

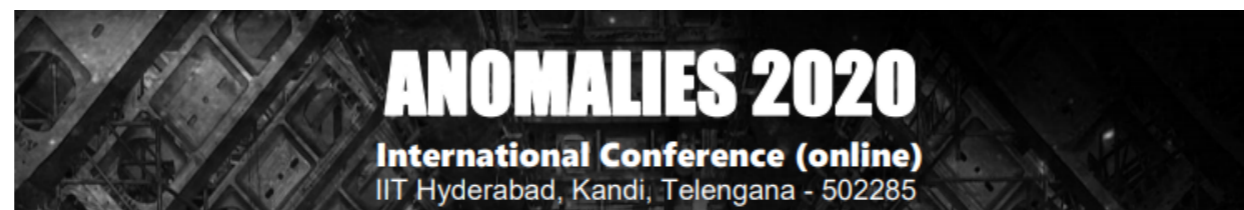
A recette for combined explanation of anomalies in ^8Be nuclear transitions and $(g - 2)_{e,\mu}$



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Based on *JHEP* 07 (2020) 235
in collaboration with

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Physics beyond the Standard Model (BSM): direction

The only laboratory evidence of BSM physics so far:
neutrino oscillations => neutrino masses



Other strong motivations: observed baryon asymmetry of the Universe, dark matter, dark energy

A number of theoretical caveats/motivations:

hierarchy problem, unification of interactions, gravity, parity violation, ...

Hundreds of theoretical candidates for BSM physics to address neutrino masses and other theoretical motivations: **how to proceed?**

Guidance from multi-frontier experimental searches



A challenge: lack of any direction from the direct collider searches so far

A particularly interesting alternative is to look for deviations from the SM @ rare processes with no or small SM backgrounds (high intensity frontier)

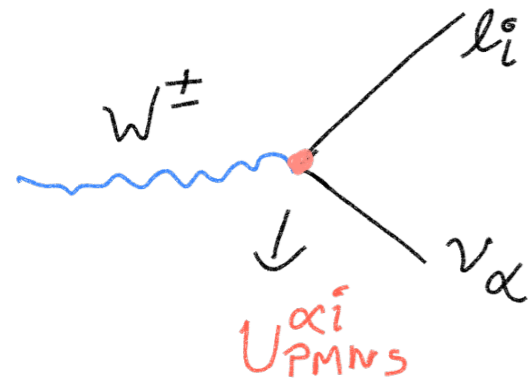
- lepton moments: $(g-2)$ and EDMs
- charged lepton flavour violation (cLFV)
- lepton number violation (LNV)
- lepton flavour universality violation (LFUV)
- ...

What's so special about leptonic observables?

Purely SM:

- strictly massless neutrinos
- conservation of total lepton number and lepton flavours
- leptonic EDMs at 4-loop level $d_e^{\text{CKM}} \leq 10^{-38} e \text{ cm}$

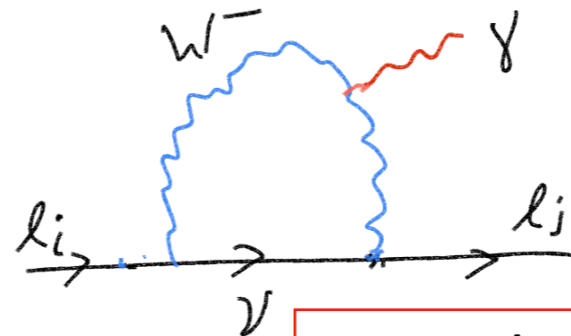
What if the SM is extended minimally to only include massive Dirac neutrinos?



$$\mathcal{L}_{\text{lepton CC}} = U_{\text{PMNS}} W_{\mu}^{-} \bar{\ell}_L \gamma^{\mu} \nu_L + \text{h.c.}$$

$$\begin{aligned} (\nu_e, \nu_{\mu}, \nu_{\tau}) &\overset{U_{\text{PMNS}}}{\longleftrightarrow} (\nu_1, \nu_2, \nu_3) \\ |\nu_{\alpha}\rangle &= U_{\alpha i}^{*} |\nu_i\rangle \end{aligned}$$

no LNV, finite but extremely tiny cLFV



$$\text{BR}(\mu \rightarrow e \gamma) \propto \left| \sum U_{\mu i}^{*} U_{e i} \frac{m_{\nu_i}^2}{M_W^2} \right|^2 \sim 10^{-54}$$

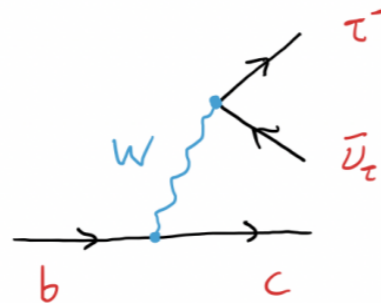
Cheng and Li '77; Petcov '77;
Marciano and Sanda '77; Shrock and Lee ...

