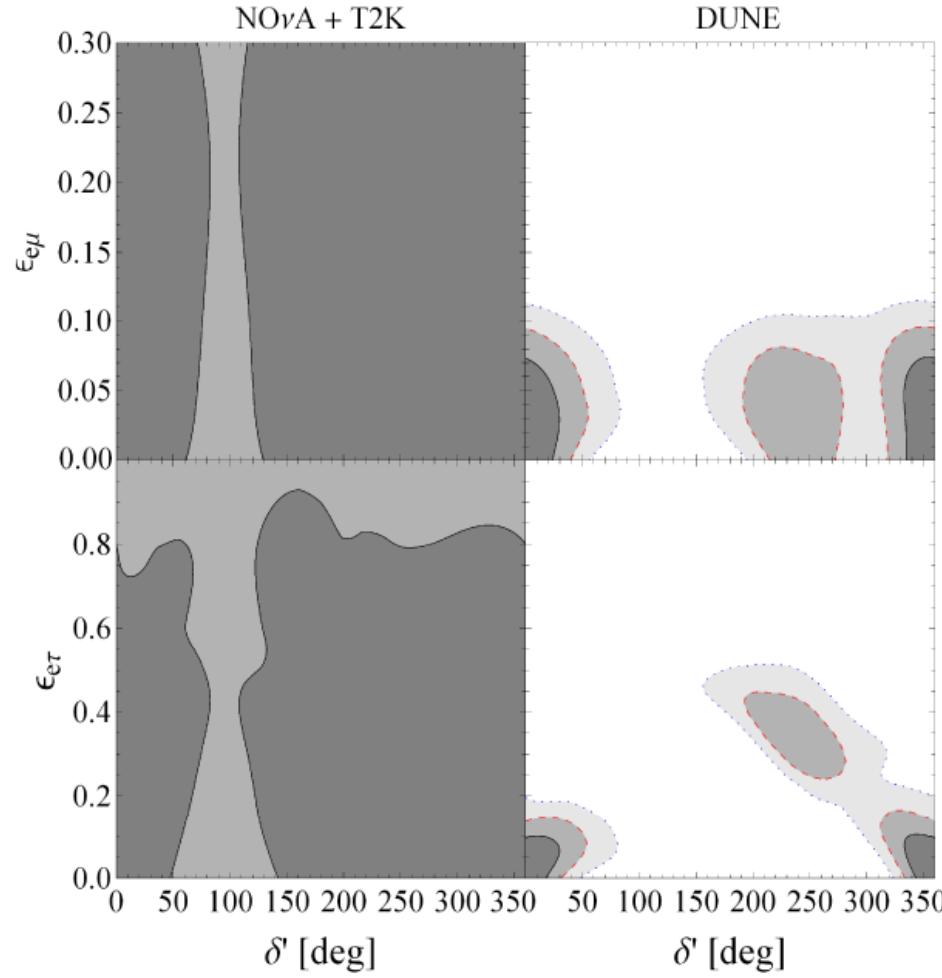
$$H_{\text{mat}} = \sqrt{2} G_F N_e(r) \begin{pmatrix} 1 & 0 & 0 \\ 0 & 0 & 0 \\ 0 & 0 & 0 \end{pmatrix} + \sqrt{2} G_F \sum_{f=e,u,d} N_f(r) \begin{pmatrix} \varepsilon_{ee}^f & \varepsilon_{e\mu}^f & \varepsilon_{e\tau}^f \\ \varepsilon_{e\mu}^{f*} & \varepsilon_{\mu\mu}^f & \varepsilon_{\mu\tau}^f \\ \varepsilon_{e\tau}^{f*} & \varepsilon_{\mu\tau}^{f*} & \varepsilon_{\tau\tau}^f \end{pmatrix}$$

Effects of NSI in long baseline experiments

Renewed interest in NSI

NSI can **fake CP-violation** and lead to **wrong** determination of θ_{23} **octant** and **mass ordering**

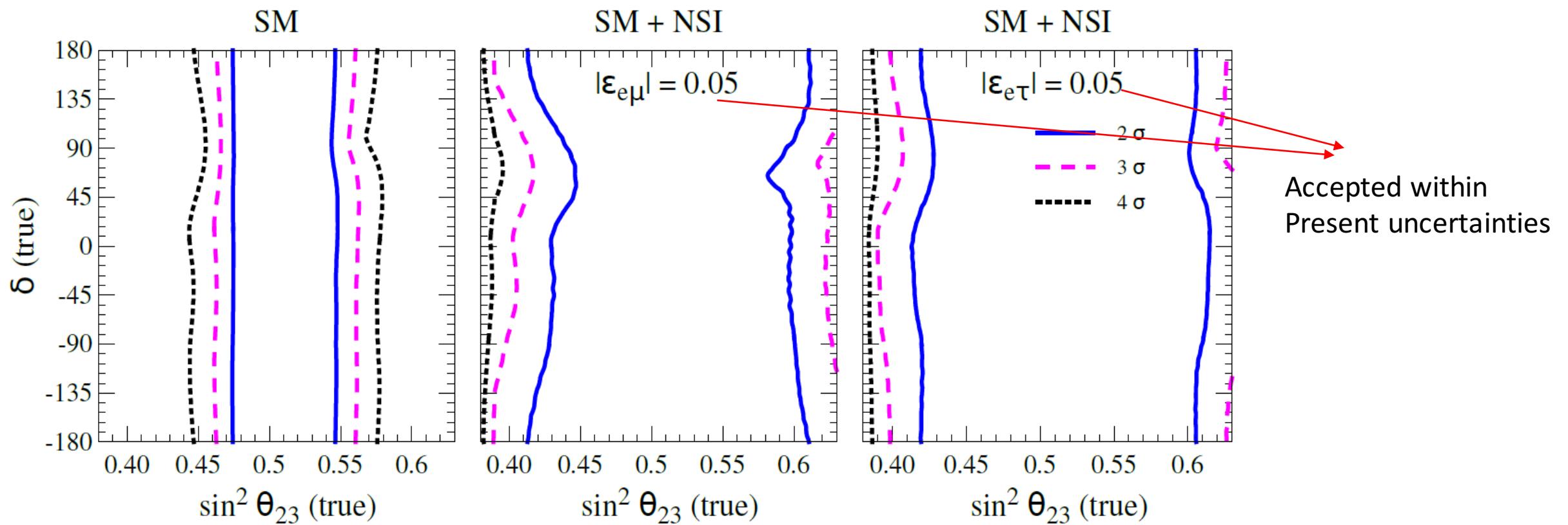
Masud and Mehta, PRD 94(2016); Forero and Huber, PLB 117 (2016); Liao, Marfatia and Whistnant PRD 93 (2016); JHEP 1701 (2017) 071; Agarwalla, Chatterjee and Palazzo, PLB 762 (2016); Verma and Bhardwaj, 1808.04263; Flore, Garces, Miranda, Phys Rev D98 (2018)35030; Wang and Zhou, 1801.05656; Deepath, Goswami and Nath, 1711.04840; 1612.00784; Fukasawa, Ghosh, Yasuda, PRD 95 (2017); Forero and Huang, JHEP 1703 (2017); Ge and Smirnov, JHEP 1610; A. de Gouvea and K Kelly, 1605.09376; Coloma, Schwetz, PRD 94 (2016)



Liao Marfatia Whisnant, PRD93 (2016)

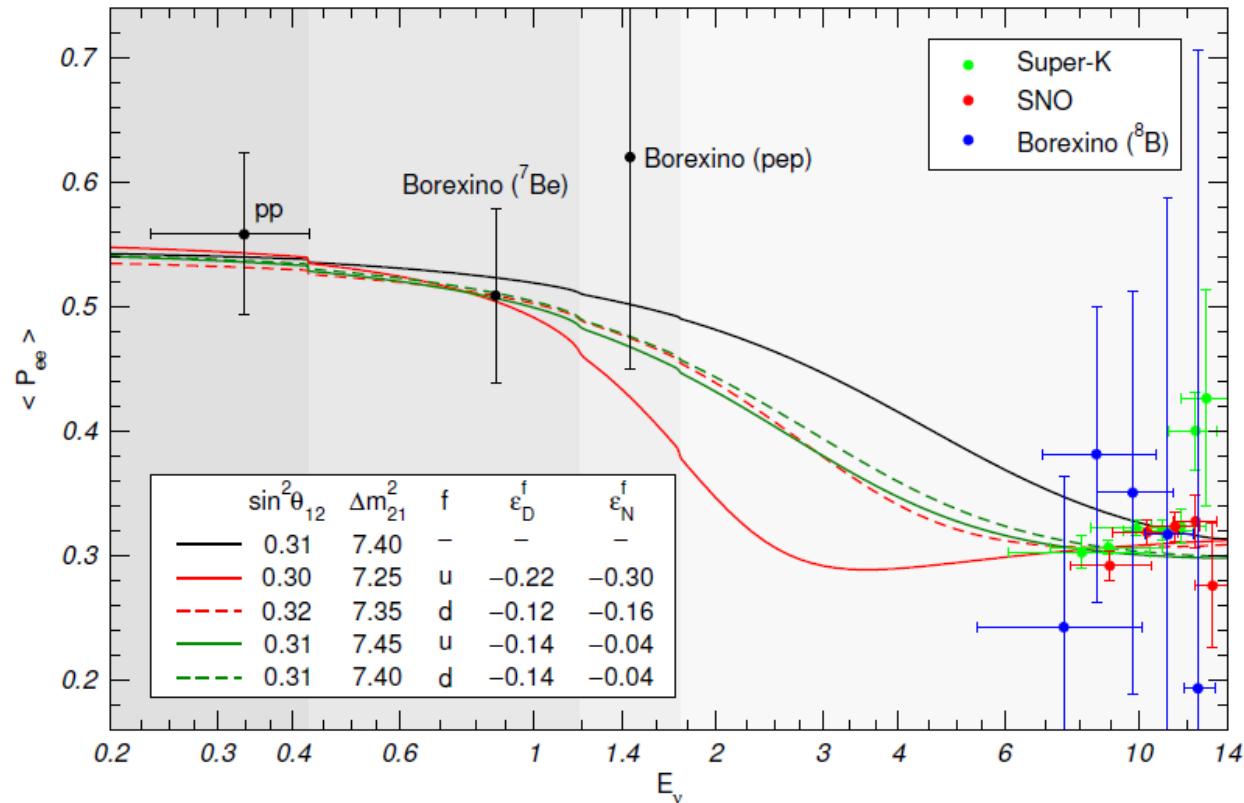
SM with $\delta = 0$

Octant discovery potential of DUNE



Agarwalla, Chatterjee and Palazzo, PLB 762 (2016)

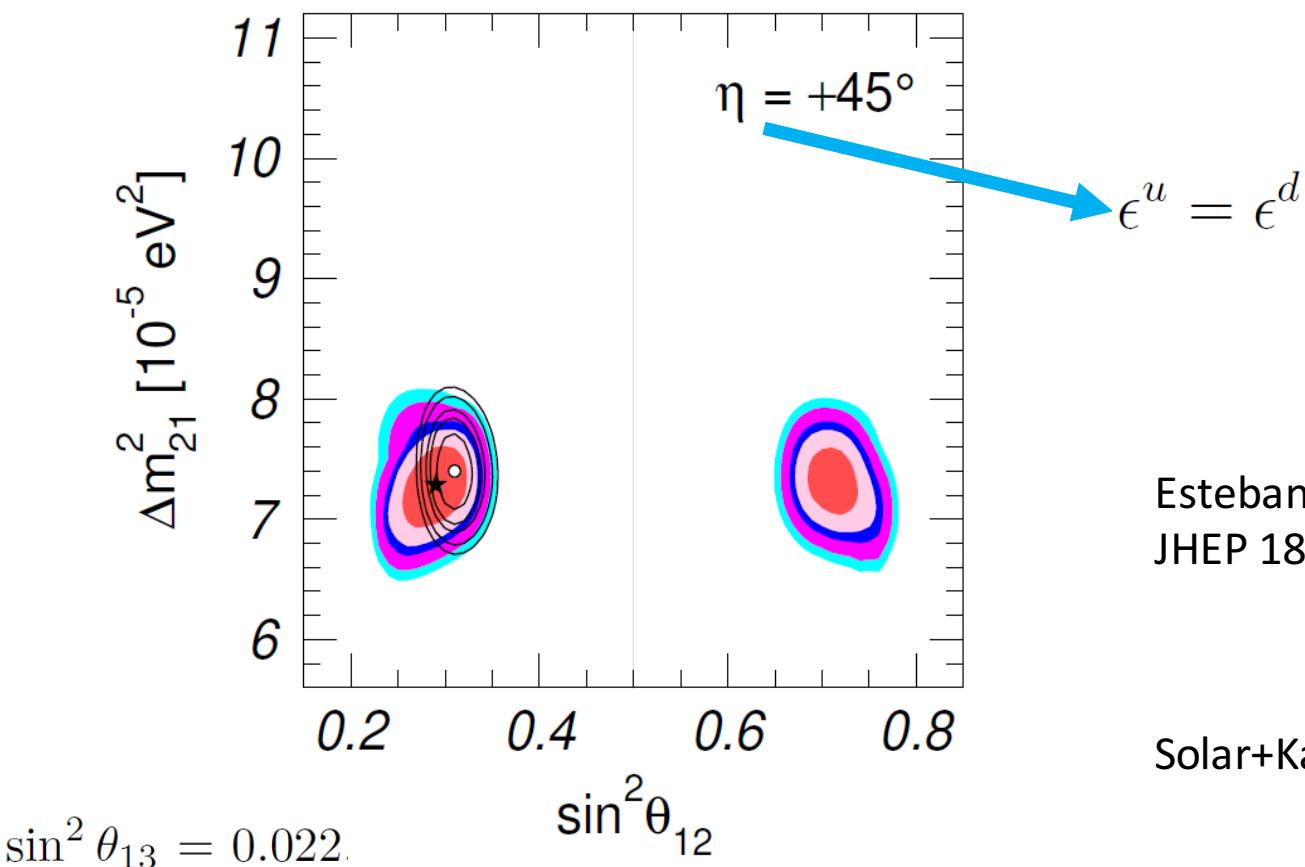
Solving solar and KamLAND tension



Maltoni and Gonzalez-Garcia, JHEP 2013

Fit to solar and KamLAND data

Miranda, Tortola and Valle, JHEP 2006; Escrihuela et al., PRD 2009



Esteban, Gonzalez-Garcia, M. Maltoni, Martinez-Soler and J Salvado,
JHEP 1808 (2018) 180, arXiv:1805.04530

Solar+KamLAND

LMA-Dark solution

LMA-Dark solution provides even a better fit. (suppression of low energy upturn)

$$\varepsilon_{ee}^u - \varepsilon_{\mu\mu}^u \quad [-1.192, -0.802]$$

$$\theta_{12} > \pi/4$$

Scattering experiments

$$\mathcal{L}_{NSI} = -2\sqrt{2}G_F \epsilon_{\alpha\beta}^{fP} (\bar{\nu}_\alpha \gamma^\mu L \nu_\beta) (\bar{f} \gamma_\mu P_f)$$

NuTeV and CHARM rule out a large part (but not all) of parameter space of LMA-Dark solution.

Davidson, Pena-Garay, Rius, SantaMaria, JHEP 2003

COHERENT experiment (a CEvNS setup) also rules out LMA-Dark solution.

P. Coloma, M.C. Gonzalez-Garcia, M. Maltoni and T. Schwetz, PRD 94 (2017) 115007;

P. Coloma, P. Denton, M.C. Gonzalez-Garcia, M. Maltoni and T. Schwetz, JHEP1704 (2017) 116

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P. Coloma, P. Denton, M.C. Gonzalez-Garcia, M. Maltoni and T. Schwetz, JHEP1704 (2017) 116

But not in the model that we shall present

Underlying theory for NSI

$$\mathcal{L}_{\text{NC-NSI}} = -2\sqrt{2}G_F \epsilon_{\alpha\beta}^{fX} (\bar{\nu}_\alpha \gamma^\mu P_L \nu_\beta) (\bar{f} \gamma_\mu P_X f)$$

Integrating out a heavy intermediate state

Neutral U(1) gauge boson as mediator

$$Z'_\mu \bar{\nu}_\alpha \gamma^\mu P_L \nu_\beta$$

$$Z'_\mu \bar{f} \gamma^\mu P_X f$$

Charged scalar (a la Fierz transformation)

$$\overline{\psi_1} P_L \psi_2 \overline{\psi_3} P_R \psi_4 = \overline{\psi_{1R}} \psi_{2L} \overline{\psi_{3L}} \psi_{4R} = -\frac{1}{2} \overline{\psi_1} \gamma^\mu P_R \psi_4 \overline{\psi_3} \gamma_\mu P_L \psi_2$$

Forero and Huang, JHEP 1703 (2017); Bischer, Rodejohann and Xu, JHEP 1810 (2018) 096, arXiv:1807.08102

Underlying theory for NSI

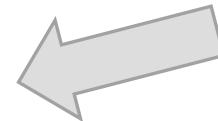
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Integrating out a heavy intermediate state

Neutral U(1) gauge boson as mediator

$$Z'_\mu \bar{\nu}_\alpha \gamma^\mu P_L \nu_\beta$$

Our Focus



$$Z'_\mu \bar{f} \gamma^\mu P_X f$$

Charged scalar (a la Fierz transformation)

$$\overline{\psi_1} P_L \psi_2 \overline{\psi_3} P_R \psi_4 = \overline{\psi_{1R}} \psi_{2L} \overline{\psi_{3L}} \psi_{4R} = -\frac{1}{2} \overline{\psi_1} \gamma^\mu P_R \psi_4 \overline{\psi_3} \gamma_\mu P_L \psi_2$$

Forero and Huang, JHEP 1703 (2017); Bischer,
Rodejohann and Xu, JHEP 1810 (2018) 096,
arXiv:1807.08102

Too small NSI

$$\mathcal{L}_{\text{NC-NSI}} = -2\sqrt{2}G_F \epsilon_{\alpha\beta}^{fX} (\bar{\nu}_\alpha \gamma^\mu P_L \nu_\beta) (\bar{f} \gamma_\mu P_X f)$$

$$\epsilon_{\alpha\beta}^f \equiv \epsilon_{\alpha\beta}^{fL} + \epsilon_{\alpha\beta}^{fR}.$$

$$\epsilon \sim \left(\frac{g_{Z'}}{m_{Z'}} \right)^2 G_F^{-1}$$

$m_{Z'} \gg 100 \text{ GeV}$



$\epsilon \ll 1$

Suggestion

What if $m_{Z'} \sim 10$ MeV

YF, “A model for large non-standard interactions leading to LMA-Dark solution,”
Phys. Lett. B748 (2015) 311-315; YF and J Heeck, “Neutrinophilic nonstandard interactions,”
PRD 94 (2016) 53010; YF and I Shoemaker, “lepton flavor violating NSI via light mediator,”
JHEP 1607 (2016) 33;
YF and M Tortola, “neutrino oscillations and non-standard interactions,” Frontiers in
Physics 6 (2018) 10; Y. Farzan, “A model for lepton flavor violating non-standard neutrino interactions,” PLB (2020)
135349; P. Denton, Y.F. and I Shoemaker,
“Activating the fourth neutrino of the 3+1 scheme,” PRD 99 (2019) 035003

Suggestion

What if $m_{Z'} \sim 10 \text{ MeV}$

$$\epsilon \sim 1$$



$$g_{Z'} \sim 10^{-4} - 10^{-5}$$

Bounds can be avoided **not** because the mass of the intermediate state is **high**

But because coupling is **small!**

Neutral current Non-Standard Interactions

NSI

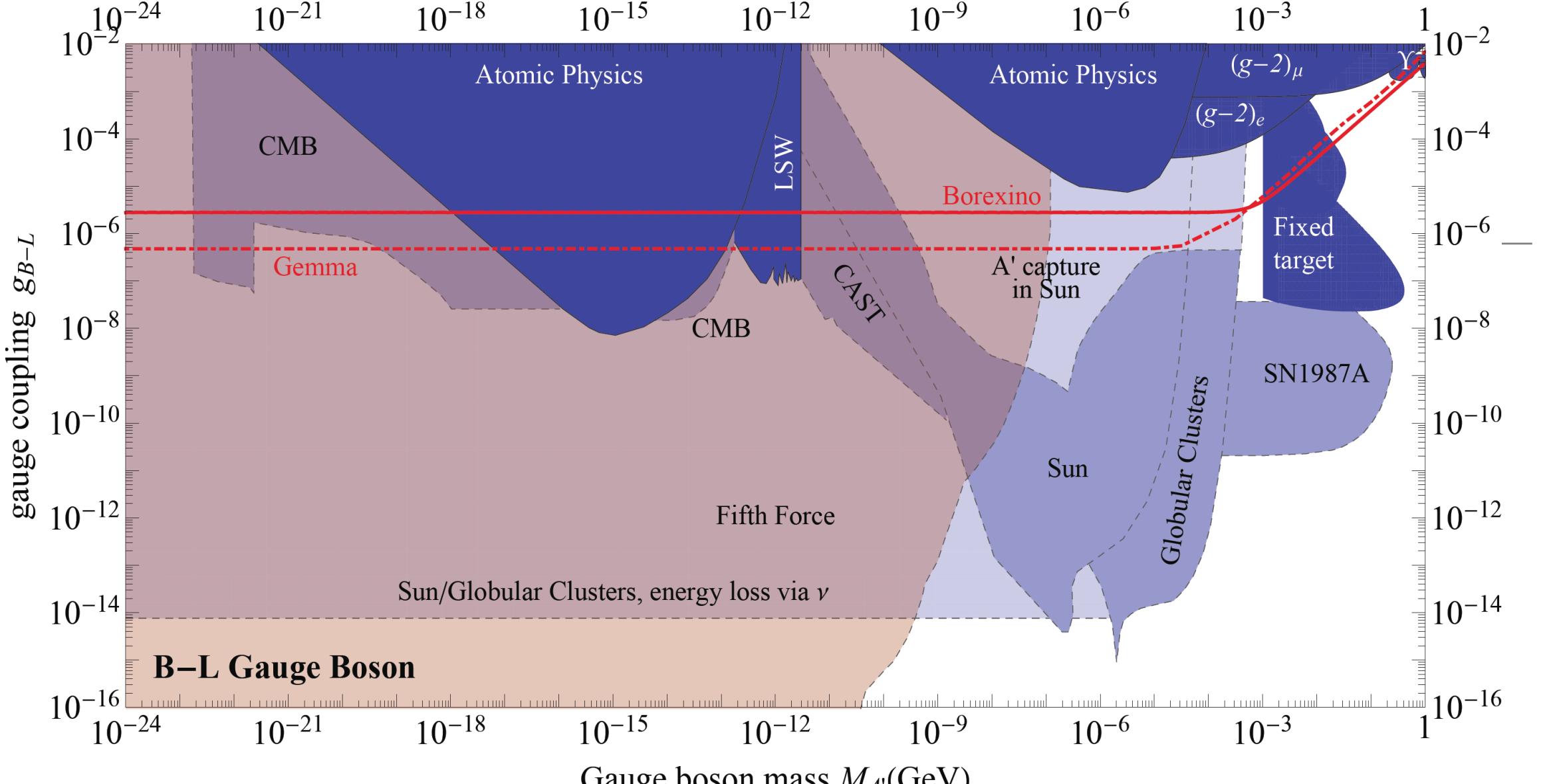
$$\mathcal{L}_{\text{NSI}} = -2\sqrt{2}G_F \varepsilon_{\alpha\beta}^{fX} (\bar{\nu}_\alpha \gamma^\mu P_L \nu_\beta)(\bar{f} \gamma_\mu P_X f)$$

Y.F. and J. Heeck, PRD94 (2016); Y.F. and Shoemaker, JHEP 1607 (2016); YF, PLB 748 (2015)

$$(g_\nu)_{\alpha\beta} \bar{\nu}_\alpha \gamma^\mu \nu_\beta Z'_\mu \quad g_B \bar{q} \gamma^\mu q Z'_\mu$$

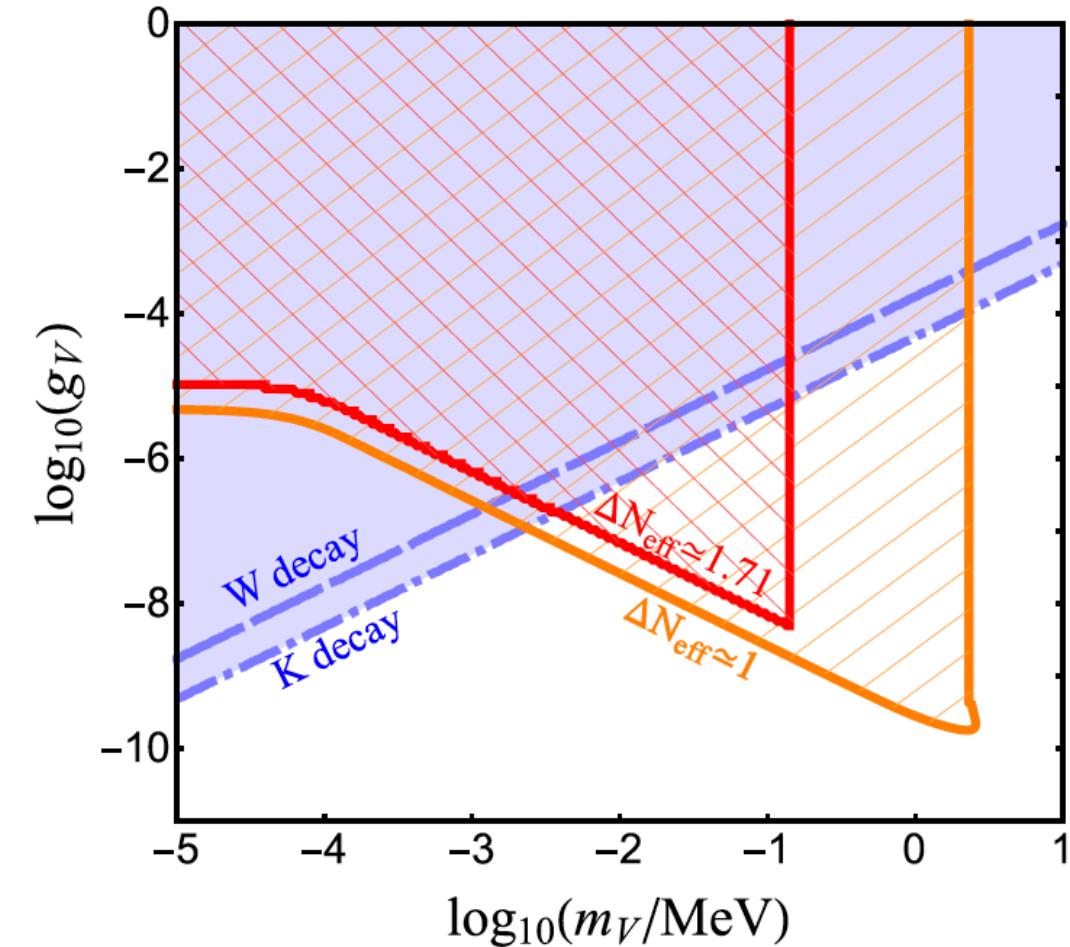
$$\epsilon_{\alpha\beta}^u = \epsilon_{\alpha\beta}^d = \frac{g_B (g_\nu)_{\alpha\beta}}{\sqrt{2} G_F M_{Z'}^2}$$

$$\sqrt{g_\nu g_B} \sim 7 \times 10^{-5} \frac{m_{Z'}}{10 \text{ MeV}} \quad \leftrightarrow \quad \epsilon_{\alpha\beta}^u = \epsilon_{\alpha\beta}^d \sim 1$$