EDM at 2-loop level, but still tiny $d_e^{\text{lep}} \leq 10^{-35} e \text{ cm}$

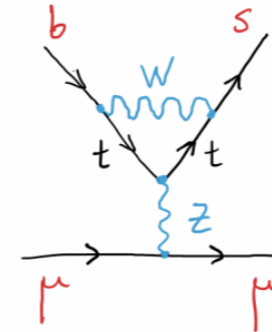
Therefore any signal from the current or upcoming experiments will be a clear indication of some nontrivial NP

Charged lepton sector is currently hosting several lingering tensions with the SM!

★ Lepton flavour universality violation in CC and NC B -decays



~15% of a SM tree-level effect



~20% of a SM loop effect

- explainable separately by invoking heavy NP: scalar LQ, RPV SUSY, heavy Z' ,
- only select few scenarios can explain them combined: vector LQ, combinations of scale LQ

see many interesting talks@
Anomalies 2020

★ Long-standing tension in $(g - 2)_\mu$ explainable by many NP candidates!

★ Emerging anomaly in $(g - 2)_e$ less-trivial to explain when combined with $(g - 2)_\mu$

★ Anomalous internal pair creation in ^8Be transitions requires light NP ~ 17 MeV

Muon and electron magnetic dipole moment

Muon (g-2):

lingering tension between SM and experiment!

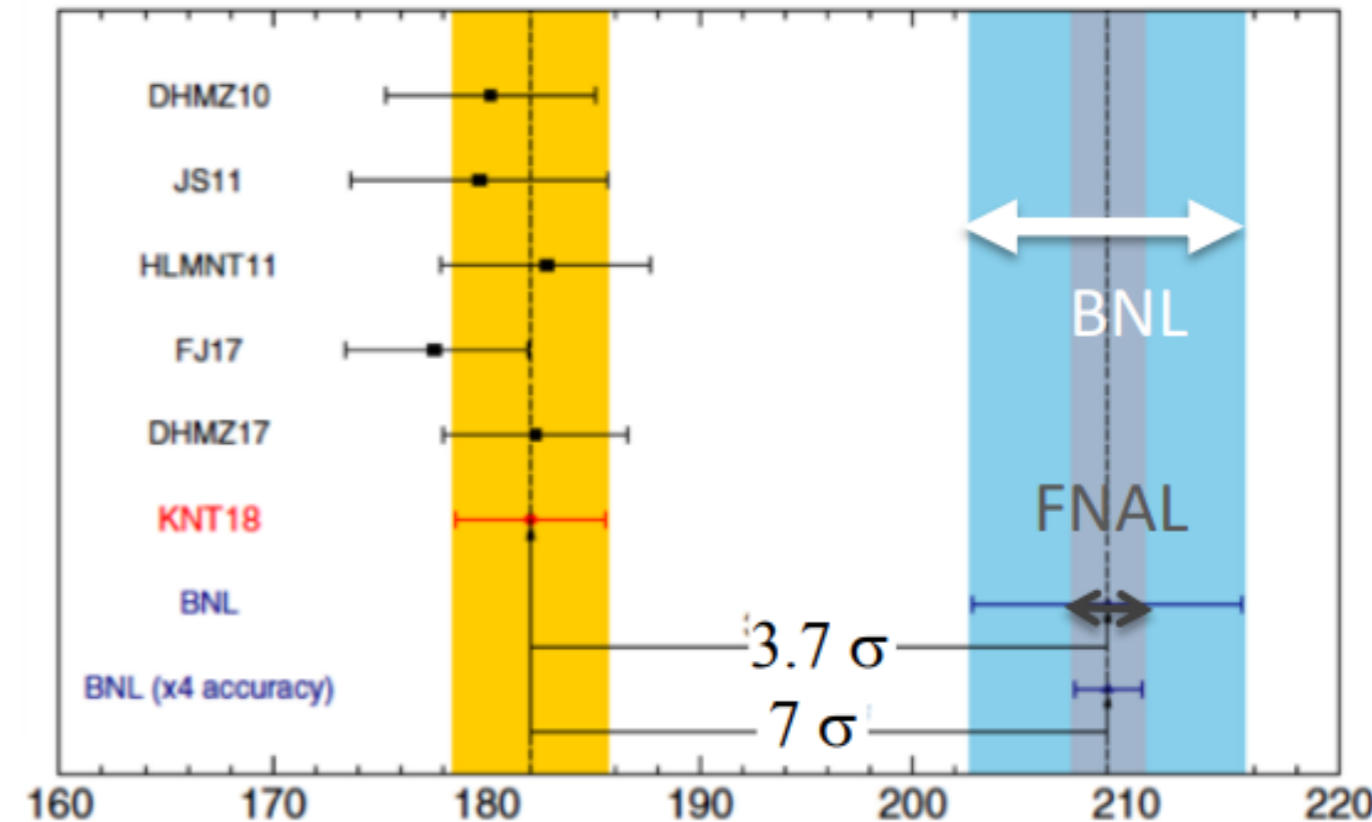
$$\Delta a_\mu := a_\mu^{\text{exp}} - a_\mu^{\text{SM}} = 279(76) \times 10^{-11}$$