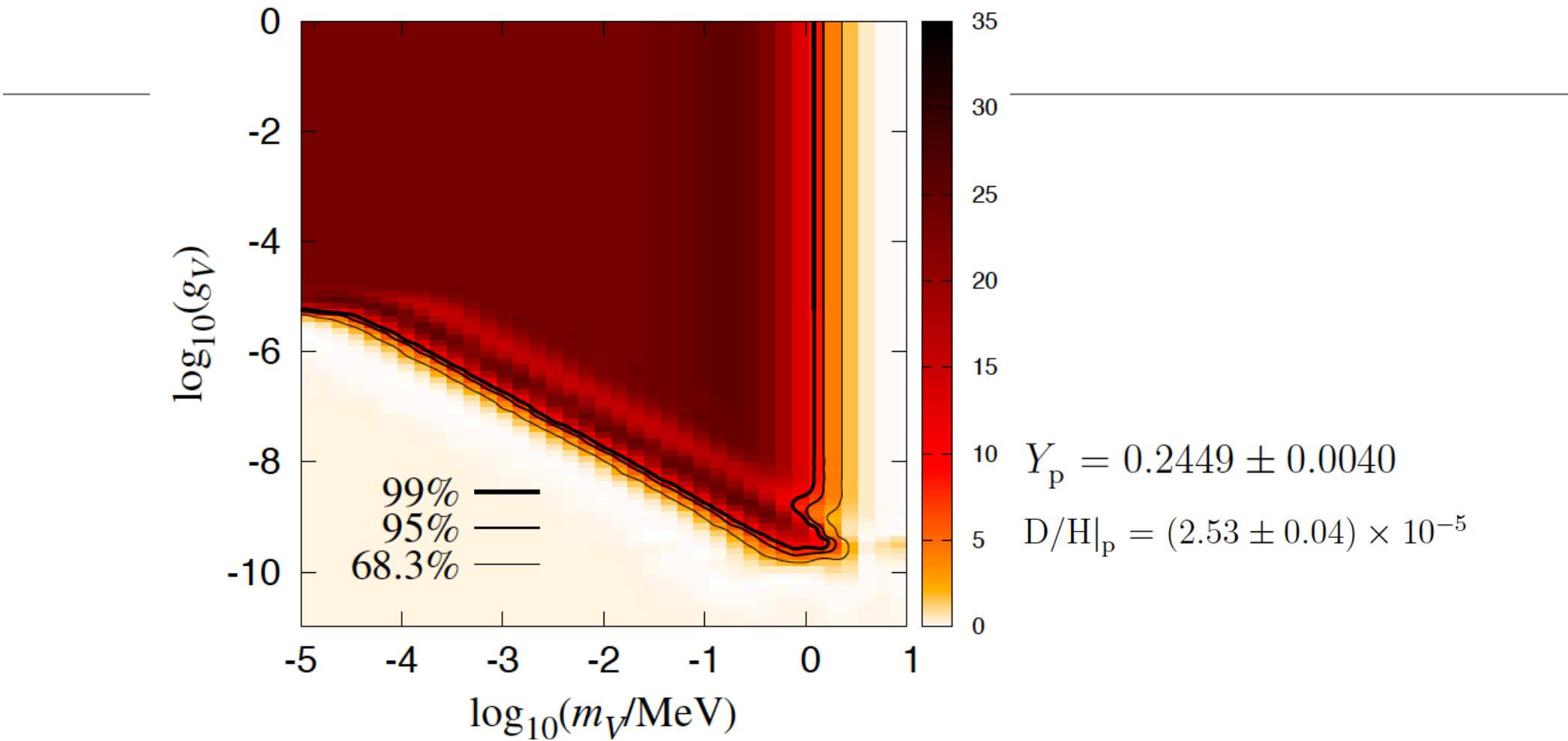


Harnik, Kopp and Machado, JCAP 1207 (2012) 026

Effect in early universe



Huang, Ohlsson, Zhou,
PRD 97 (2018) 075009

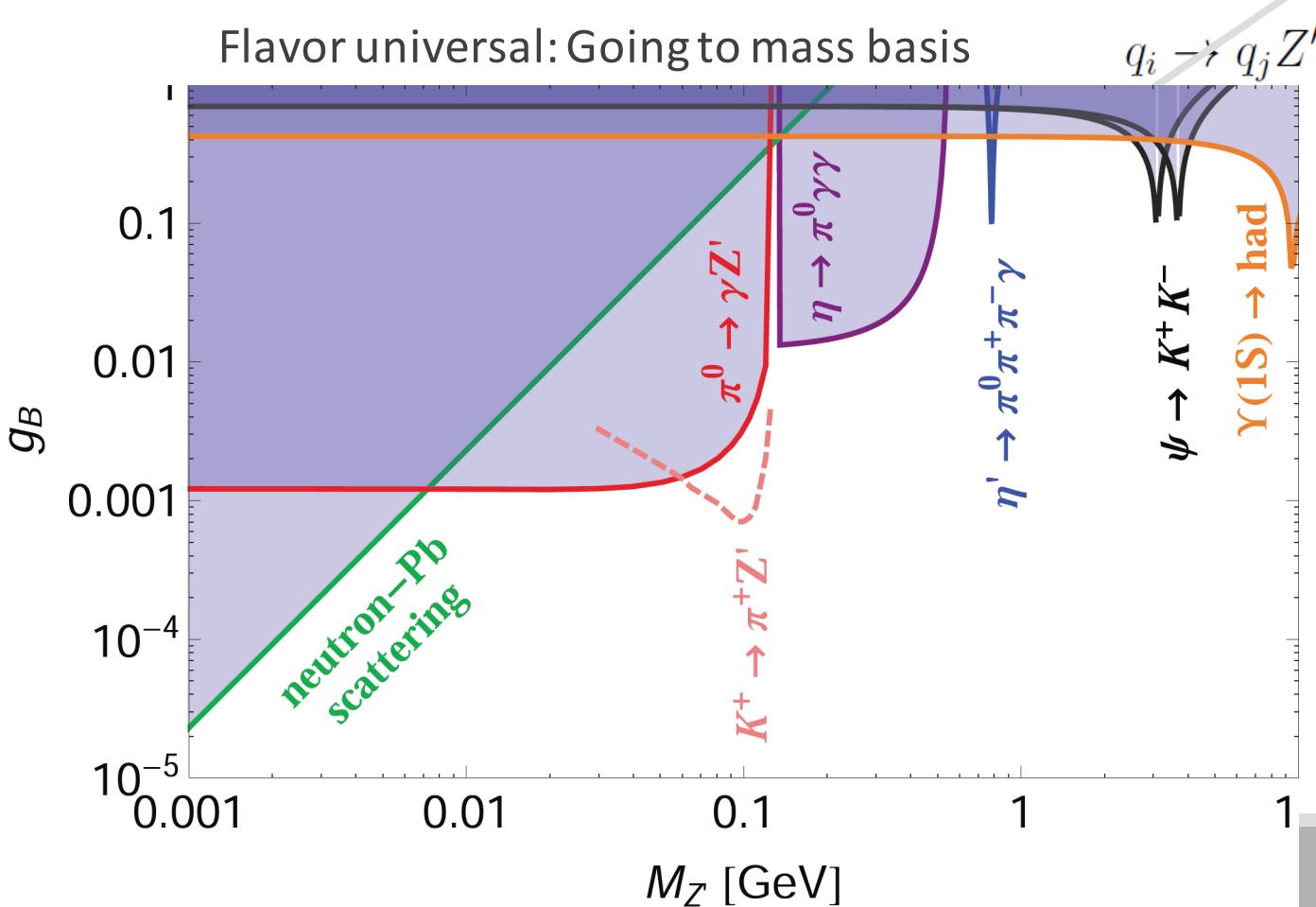


Huang, Ohlsson, Zhou, PRD 97 (2018) 075009

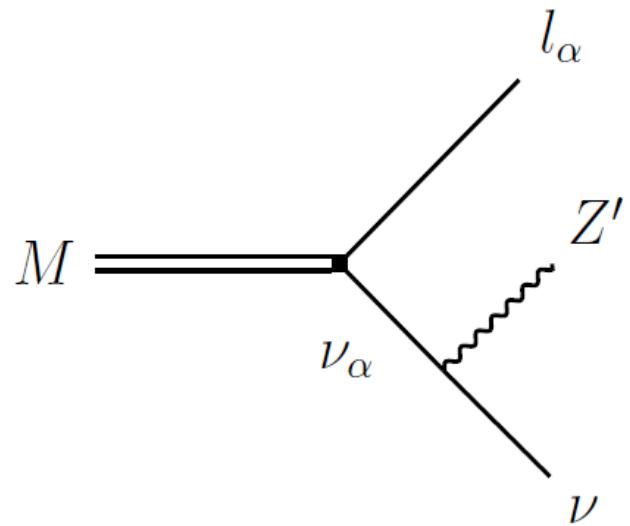
Coupling to quarks

Non-chiral couplings: No impact on total measurement at SNO

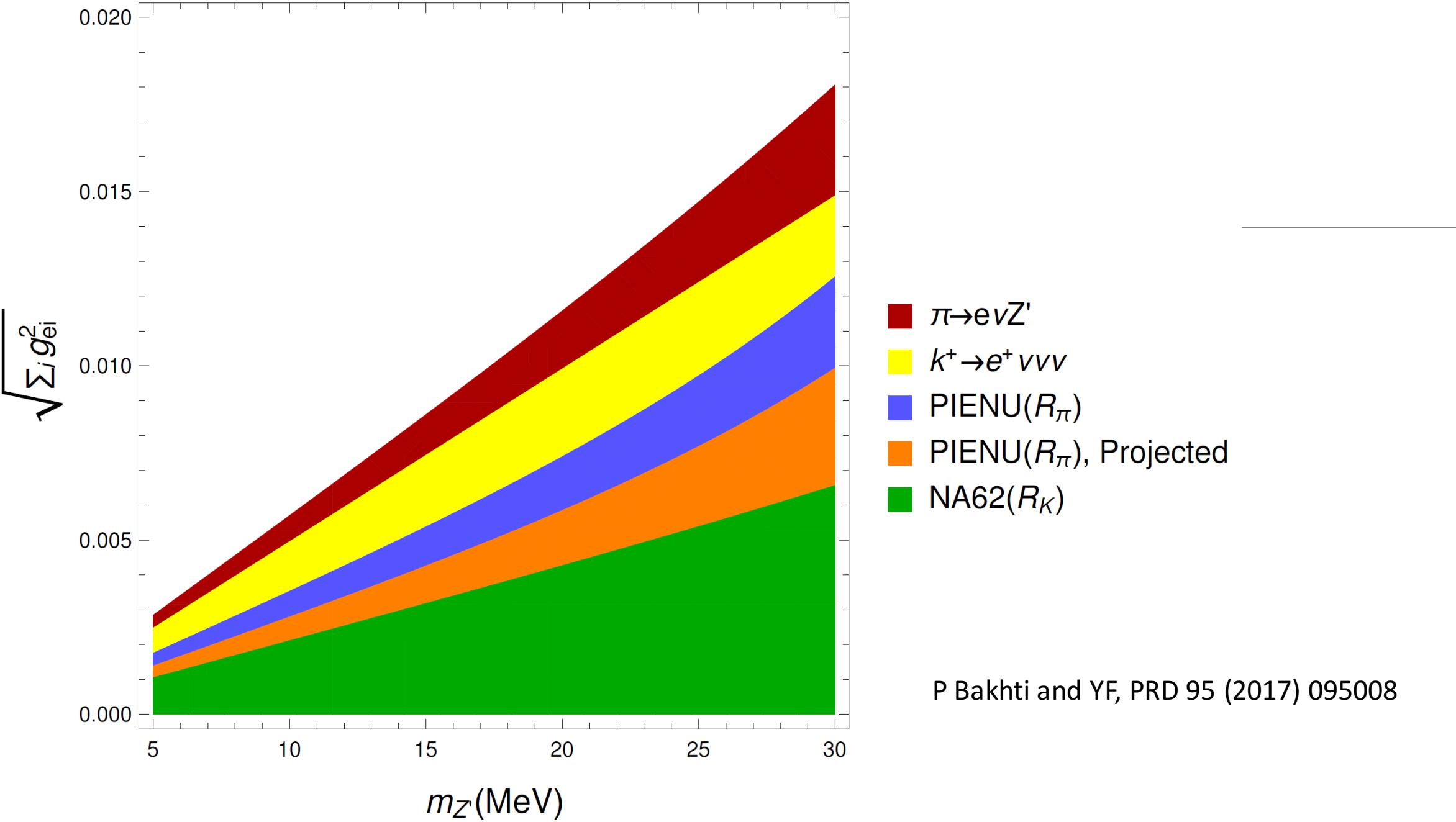
Flavor universal: Going to mass basis

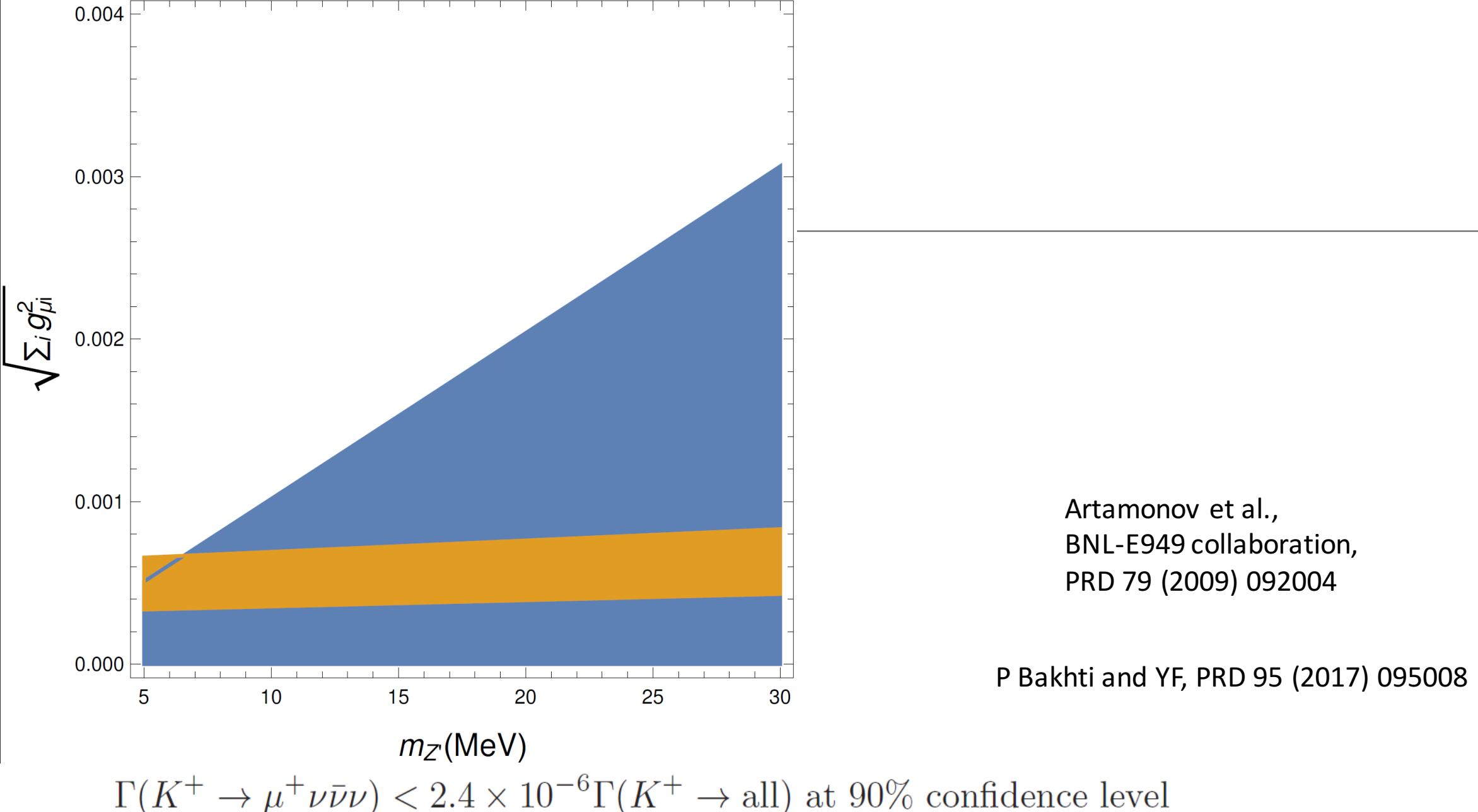


Bounds on Couplings of neutrinos



$$R_M \equiv \frac{Br(M^+ \rightarrow e^+ + \text{missing energy})}{Br(M^+ \rightarrow \mu^+ + \text{missing energy})} \quad M^+ = \pi^+, K^+$$





Neutrino scattering experiments

$$q^2 \gg m_{Z'}^2$$

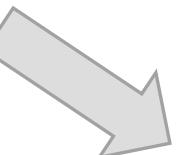
$$\mathcal{L}_{NSI} = -2\sqrt{2}G_F c_{\alpha\beta}^{fP} (\bar{\nu}_\alpha \gamma^\mu L \nu_\beta) (\bar{f} \gamma_\mu P f)$$

Suppression factor

$$m_{Z'}^2 / (q^2 - m_{Z'}^2)$$

Neutrino scattering experiments

$$q^2 \gg m_{Z'}^2$$


$$\mathcal{L}_{NSI} = -2\sqrt{2}G_F \epsilon_{\alpha\beta}^{fP} (\bar{\nu}_\alpha \gamma^\mu L \nu_\beta) (\bar{f} \gamma_\mu P f)$$

$$10 \text{ MeV} \lesssim m_{Z'} \ll 1 \text{ GeV}$$

Relaxing bounds from scattering experiments, **NuTeV** and **CHARM**

New U(1) gauge symmetry

Direct coupling to neutrinos

Gauge symmetry:

$$a_e L_e + a_\mu L_\mu + a_\tau L_\tau + B$$

Coupling to neutrinos through mixing with ψ : κ_α

Gauge symmetry:

$$a_\psi L_\psi + B$$

New U(1) gauge symmetry

Direct coupling to neutrinos

Gauge symmetry:

$$a_e L_e + a_\mu L_\mu + a_\tau L_\tau + B$$



Charged leptons couple to Z'

Coupling to neutrinos through mixing with ψ : κ_α

Gauge symmetry:

$$a_\psi L_\psi + B$$



Charged leptons do not couple

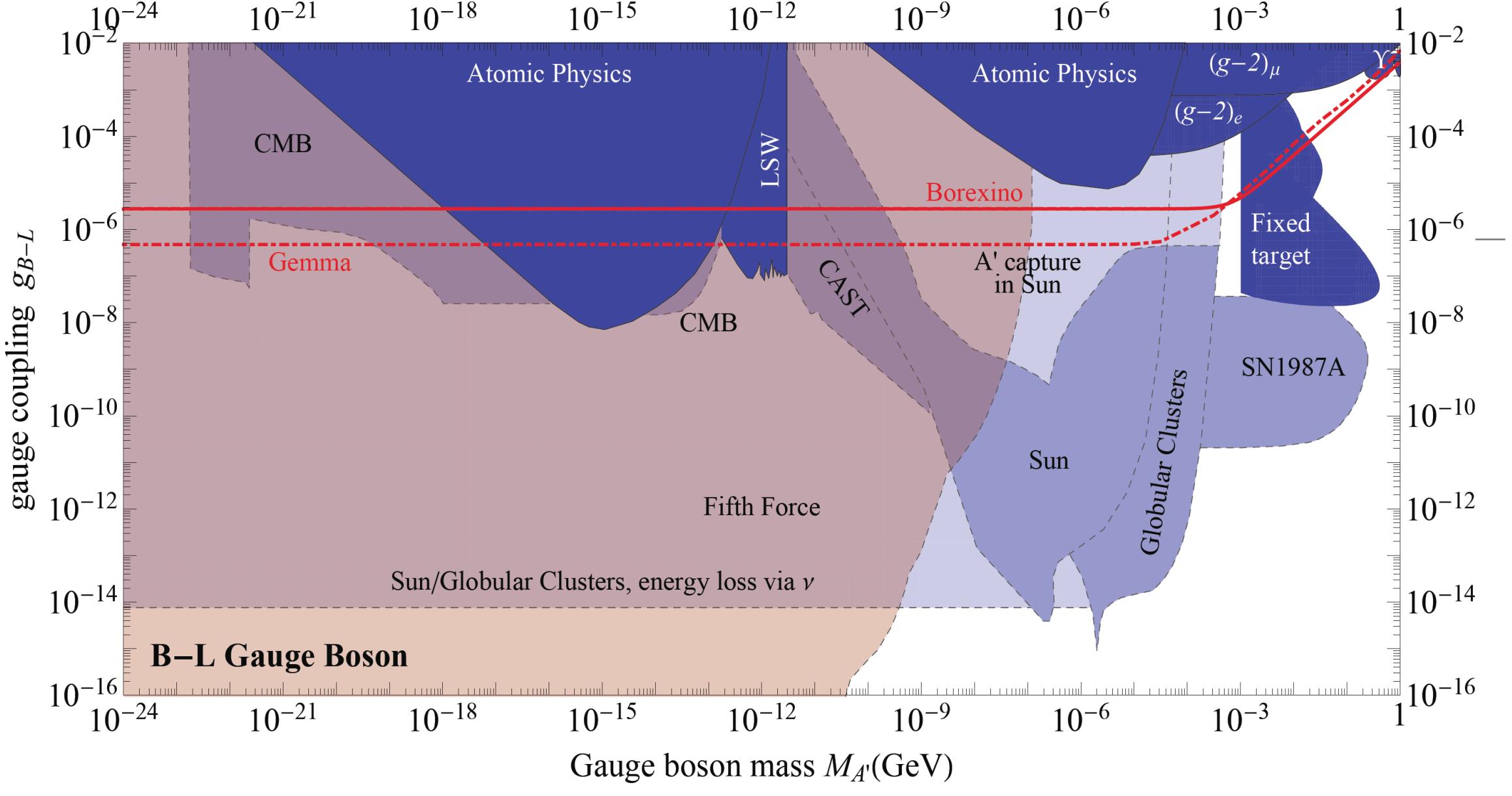
Coupling to neutrinos

Direct coupling to neutrinos

Gauge symmetry:

$$a_e L_e + a_\mu L_\mu + a_\tau L_\tau + B$$

$$\epsilon_{\alpha\alpha}^u = \epsilon_{\alpha\alpha}^d = \frac{g'^2 a_\alpha}{6\sqrt{2}G_F m_{Z'}^2} \quad \text{and} \quad \epsilon_{\alpha\alpha}^u = 0|_{\alpha \neq \beta}.$$



$$g'a_e < 3 \times 10^{-11}$$

Harnik, Kopp and Machado, JCAP 1207 (2012) 026

$$a_e L_e + a_\mu L_\mu + a_\tau L_\tau + B$$

$$a_e = 0$$

Anomaly cancelation:

$$a_\mu = a_\tau = -3/2$$

Reproducing best fit

$$g' = 4 \times 10^{-5} \frac{m_{Z'}}{10 \text{ MeV}} \left(\frac{\epsilon_{ee} - \epsilon_{\mu\mu}}{0.3} \right)^{1/2}$$

$$\epsilon_{ee} - \epsilon_{\mu\mu} = 0.3$$

Best fit reconciling KamLAND and solar neutrino data

Miranda, Tortola, Valle, JHEP 10 (2006) 8

LFV NSI for neutrinos but not for charged leptons

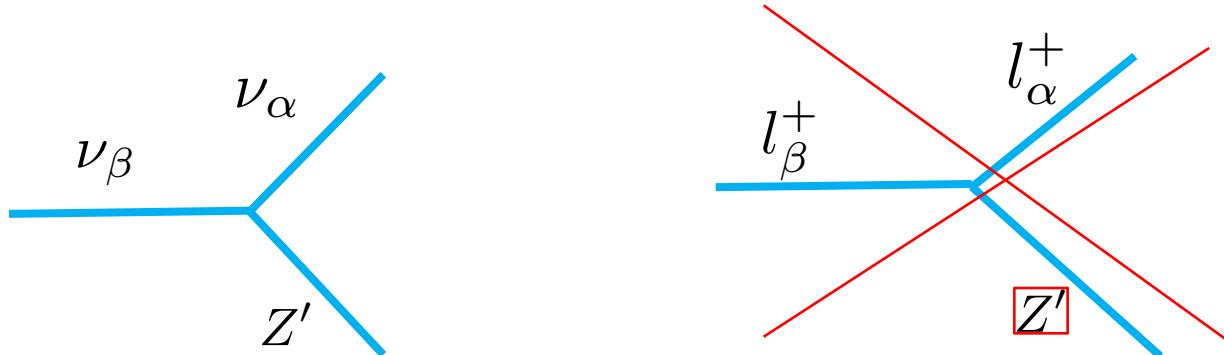
$$a_\psi L_\psi + B$$

Mixing with ψ :

$$\begin{array}{l} \nu_\alpha + \kappa_\alpha \psi \\ -\kappa_\alpha \nu_\alpha + \psi \end{array}$$

$$\begin{array}{l} \nu_\beta + \kappa_\beta \psi \\ -\kappa_\beta \nu_\beta + \psi \end{array}$$

$$g' a_\Psi Z'_\mu \left(\sum_{\alpha, \beta} \kappa_\alpha^* \kappa_\beta \bar{\nu}_\alpha \gamma^\mu P_L \nu_\beta - \kappa_\alpha^* \bar{\nu}_\alpha \gamma^\mu P_L \Psi - \kappa_\alpha \bar{\Psi} \gamma^\mu P_L \nu_\alpha \right)$$



Coupling of neutrinos through mixing

$$g' a_\Psi Z'_\mu \left(\sum_{\alpha, \beta} \kappa_\alpha^* \kappa_\beta \bar{\nu}_\alpha \gamma^\mu P_L \nu_\beta - \kappa_\alpha^* \bar{\nu}_\alpha \gamma^\mu P_L \Psi - \kappa_\alpha \bar{\Psi} \gamma^\mu P_L \nu_\alpha \right)$$

$$\epsilon_{\alpha\beta}^u = \epsilon_{\alpha\beta}^d = \frac{g'^2 a_\Psi \kappa_\alpha^* \kappa_\beta}{6\sqrt{2} G_F m_{Z'}^2}$$

$$\epsilon_{\alpha\alpha}^{u(d)} \epsilon_{\beta\beta}^{u(d)} = |\epsilon_{\alpha\beta}^{u(d)}|^2$$

$$|\kappa_e|^2 < 2.5 \times 10^{-3} \quad |\kappa_\mu|^2 < 4.4 \times 10^{-4} \quad |\kappa_\tau|^2 < 5.6 \times 10^{-3} \quad \text{at } 2\sigma$$

Fernandez-Martinez et al., JHEP 08 (2016) 033

Coupling of neutrinos through mixing

$$g' a_\Psi Z'_\mu \left(\sum_{\alpha, \beta} \kappa_\alpha^* \kappa_\beta \bar{\nu}_\alpha \gamma^\mu P_L \nu_\beta - \kappa_\alpha^* \bar{\nu}_\alpha \gamma^\mu P_L \Psi - \kappa_\alpha \bar{\Psi} \gamma^\mu P_L \nu_\alpha \right)$$

$$\epsilon_{\alpha\beta}^u = \epsilon_{\alpha\beta}^d = \frac{g'^2 a_\Psi \kappa_\alpha^* \kappa_\beta}{6\sqrt{2} G_F m_{Z'}^2}$$

$$\epsilon_{\alpha\alpha}^{u(d)} \epsilon_{\beta\beta}^{u(d)} = |\epsilon_{\alpha\beta}^{u(d)}|^2$$

$$\epsilon_{\alpha\beta}^u = \epsilon_{\alpha\beta}^d = 1 \left(\frac{g'}{10^{-5}} \right) \left(\frac{g' a_\Psi}{1} \right) \frac{\kappa_\alpha^* \kappa_\beta}{10^{-3}} \left(\frac{10 \text{ MeV}}{m_{Z'}} \right)^2$$

Flavor structure of NSI

$$\begin{array}{ccc} a_\psi L_\psi + B & \xrightarrow{\kappa_\alpha, \kappa_\beta} & \epsilon_{\alpha\beta}^f \epsilon_{\beta\alpha}^f = \epsilon_{\alpha\alpha}^f \epsilon_{\beta\beta}^f. \\ \text{More than one } \psi & \xrightarrow{} & |\epsilon_{\alpha\beta}^f|^2 < |\epsilon_{\alpha\alpha}^f \epsilon_{\beta\beta}^f| \end{array}$$