$$a_\mu^{\text{BNL}} = 116\,592\,089(63) \times 10^{-11}$$

$$a_\mu^{\text{SM}} = 116\,591\,810(43) \times 10^{-11}$$

the latest consensus value

current tension @ 3.7σ



upcoming experimental results from Fermilab/JPARC will update the current deadlock

Electron (g-2): interesting development with new measurement of α using Cs

Parker et. al.
Science (2018)

$$a_e^{\text{SM}}|_{\alpha_{\text{Cs}}} = 1\,159\,652\,181.61(23) \times 10^{-12}$$

$$\Delta a_e := a_e^{\text{exp}} - a_e^{\text{SM}} = -0.88(36) \times 10^{-12}$$

current tension @ 2.5σ

Another developing anomaly ?

Minimal scenarios: explaining $(g - 2)_\mu$ and $(g - 2)_e$ simultaneously

$$\Delta a_\mu := a_\mu^{\text{exp}} - a_\mu^{\text{SM}} = 279(76) \times 10^{-11}$$

$$\Delta a_e := a_e^{\text{exp}} - a_e^{\text{SM}} = -0.88(36) \times 10^{-12}$$

Heavy NP EFT:

$$\mathcal{H}_{\text{eff}} = c_R^{\ell_f \ell_i} \bar{\ell}_f \sigma_{\mu\nu} P_R \ell_i F^{\mu\nu} + \text{h.c.}$$

$$a_i \sim -\frac{2m_i}{e} (c_R^{\ell_i \ell_i} + c_R^{\ell_i \ell_i^*})$$

$$\text{Br}[\mu \rightarrow e \gamma] \sim \frac{m_\mu^3}{4\pi \Gamma_\mu} (|c_R^{\mu e}|^2 + |c_R^{e\mu}|^2)$$

NP with universal coupling:



$$\frac{\Delta a_\mu}{\Delta a_e} \sim \frac{m_\mu^2}{m_e^2}$$

$$\frac{\Delta a_\mu}{\Delta a_e} \sim \frac{m_\mu}{m_e}$$

Neither compatible with the observed behaviour

Giudice et al JHEP 2012
Crivellin et al. PRD 2018
Calibbi et al JHEP 2020
++

Ingredients to achieve a simultaneous explanation:

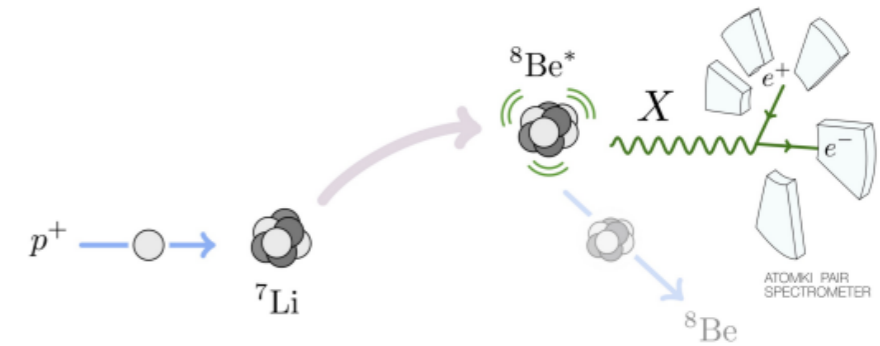
breaking the universality of the flavour structure of NP

some type of cancellation among different contributions

Vector-like leptons together with nontrivial NP seems to be a plausible option!

Anomalies in nuclear transitions of: ^8Be and ^4He

- Create excited $^8\text{Be}^*$ from a p-beam on ^7Li
- Nucleus de-excites emitting a γ
- Measure angular distribution of e^+e^- from internal pair creation



In 2016, the ATOMKI collaboration reported to have seen a “ 6.8σ ” excess in $^8\text{Be}^* \rightarrow ^8\text{Be} \gamma (\rightarrow e^+e^-)$ transition, compatible with a resonance Krasznahorkay et al PRL 2016 2019 reinvestigation @ “ 5σ ”

$$^8\text{Be}^{*'}(j^\pi = 1^+, T = 1^*) \rightarrow ^8\text{Be}^0(j^\pi = 0^+, T = 0), E = 17.64 \text{ MeV}$$

$$^8\text{Be}^*(j^\pi = 1^+, T = 0^*) \rightarrow ^8\text{Be}^0(j^\pi = 0^+, T = 0), E = 18.15 \text{ MeV}$$

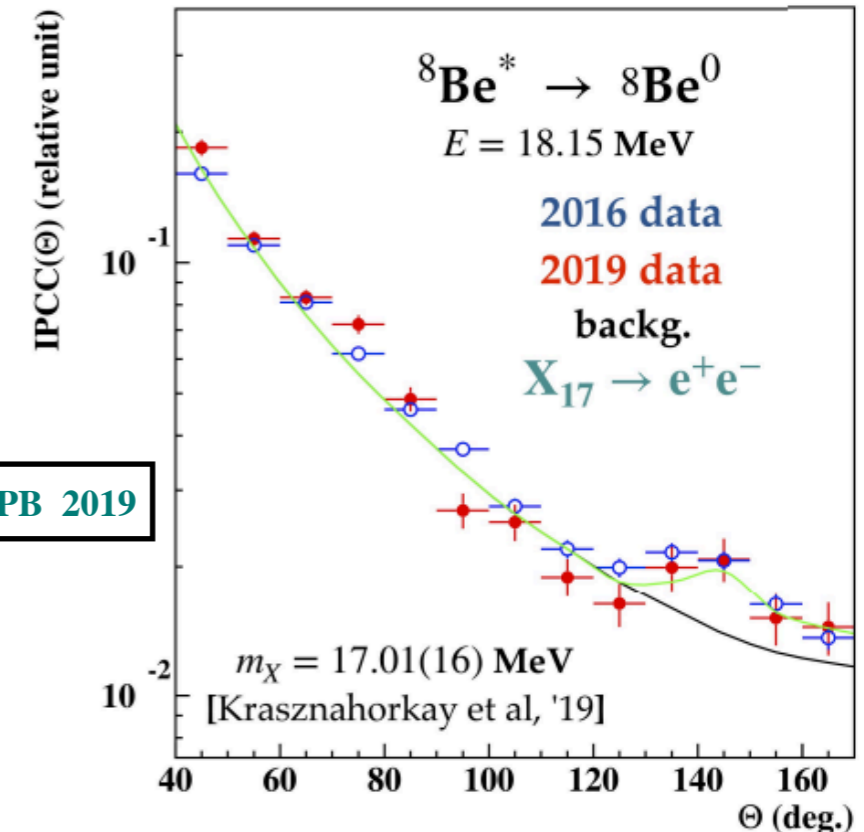
Resonance observed in isospin conserving transition
but absent in isospin violating one!