Y.F. and J. Heeck, “[Neutrinophilic Nonstandard interactions](#),” PRD 94 (2016) 053010

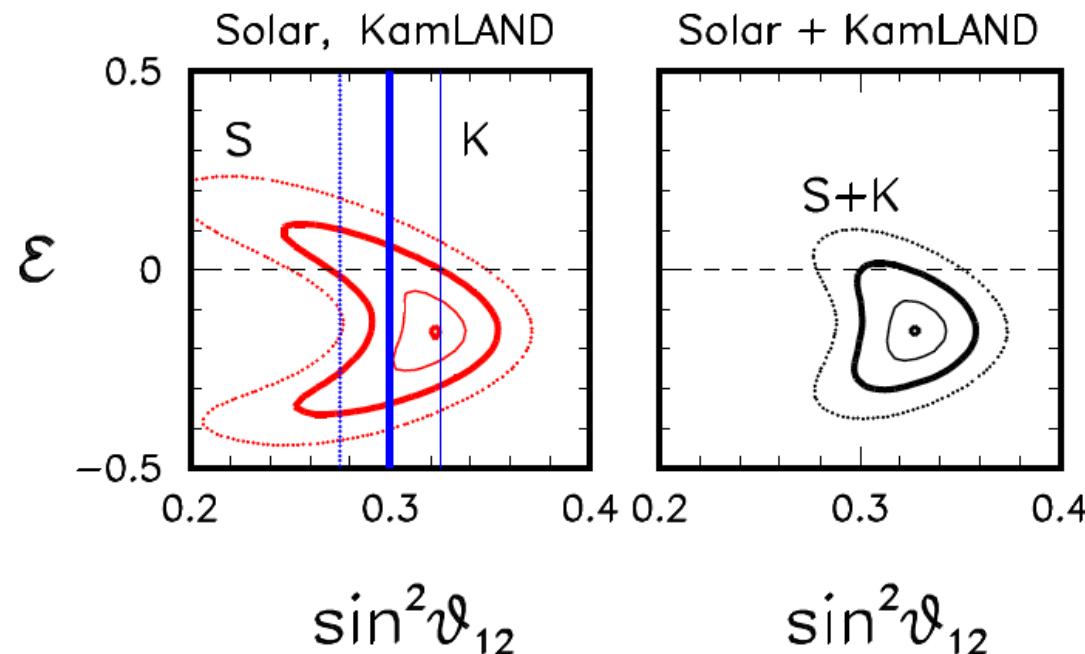
How can we obtain the opposite relation?

$$|\epsilon_{\alpha\beta}^f| > |\epsilon_{\alpha\alpha}^f \epsilon_{\beta\beta}^f|^{1/2}$$

Y.F., “[A model for lepton flavor violating Non-standard neutrino interactions](#),” PLB (2020) 135349

Hint from solar neutrinos

$$\epsilon = \epsilon_{e\mu}^{dV} \cos \theta_{23} - \epsilon_{e\tau}^{dV} \sin \theta_{23}$$

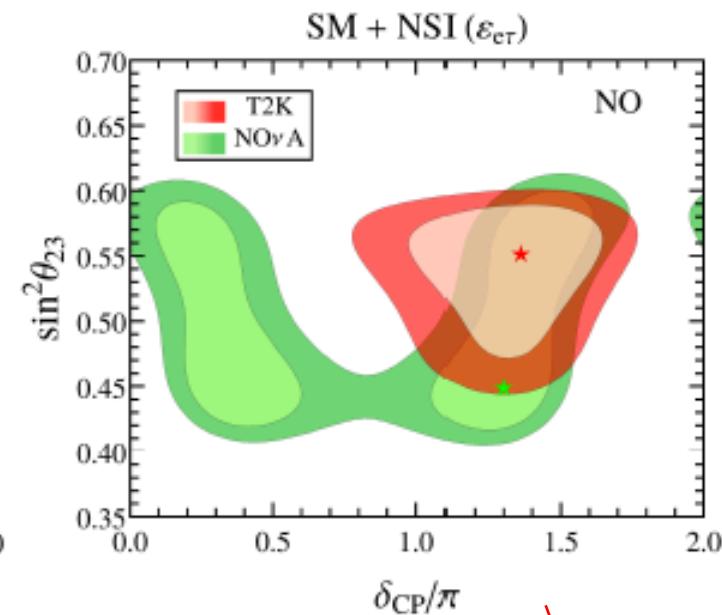
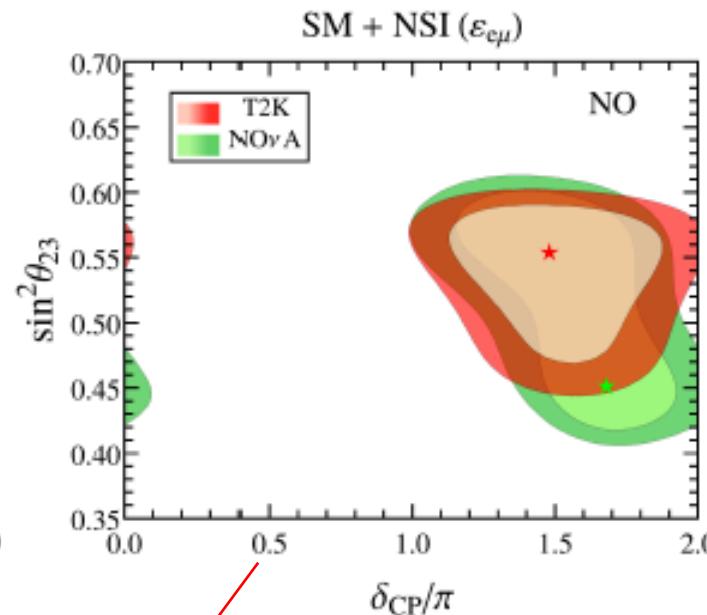
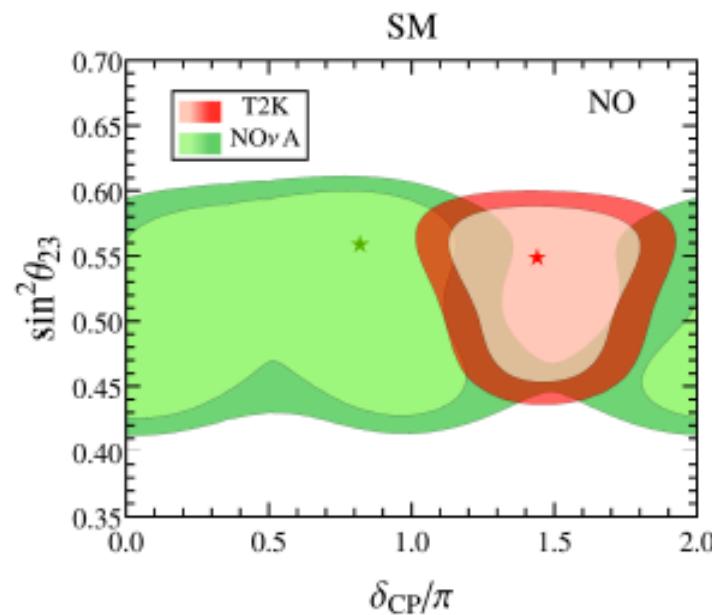


$$|\epsilon_{\alpha\beta}^f| > |\epsilon_{\alpha\alpha}^f \epsilon_{\beta\beta}^f|^{1/2}$$

Palazzo, PRD 83 (2011)

NSI as solution to Nova and T2K discrepancy

Chatterjee and Palazzo, 2008.014161



68%
90%

$$|\varepsilon_{e\mu}| = 0.15, \phi_{e\mu} = 1.38\pi$$

$$|\varepsilon_{e\tau}| = 0.275, \phi_{e\tau} = 1.62\pi$$

What we need

$$\left[\begin{array}{l} g_f(\bar{f}\gamma^\mu f)Z'_\mu \\ (g_\nu)_{\alpha\beta}(\bar{\nu}_\alpha\gamma^\mu\nu_\beta)Z'_\mu \end{array} \right] \quad \alpha \neq \beta \quad \rightarrow \quad \epsilon_{\alpha\beta}^f = \frac{g_f(g_\nu)_{\alpha\beta}}{2\sqrt{2}G_F m_{Z'}^2}$$

Y.F., “A model for lepton flavor violating
Non-standard neutrino interactions,”
PLB (2020) 135349

Coupling to neutrinos

new gauge $U'(1)$

$\psi_1 \rightarrow e^{i\alpha} \psi_1$ and $\psi_2 \rightarrow e^{-i\alpha} \psi_2$.

$$\psi_1 \equiv \frac{N_1 + N_2}{\sqrt{2}} \quad \text{and} \quad \psi_2 \equiv \frac{N_1 - N_2}{\sqrt{2}},$$

$$g_\psi (\bar{\psi}_1 \gamma^\mu \psi_1 - \bar{\psi}_2 \gamma^\mu \psi_2) Z'_\mu = g_\psi (\bar{N}_1 \gamma^\mu N_2 + \bar{N}_2 \gamma^\mu N_1) Z'_\mu.$$

Y.F., “A model for lepton flavor violating Non-standard neutrino interactions,” PLB (2020) 135349

Trick!

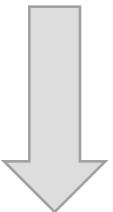
$$g_\psi (\bar{\psi}_1 \gamma^\mu \psi_1 - \bar{\psi}_2 \gamma^\mu \psi_2) Z'_\mu = g_\psi (\bar{N}_1 \gamma^\mu N_2 + \bar{N}_2 \gamma^\mu N_1) Z'_\mu.$$

Mixed with ν_α

$$\sin \alpha$$

Mixed with ν_β

$$\sin \beta$$



$$(g_\nu)_{\alpha\beta} (\bar{\nu}_\alpha \gamma^\mu \nu_\beta) Z'_\mu \quad \alpha \neq \beta.$$

$$(g_\nu)_{\alpha\beta} = g_\psi \sin \alpha \sin \beta.$$

How to obtain the mixing?

$$U'(1), \phi \rightarrow e^{i\alpha} \phi.$$

Z_2 symmetry

$$\psi_1 \leftrightarrow \psi_2, \quad Z' \rightarrow -Z' \quad \text{and} \quad \phi \rightarrow -\phi^*$$

$$L_\alpha \rightarrow L_\alpha \quad L_\beta \rightarrow -L_\beta$$

The diagram illustrates the decomposition of a state into even and odd components. A horizontal line represents the state, which is split into two parts by a vertical dashed line. Red arrows point from the text "Even" and "odd" to the left and right parts respectively. Below the diagram, the state is expressed as a linear combination of two components: $\psi_1 \equiv \frac{N_1 + N_2}{\sqrt{2}}$ and $\psi_2 \equiv \frac{N_1 - N_2}{\sqrt{2}}$.

$$\psi_1 \equiv \frac{N_1 + N_2}{\sqrt{2}} \quad \text{and} \quad \psi_2 \equiv \frac{N_1 - N_2}{\sqrt{2}},$$

$$\phi\psi_1 - \phi^*\psi_2$$

$$Z_2$$

Even

$$\phi\psi_1 + \phi^*\psi_2$$

Odd

$$Y_1 \bar{N}_{R1}(\phi\psi_1 + \phi^*\psi_2) + Y_2 \bar{N}_{R2}(\phi\psi_1 - \phi^*\psi_2)$$



$$m_{N_1} \bar{N}_{R1} N_1 + m_{N_2} \bar{N}_{R2} N_2$$

$$m_{N_1} = Y_1 v_\phi \quad m_{N_2} = Y_2 v_\phi$$

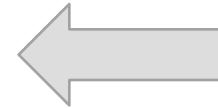
$$Y_{R\alpha} \bar{N}_{1R} H^T c L_\alpha + Y_{R\beta} \bar{N}_{2R} H^T c L_\beta$$

The equation consists of two terms separated by a plus sign. Each term contains a scalar coefficient ($Y_{R\alpha}$ or $Y_{R\beta}$), a fermion field (\bar{N}_{1R} or \bar{N}_{2R}), a metric tensor (H^T), a charge vector (c), and a lepton field (L_α or L_β). Two yellow arrows point from the terms to the words "even" and "odd" respectively.

$$Y_{R\alpha} \bar{N}_{1R} H^T c L_\alpha + Y_{R\beta} \bar{N}_{2R} H^T c L_\beta$$

$$m_{N_1} = Y_1 v_\phi$$

$$[\nu_\alpha^T \ N_1^T \ N_{1R}^\dagger c] c \begin{bmatrix} 0 & 0 & Y_{R\alpha} \langle H \rangle \\ 0 & 0 & m_{N_1} \\ Y_{R\alpha} \langle H \rangle & m_{N_1} & 0 \end{bmatrix} \begin{bmatrix} \nu_\alpha \\ N_1 \\ c N_{1R}^* \end{bmatrix}$$



Inverse seesaw

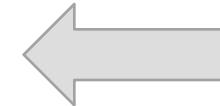
$$\begin{bmatrix} 1 & -\frac{Y_{R\alpha} \langle H \rangle}{m_{N_1}} & 0 \\ \frac{Y_{R\alpha} \langle H \rangle}{m_{N_1}} & \frac{1}{\sqrt{2}} & -\frac{1}{\sqrt{2}} \\ \frac{Y_{R\alpha} \langle H \rangle}{m_{N_1}} & \frac{1}{\sqrt{2}} & \frac{1}{\sqrt{2}} \end{bmatrix}$$

$$\sin \alpha = -\frac{Y_{R\alpha} \langle H \rangle}{m_{N_1}}$$

$$Y_{R\alpha} \bar{N}_{1R} H^T c L_\alpha + Y_{R\beta} \bar{N}_{2R} H^T c L_\beta$$

$$m_{N_1} = Y_1 v_\phi$$

$$[\nu_\alpha^T \ N_1^T \ N_{1R}^\dagger c] c \begin{bmatrix} 0 & 0 & Y_{R\alpha} \langle H \rangle \\ 0 & 0 & m_{N_1} \\ Y_{R\alpha} \langle H \rangle & m_{N_1} & 0 \end{bmatrix} \begin{bmatrix} \nu_\alpha \\ N_1 \\ c N_{1R}^* \end{bmatrix}$$



Inverse seesaw

$$\begin{bmatrix} 1 & -\frac{Y_{R\alpha} \langle H \rangle}{m_{N_1}} & 0 \\ \frac{Y_{R\alpha} \langle H \rangle}{m_{N_1}} & \frac{1}{\sqrt{2}} & -\frac{1}{\sqrt{2}} \\ \frac{Y_{R\alpha} \langle H \rangle}{m_{N_1}} & \frac{1}{\sqrt{2}} & \frac{1}{\sqrt{2}} \end{bmatrix}$$

Similarly for $\nu_\alpha \rightarrow \nu_\beta$,
 $Y_{R\alpha} \rightarrow Y_{R\beta}$,
 $m_{N_1} \rightarrow m_{N_2}$

$$\sin \beta = -\frac{Y_{R\beta} \langle H \rangle}{m_{N_2}}$$

Flavor structure of NSI

$$(g_\nu)_{\alpha\beta} = g_\psi \sin \alpha \sin \beta.$$

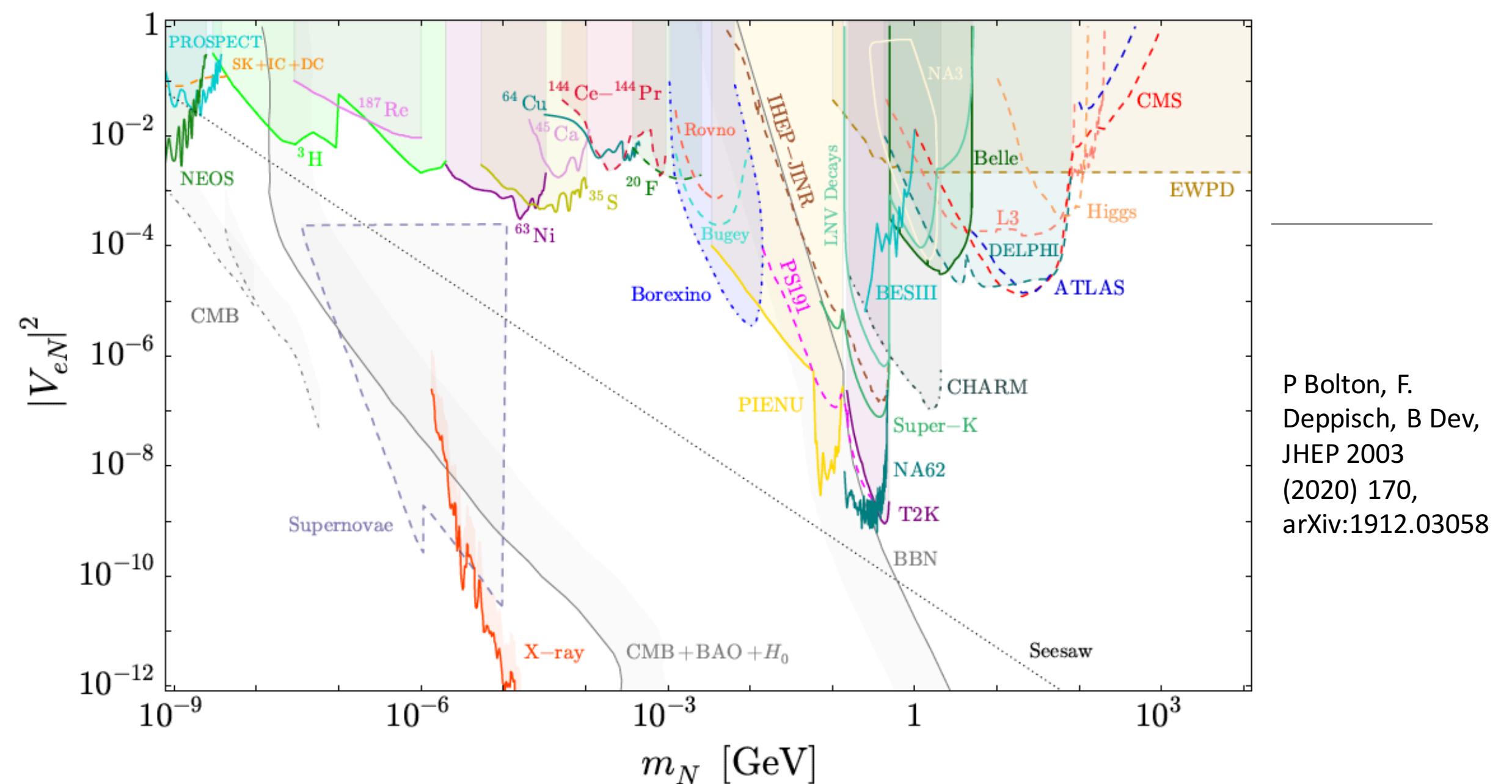
$$(g_\nu)_{\alpha\alpha} = 0 \qquad \qquad \epsilon_{\alpha\alpha} = 0$$

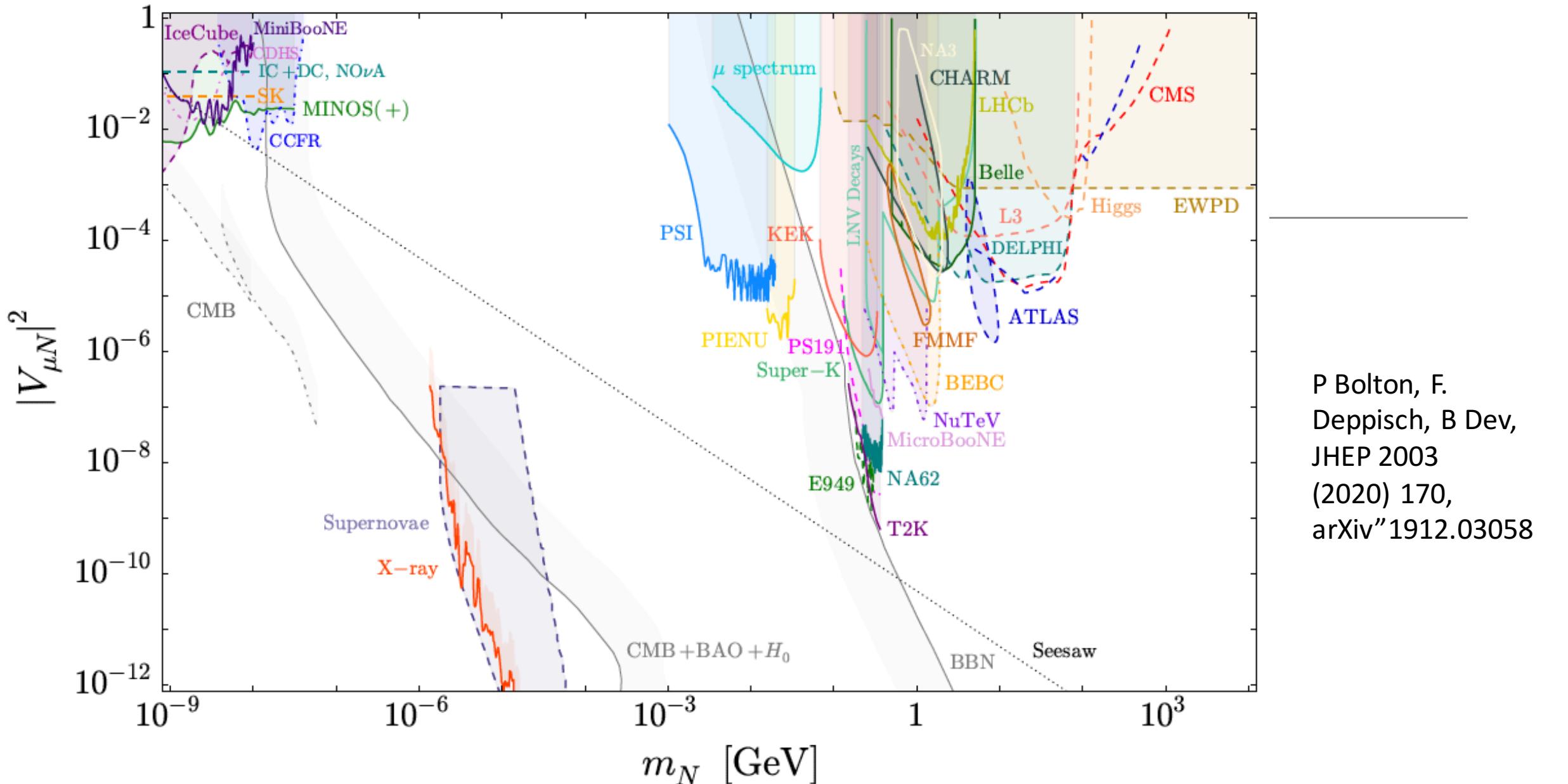
$$(g_\nu)_{\beta\beta} = 0 \quad \longrightarrow \quad \epsilon_{\beta\beta} = 0$$

$$(g_\nu)_{\alpha\beta} \neq 0 \qquad \qquad \epsilon_{\alpha\beta} \neq 0$$

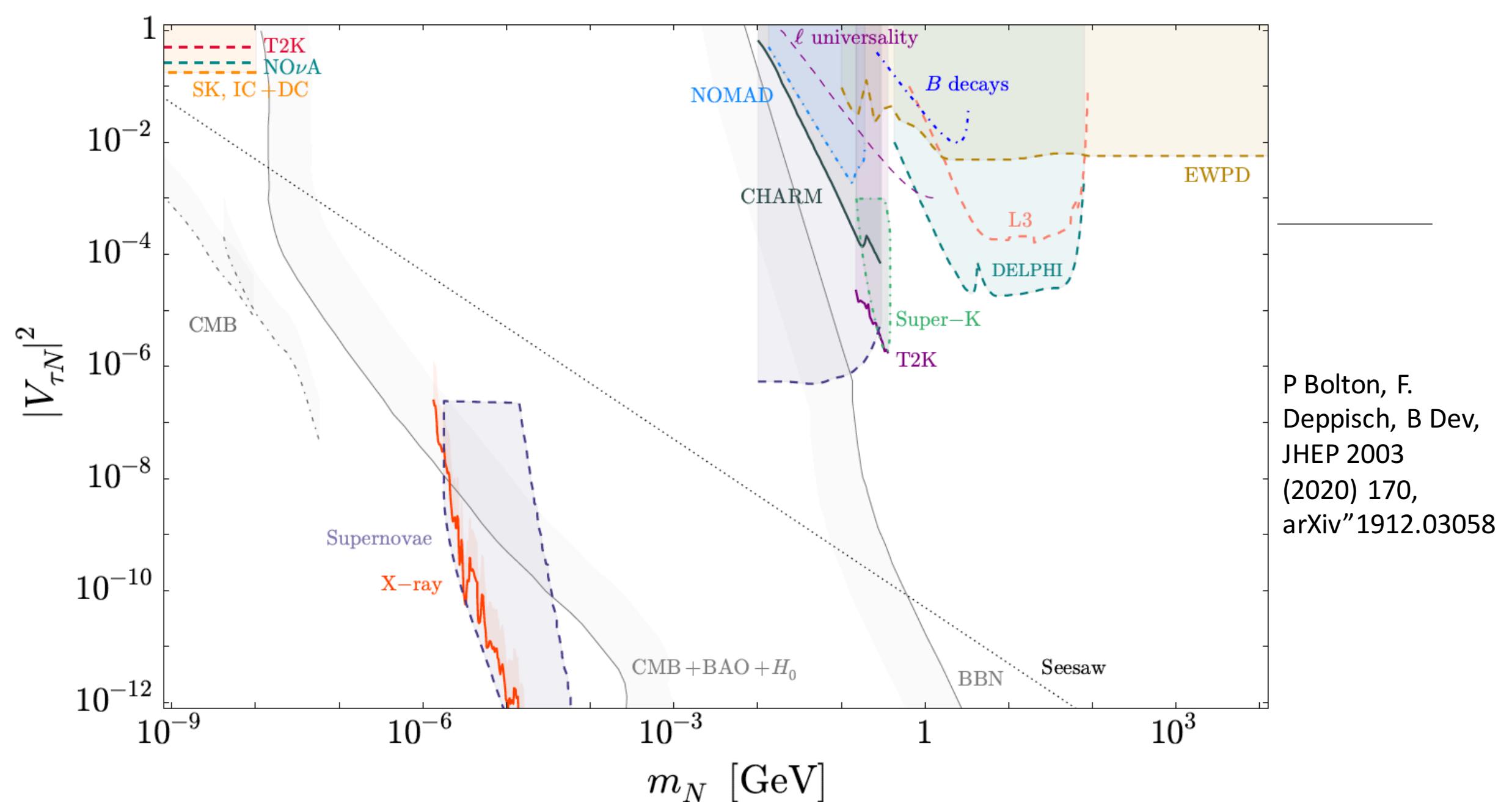
Bounds on the mixing of N_1 and N_2 with active neutrinos
I.e., Bounds on

$$\sin \alpha \text{ and } \sin \beta$$





P Bolton, F.
 Deppisch, B Dev,
 JHEP 2003
 (2020) 170,
 arXiv"1912.03058



$m_{N_1}, m_{N_2} > 500 \text{ MeV}$



No bound from supernova and BBN or Kaon decay

$$m_{N_1} = Y_1 v_\phi \quad m_{N_2} = Y_2 v_\phi$$

$$m_{Z'} = g_\psi v_\phi / \sqrt{2} > (g_\psi / Y_{1,2}) 500 \text{ MeV}$$

$$\epsilon_{\alpha\beta}^q = \frac{0.12}{g_\psi} \frac{g_q}{10^{-3}}$$

Can we escape the bounds?

Most of the bounds come from searching the last charged leptons.