Best fit for the **isospin conserving** transition: Krasznahorkay et al APPB 2019

$$m_X = 17.01(16) \text{ MeV}$$

$$\Gamma_X/\Gamma_\gamma = 6(1) \times 10^{-6}$$

***Isospin mixing can affect these fit values



Similar anomaly in e^+e^- angular correlation of ^4He ($0^- \rightarrow 0^+$, 21.01 MeV decay) @ 7.2σ

Anomaly in ^8Be nuclear transition: suspects

$$^8\text{Be}^{*'}(j^\pi = 1^+, T = 1^*) \rightarrow ^8\text{Be}^0(j^\pi = 0^+, T = 0), E = 17.64 \text{ MeV}$$

$$^8\text{Be}^*(j^\pi = 1^+, T = 0^*) \rightarrow ^8\text{Be}^0(j^\pi = 0^+, T = 0), E = 18.15 \text{ MeV}$$

Possible candidates for X_{17} :

★ **Light scalar resonance** \Rightarrow would violate angular momentum conservation in $1^+ \rightarrow 0^+$ transition

★ **Light pseudo-scalar**: minimal models already excluded in the required coupling range
can be partially circumvented in the presence of additional non-photonic couplings

Doebrich et al. JHEP 2016
Ellwanger et al. JHEP 2016

★ **Light vector**: severe constraints on couplings for the relevant mass range
(more details on next slides)

Feng et al. PRL 2016; PRD 2017; 2020

★ **Light axial vector**: possible, requires ab-initio computation for the relevant form factors

Kozaczuk et al PRD 2017

○ Other exotic possibilities explored range from open string QED mesons to “4 bare quarks” interpretation

Couplings of the new vector boson for ${}^8\text{Be}$

A new Z' NC can be parametrised with effective couplings: $J_{Z'}^\mu = e\bar{\psi}_i\gamma^\mu(\varepsilon_{ij}^V + \gamma^5\varepsilon_{ij}^A)\psi_j$

in the simple case of purely vector quark current; the isospin conserving limit gives

$$\frac{\Gamma({}^8\text{Be}^* \rightarrow {}^8\text{Be} + Z')}{\Gamma({}^8\text{Be}^* \rightarrow {}^8\text{Be} + \gamma)} \simeq (\varepsilon_p^V + \varepsilon_n^V)^2 \left[1 - \left(\frac{m_{Z'}}{18.15 \text{ MeV}} \right)^2 \right]^{\frac{3}{2}}$$

$$\begin{aligned} \varepsilon_p^V &\simeq 2\varepsilon_{uu}^V + \varepsilon_{dd}^V \\ \varepsilon_n^V &\simeq \varepsilon_{uu}^V + 2\varepsilon_{dd}^V \end{aligned}$$

including isospin mixing effects à la Feng et.al.

leads to about 15% modification in allowed ranges

$$\frac{\Gamma({}^8\text{Be}^* \rightarrow {}^8\text{Be} + Z')}{\Gamma({}^8\text{Be}^* \rightarrow {}^8\text{Be} + \gamma)} \simeq |0.05(\varepsilon_p^V + \varepsilon_n^V) + 0.95(\varepsilon_p^V - \varepsilon_n^V)|^2 \left[1 - \left(\frac{m_{Z'}}{18.15 \text{ MeV}} \right)^2 \right]^{\frac{3}{2}}$$

$$\begin{aligned} &{}^8\text{Be}^{*'}(j^\pi = 1^+, T = 1^*) \rightarrow {}^8\text{Be}^0(j^\pi = 0^+, T = 0), \quad E = 17.64 \text{ MeV} \\ &{}^8\text{Be}^*(j^\pi = 1^+, T = 0^*) \rightarrow {}^8\text{Be}^0(j^\pi = 0^+, T = 0), \quad E = 18.15 \text{ MeV} \end{aligned}$$

the null results for the mostly isotriplet excited state require a kinematic suppression in the presence of isospin mixing => a larger preferred mass for the Z' to achieve the required phase space suppression

for a mass 17.5 MeV the normalised branching fraction fit can be as low as $\Gamma_{Z'}/\Gamma_\gamma = 0.5 \times 10^{-6}$

Conservative range consistent with data:

$$|\varepsilon_n^V + \varepsilon_p^V| \simeq (2 - 15) \times 10^{-3} \sqrt{\text{BR}(Z' \rightarrow e^+e^-)^{-1}}$$

Couplings of the new vector boson for ${}^8\text{Be}$

$$J_{Z'}^\mu = e\bar{\psi}_i\gamma^\mu(\varepsilon_{ij}^V + \gamma^5\varepsilon_{ij}^A)\psi_j$$

$$|\varepsilon_n^V + \varepsilon_p^V| \simeq (2 - 15) \times 10^{-3} \sqrt{\text{BR}(Z' \rightarrow e^+e^-)^{-1}} \longleftarrow \text{from normalised branching fraction fit}$$

Z' should be sufficiently short lived for its decay to occur inside the Atomki spectrometer $\sim \mathcal{O}(\text{cm})$

$$\Gamma(Z' \rightarrow e^+e^-) = (|\varepsilon_{ee}^V|^2 + |\varepsilon_{ee}^A|^2) \frac{\lambda^{\frac{1}{2}}(m_{Z'}, m_e, m_e)}{24\pi m_{Z'}}$$

$$|\varepsilon_{ee}^V| \gtrsim 1.3 \times 10^{-5} \sqrt{\text{BR}(Z' \rightarrow e^+e^-)}$$

Atomic parity violation in Caesium

$$|\varepsilon_{ee}^A| \lesssim 2.6 \times 10^{-9}$$

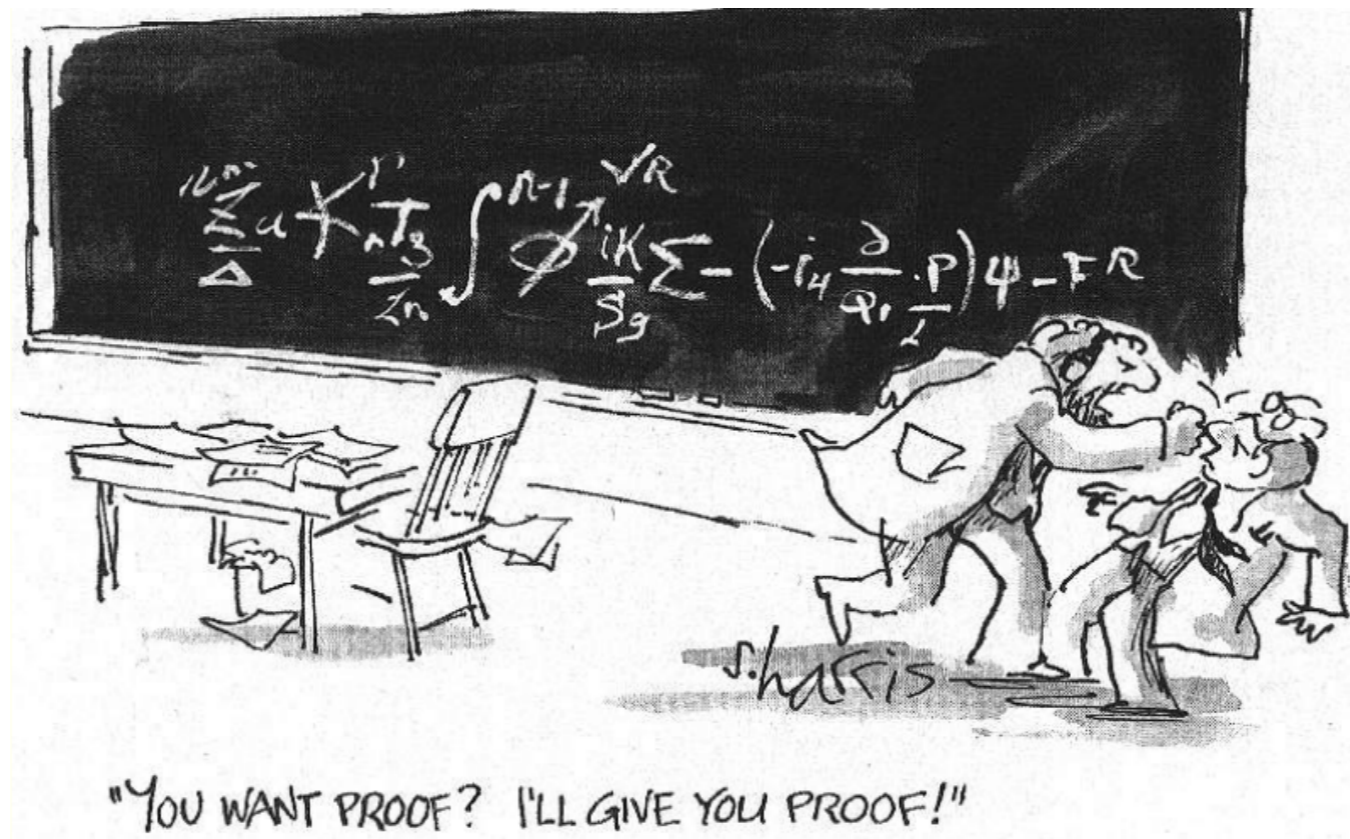
Can pure dark photon work as a solution?