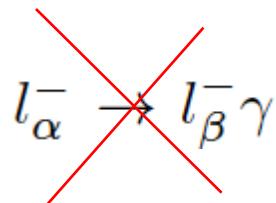
Electroweak interactions: $N \rightarrow l_\alpha \bar{l}_\beta \nu$

The dominant decay mode in our model: $N \rightarrow Z' \nu \quad Z' \rightarrow \nu \bar{\nu}$

Lepton flavor violating process

Violation of unitarity:

$$(U_{PMNS}^\dagger \cdot U_{PMNS})_{\alpha\beta}|_{\alpha \neq \beta}$$

$$l_\alpha^- \rightarrow l_\beta^- \gamma$$


ν_α mixes with N_1

ν_β mixes with N_2

two-loop suppressed

Violation of unitarity of the mixing matrix

$Z \rightarrow \text{invisibles}$

$W \rightarrow l + \text{missing energy}$

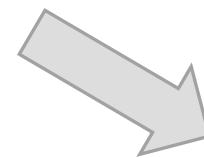
Deviation from SM is
Suppressed both by $\sin^2 \alpha$ or $\sin^2 \beta$ and $O\left(\frac{m_N^2}{m_W^2}\right)$

$$m_N > m_K,$$

$K^+(\pi^+) \rightarrow l_\alpha^+ \nu$

$K^+(\pi^+) \rightarrow l_\beta^+ \nu$

$$\sin \alpha, \sin \beta < 0.03$$



$$(g_\nu)_{\alpha\beta}|_{\alpha \neq \beta} < 10^{-3} g_\psi$$

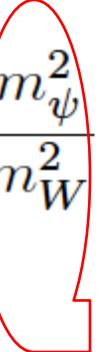
LFV charged lepton decay

~~$l_\alpha \rightarrow l_\beta \gamma$~~

two-loop suppressed

$l_\alpha \rightarrow l_\beta Z'$

One-loop effect

$$\frac{m_\alpha}{4\pi} \left(\frac{\frac{m_\psi^2}{m_W^2}}{\frac{g_\nu}{16\pi^2}} \right)^2 g_{SU(2)}^4 \frac{m_\alpha^2}{m_{Z'}^2}$$


GIM suppression

LFV charged lepton decay

~~$l_\alpha \rightarrow l_\beta \gamma$~~

two-loop suppressed

$l_\alpha \rightarrow l_\beta Z'$

One-loop effect

PDG:

$$\text{Br}(\tau \rightarrow eZ') < 2.7 \times 10^{-3} \quad \text{and} \quad \text{Br}(\tau \rightarrow \mu Z') < 5 \times 10^{-3}$$

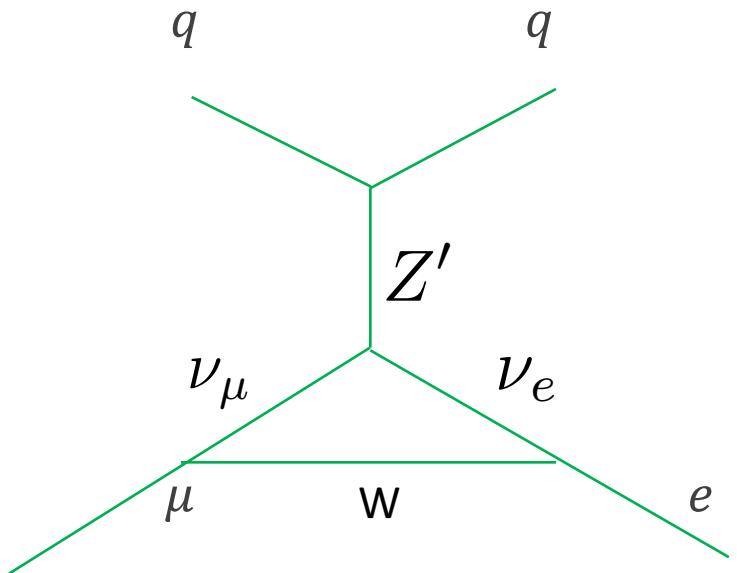
Heeck and Rodejohann,
PLB776 (2018) 385

$$Br(\mu \rightarrow eZ') < 10^{-5}$$



Close to the prediction for $(g_\nu)_{\mu e} \sim 10^{-3}$ and $m_{Z'} \sim 10 \text{ MeV}$

muon to electron conversion



SINDRUM II collaboration
Bertl et al., Eur Phys J C 47 (2006) 337

$$R < 7 \times 10^{-13}$$

$$R = \frac{\Gamma(\mu + N \rightarrow e + N)}{\Gamma(\mu + N \rightarrow \nu_\mu + N')} \sim \frac{(g_\nu)_{e\mu}^2 g_q^2}{(16\pi^2)^2} \left(\frac{m_\psi^2}{m_\mu^2 + m_{Z'}^2} \right)^2 = 5 \times 10^{-15} \left(\frac{g_\nu}{10^{-3}} \right)^2 \left(\frac{g_q}{10^{-4}} \right)^2 \left(\frac{m_\psi}{1 \text{ GeV}} \right)^4$$

Mu2e, COMET

$$R \sim 5 \times 10^{-17}$$

Smoking gun of the model

- 1) $\epsilon_{e\mu} \sim 0.1$
- 2) Muon to e conversion on nuclei but $\mu^- \rightarrow e^- \gamma$
- 3) $\mu^- \rightarrow e^- Z'$
- 4) $K^+(\pi^+) \rightarrow l^+ + \text{missing energy}$

Summary

In the neutrino precision era, we should take possibility of NSI more serious.

New $\text{U}(1)$: Light mediator, small coupling  large NSI

Mixing of neutrinos with fermions charged under new $\text{U}(1)$  LFV NSI for neutrinos
No LFV NSI for charged leptons

Models for arbitrary flavor structure: $\epsilon_{\alpha\alpha}\epsilon_{\beta\beta} > |\epsilon_{\alpha\beta}|^2$ or $\epsilon_{\alpha\alpha}\epsilon_{\beta\beta} < |\epsilon_{\alpha\beta}|^2$

Backup slides

Higgs invisible decay mode

$$Y_{R\alpha} \bar{N}_{1R} H^T c L_\alpha + Y_{R\beta} \bar{N}_{2R} H^T c L_\beta$$

$$\downarrow$$

$$H \rightarrow \bar{\nu}_\alpha N_1$$

$$\downarrow$$

$$H \rightarrow \bar{\nu}_\beta N_2$$

$$Y_{R\alpha}^2 m_H / (4\pi)$$

$$Y_{R\beta}^2 m_H / (4\pi)$$

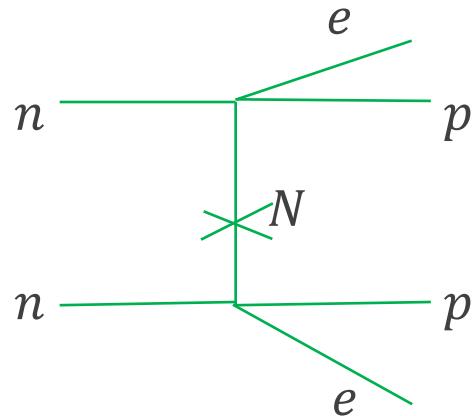
PDG

$$\text{Br}(H \rightarrow \text{invisibles}) < 0.2 \quad \rightarrow \quad Y_{R\alpha,\beta} \langle H \rangle < 2 \text{ GeV}$$

In our model:

$$Y_{R\alpha,\beta} \langle H \rangle \sim 15 \text{ MeV}$$

Lepton number violation



Majorana mass

$$m_N N^T c N$$

LHCb: $B^- \rightarrow \pi^+ \mu^- \mu^-$

Dirac mass

$$m_N \bar{N} N$$

$$\frac{M_N}{2} (\psi_1^T c \psi_2 + \psi_2^T c \psi_1) + H.c. = \frac{M_N}{2} (N_1^T c N_1 - N_2^T c N_2) + H.c.$$

Z' coupling to matter fields

1

Gauging a linear combination of Baryon number and lepton numbers

$$B - (a_e L_e + a_\mu L_\mu + a_\tau L_\tau)$$

$$a_e + a_\mu + a_\tau = 3$$

$$g_q = g_B/3 \text{ and } g_\alpha = a_\alpha g_B \text{ where } \alpha \in \{e, \mu, \tau\}$$

2

Kinetic mixing with hypercharge gauge boson

$$\delta Z'_{\mu\nu} B^{\mu\nu}$$

Photon component

$$g_f = (Q_f e) \cos \theta_W \delta.$$

Z component

Coupling suppressed by $(m_{Z'}^2/m_Z^2)\delta \sin \theta_W$

z' coupling to matter fields

1

Gauging a linear combination of Baryon number and lepton numbers

$$B - (a_e L_e + a_\mu L_\mu + a_\tau L_\tau)$$

$$a_e + a_\mu + a_\tau = 3$$

$$g_q = g_B/3 \text{ and } g_\alpha = a_\alpha g_B \text{ where } \alpha \in \{e, \mu, \tau\}$$

2

Kinetic mixing with hypercharge gauge boson

$$\delta Z'_{\mu\nu} B^{\mu\nu}$$

Photon component

$$g_f = (Q_f e) \cos \theta_W \delta.$$



$$\epsilon_{\alpha\beta}^p = -\epsilon_{\alpha\beta}^e$$



NSI in CE ν NS

CONUS, COHERENT

NO NSI in neutrino oscillation

Gauging $B - (a_e L_e + a_\mu L_\mu + a_\tau L_\tau)$

$$a_e = 0$$

$$130 \text{ MeV} > m_{Z'} > 10 \text{ MeV}$$

$$g_q \sim g_\tau \sim g_\mu \sim g_\nu < 10^{-3}$$

$$Z' \rightarrow \nu\bar{\nu}$$

$$(g_\nu)_{\alpha\beta} = 10^{-3} g_\psi \text{ and } m_{Z'} \sim 500 \text{ MeV} g_\psi$$

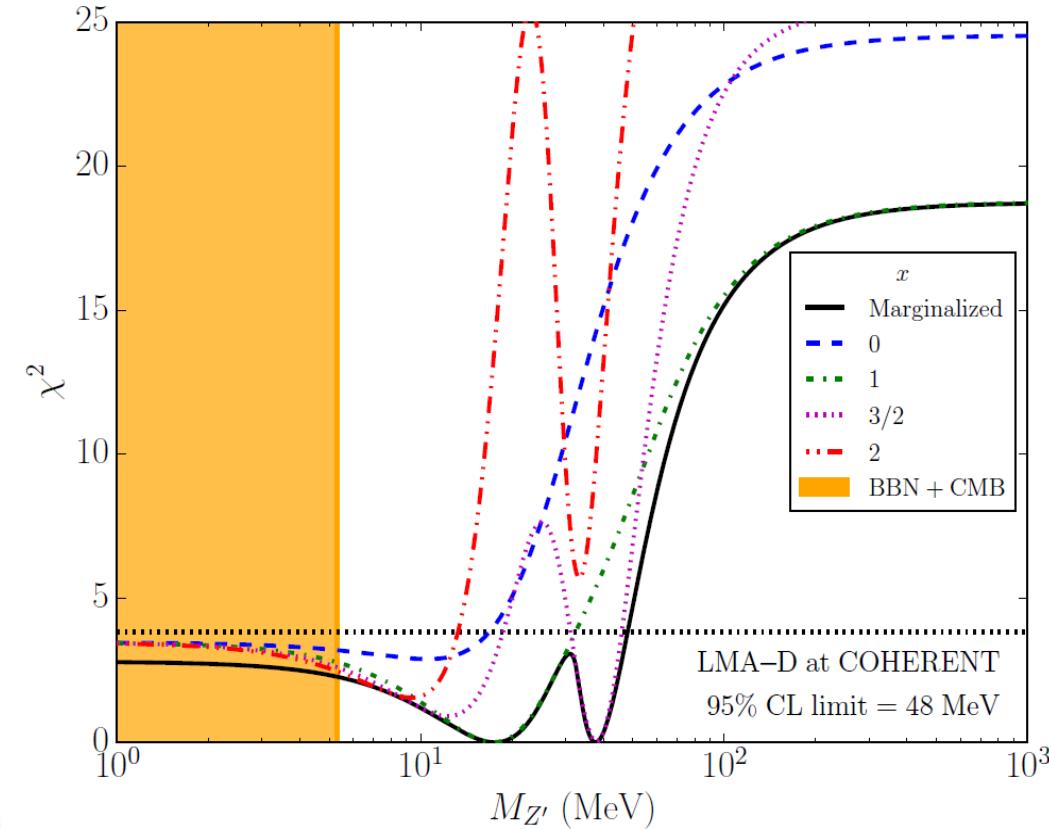
$$\epsilon_{\alpha\beta}^q = \frac{0.12}{g_\psi} \frac{g_q}{10^{-3}}$$

LMA-Dark after COHERENT data

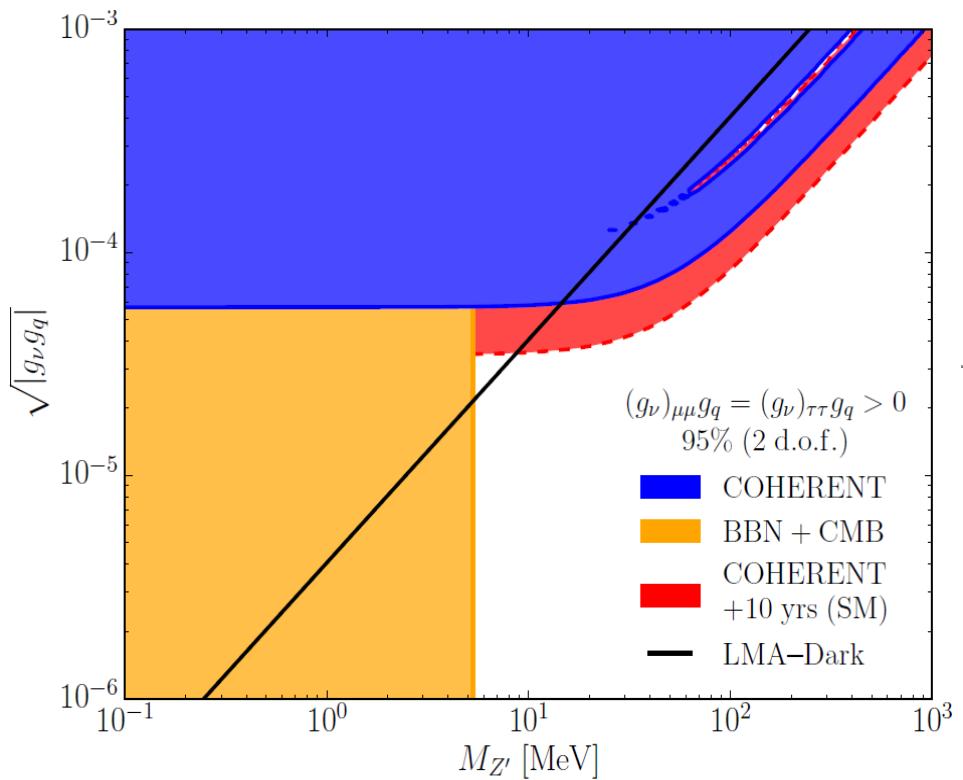
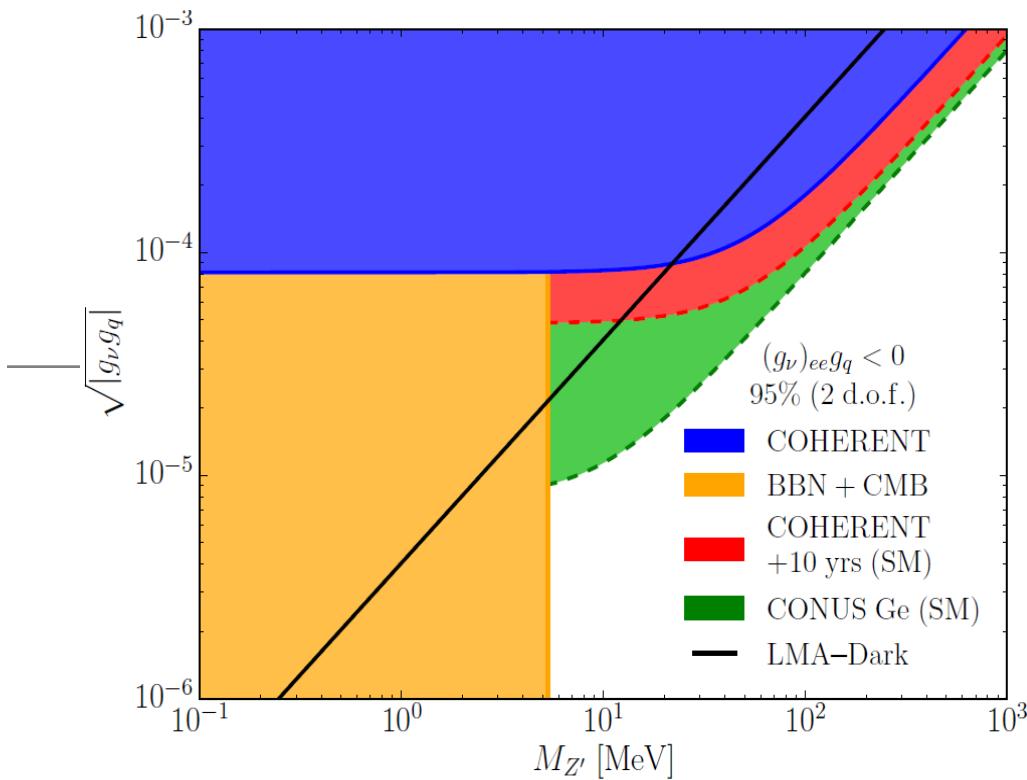
$$(\epsilon_{ee}, \epsilon_{\mu\mu}, \epsilon_{\tau\tau}) = (x - 2, x, x)$$

$$\epsilon_{ee}^{u,V} = \epsilon_{ee}^{d,V} = \frac{x}{4} - \frac{1}{2}$$

$|M_{Z'} > 48 \text{ MeV at 95\% C.L. (1 d.o.f.)}|$



Denton, YF and Shoemaker, JHEP 1807 (2018) 037; arXiv:1804.03660.

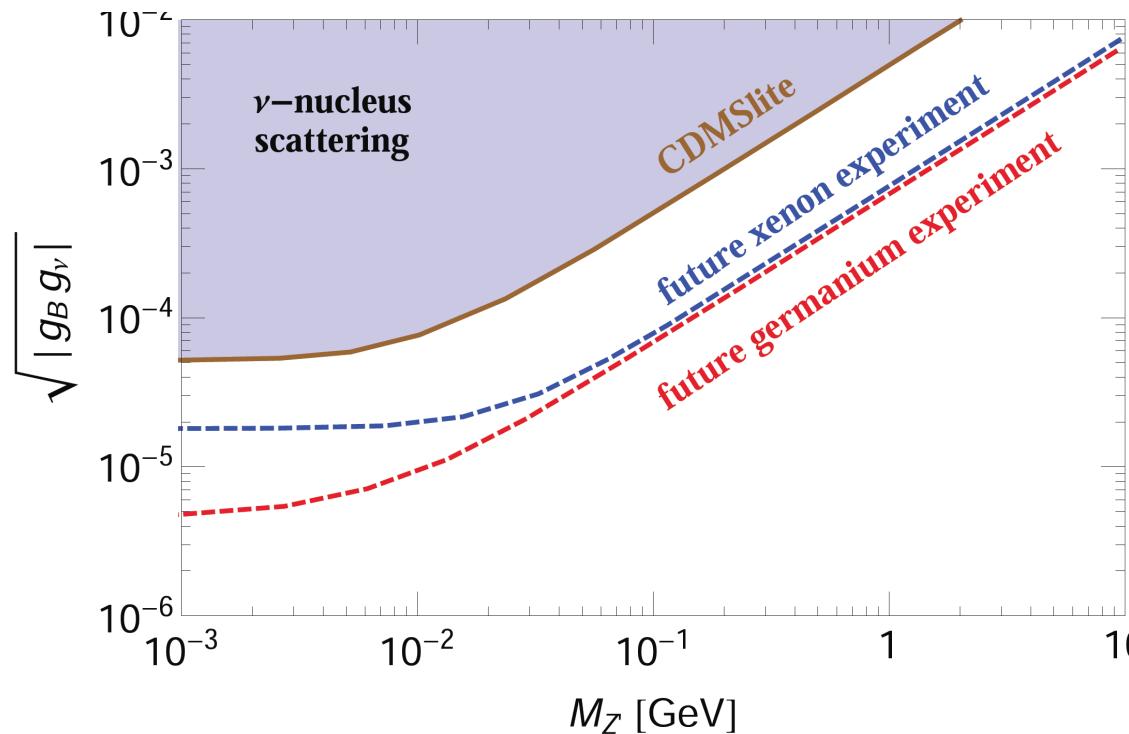


Denton, YF and Shoemaker, JHEP 1807 (2018) 037; arXiv:1804.03660.

COherent NeUtrino Scattering experiment (CONUS)

Germanium detector with detection threshold of 0.1 keV located 17 m away from a nuclear power plant 3.9 GW in Brokdorf, Germany

Solar neutrino interaction at DM direct detection experiments

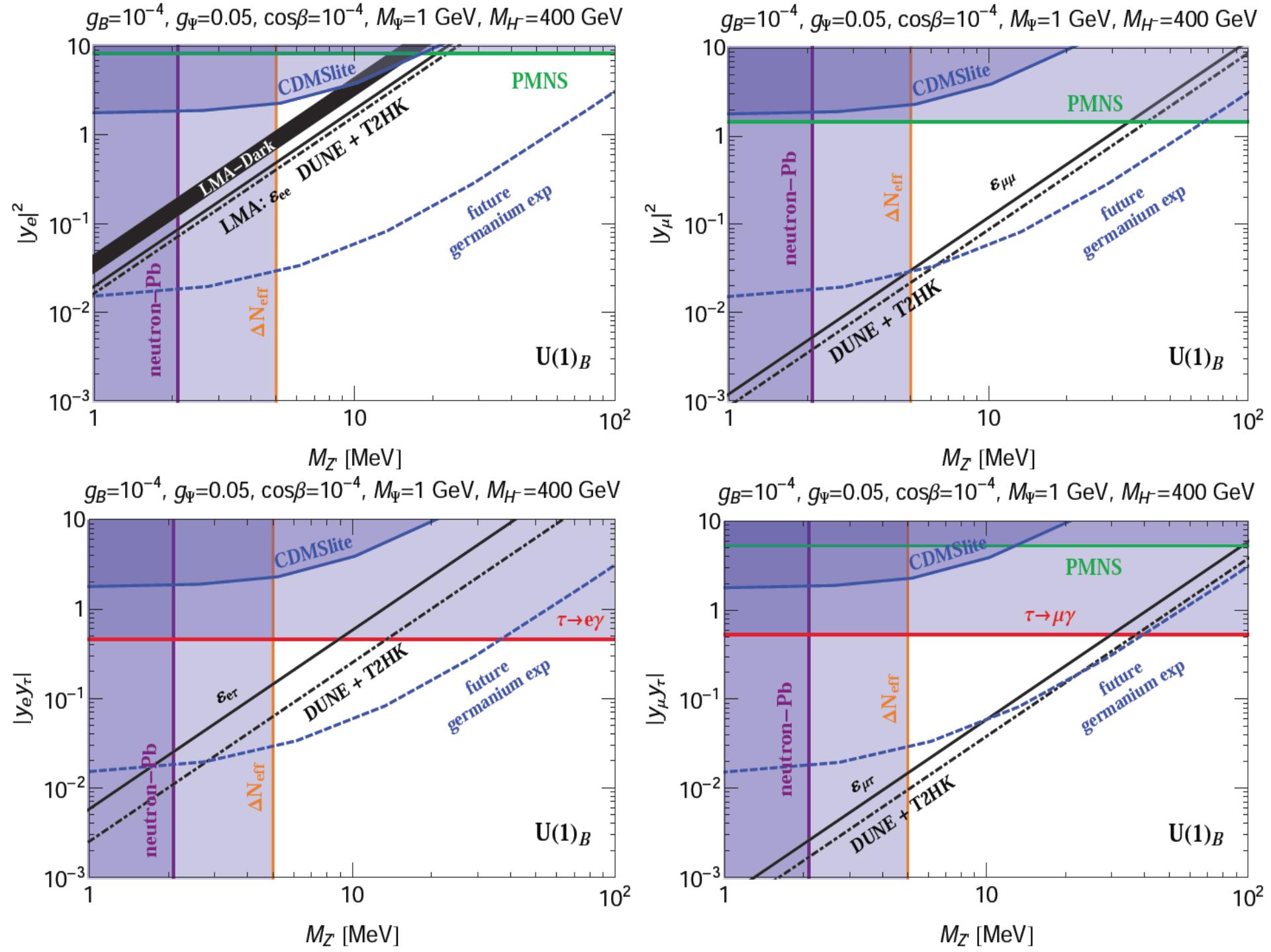


Y.F. and J. Heeck, PRD94 (2016);

Cerdeno et al, JHEP 05 (2016) 118

SuperCDMS SNOLAB

LUX-ZEPLIN



Y.F. and J. Heeck, PRD94 (2016)

Solar neutrino coherent
Interaction in future direct
dark matter search experiments

$$\kappa_\alpha = \frac{y_\alpha \langle H' \rangle}{M_\Psi} = \frac{y_\alpha v \cos \beta}{\sqrt{2} M_\Psi}$$

		90% CL		3 σ	
Param.	best-fit	LMA	LMA \oplus LMA-D	LMA	LMA \oplus LMA-D
$\varepsilon_{ee}^u - \varepsilon_{\mu\mu}^u$	+0.298	[+0.00, +0.51]	\oplus [-1.19, -0.81]	[-0.09, +0.71]	\oplus [-1.40, -0.68]
$\varepsilon_{\tau\tau}^u - \varepsilon_{\mu\mu}^u$	+0.001	[-0.01, +0.03]	[-0.03, +0.03]	[-0.03, +0.20]	[-0.19, +0.20]
$\varepsilon_{e\mu}^u$	-0.021	[-0.09, +0.04]	[-0.09, +0.10]	[-0.16, +0.11]	[-0.16, +0.17]
$\varepsilon_{e\tau}^u$	+0.021	[-0.14, +0.14]	[-0.15, +0.14]	[-0.40, +0.30]	[-0.40, +0.40]
$\varepsilon_{\mu\tau}^u$	-0.001	[-0.01, +0.01]	[-0.01, +0.01]	[-0.03, +0.03]	[-0.03, +0.03]
ε_D^u	-0.140	[-0.24, -0.01]	\oplus [+0.40, +0.58]	[-0.34, +0.04]	\oplus [+0.34, +0.67]
ε_N^u	-0.030	[-0.14, +0.13]	[-0.15, +0.13]	[-0.29, +0.21]	[-0.29, +0.21]
$\varepsilon_{ee}^d - \varepsilon_{\mu\mu}^d$	+0.310	[+0.02, +0.51]	\oplus [-1.17, -1.03]	[-0.10, +0.71]	\oplus [-1.44, -0.87]
$\varepsilon_{\tau\tau}^d - \varepsilon_{\mu\mu}^d$	+0.001	[-0.01, +0.03]	[-0.01, +0.03]	[-0.03, +0.19]	[-0.16, +0.19]
$\varepsilon_{e\mu}^d$	-0.023	[-0.09, +0.04]	[-0.09, +0.08]	[-0.16, +0.11]	[-0.16, +0.17]
$\varepsilon_{e\tau}^d$	+0.023	[-0.13, +0.14]	[-0.13, +0.14]	[-0.38, +0.29]	[-0.38, +0.35]
$\varepsilon_{\mu\tau}^d$	-0.001	[-0.01, +0.01]	[-0.01, +0.01]	[-0.03, +0.03]	[-0.03, +0.03]
ε_D^d	-0.145	[-0.25, -0.02]	\oplus [+0.49, +0.57]	[-0.34, +0.05]	\oplus [+0.42, +0.70]
ε_N^d	-0.036	[-0.14, +0.12]	[-0.14, +0.12]	[-0.28, +0.21]	[-0.28, +0.21]