NO, couplings due to kinetic mixing with photon: $\varepsilon_n^V = \varepsilon_\nu^V = 0$, $\varepsilon_p^V = -\varepsilon_{ee}^V$

NA48/2 bound for $\pi^0 \rightarrow \gamma A'$ leads to $|\varepsilon_p^V| \lesssim 1.2 \times 10^{-3}$ **X**

“protophobic” scenarios are preferred

After the experiments: which new physics model ?



A “prototype” extension of the SM: $U(1)_{B-L}$

Field	$SU(3)_c$	$SU(2)_L$	$U(1)_Y$	$U(1)_{B-L}$
$Q = (u_L, d_L)^T$	3	2	$\frac{1}{6}$	$\frac{1}{3}$
$\ell = (\nu_L, e_L)^T$	1	2	$-\frac{1}{2}$	-1
u_R	3	1	$\frac{2}{3}$	$\frac{1}{3}$
d_R	3	1	$-\frac{1}{3}$	$\frac{1}{3}$
e_R	1	1	-1	-1
h_{SM}	1	2	$\frac{1}{2}$	0
N_R	1	1	0	-1
$L_{L,R} = (L_{L,R}^0, L_{L,R}^-)^T$	1	2	$-\frac{1}{2}$	1
$E_{L,R}$	1	1	-1	1
h_X	1	1	0	2

New scalar singlet h_X : spontaneously breaks $U(1)_{B-L}$ below the EW scale giving a 17 MeV Z'

3 gen $\times N_R$: cancel the triangular gauge anomalies

3 gen \times (isodoublet + isosinglet) vector-like lepton: provides non-universality to new charged lepton NC

also plays an essential role in cancelling the NC interaction of neutrinos to Z'

A “prototype” extension of the SM: $U(1)_{B-L}$

Natural type-I seesaw mass

$$\mathcal{L}_{\text{Yuk.}} \supseteq -y_\ell^{ij} h_{\text{SM}} \bar{\ell}_L^i e_R^j + y_\nu^{ij} \tilde{h}_{\text{SM}} \bar{\ell}_L^i N_R^j - \frac{1}{2} y_M^{ij} h_X \bar{N}_R^{ic} N_R^j$$

$U(1)_{B-L}$ is kinetically mixed with the $U(1)_Y$

$$\mathcal{L}_{\text{kin}}^{\text{gauge}} \supseteq -\frac{1}{4} \tilde{F}_{\mu\nu} \tilde{F}^{\mu\nu} - \frac{1}{4} \tilde{F}'_{\mu\nu} \tilde{F}'^{\mu\nu} + \frac{\epsilon_k}{2} \tilde{F}_{\mu\nu} \tilde{F}'^{\mu\nu}$$

Field	SU(3) _c	SU(2) _L	U(1) _Y	U(1) _{B-L}
$Q = (u_L, d_L)^T$	3	2	$\frac{1}{6}$	$\frac{1}{3}$
$\ell = (\nu_L, e_L)^T$	1	2	$-\frac{1}{2}$	-1
u_R	3	1	$\frac{2}{3}$	$\frac{1}{3}$
d_R	3	1	$-\frac{1}{3}$	$\frac{1}{3}$
e_R	1	1	-1	-1
h_{SM}	1	2	$\frac{1}{2}$	0
N_R	1	1	0	-1
$L_{L,R} = (L_{L,R}^0, L_{L,R}^-)^T$	1	2	$-\frac{1}{2}$	1
$E_{L,R}$	1	1	-1	1
h_X	1	1	0	2

=> mass mixing between $U(1)_{B-L}$ boson and W^3 with $\tan 2\theta' \simeq -2 \frac{\epsilon_k}{\sqrt{1 - \epsilon_k^2}} \sin \theta_w$

Diagonalising kinetic and mass mixing gives physical (gauge) couplings (at leading order):

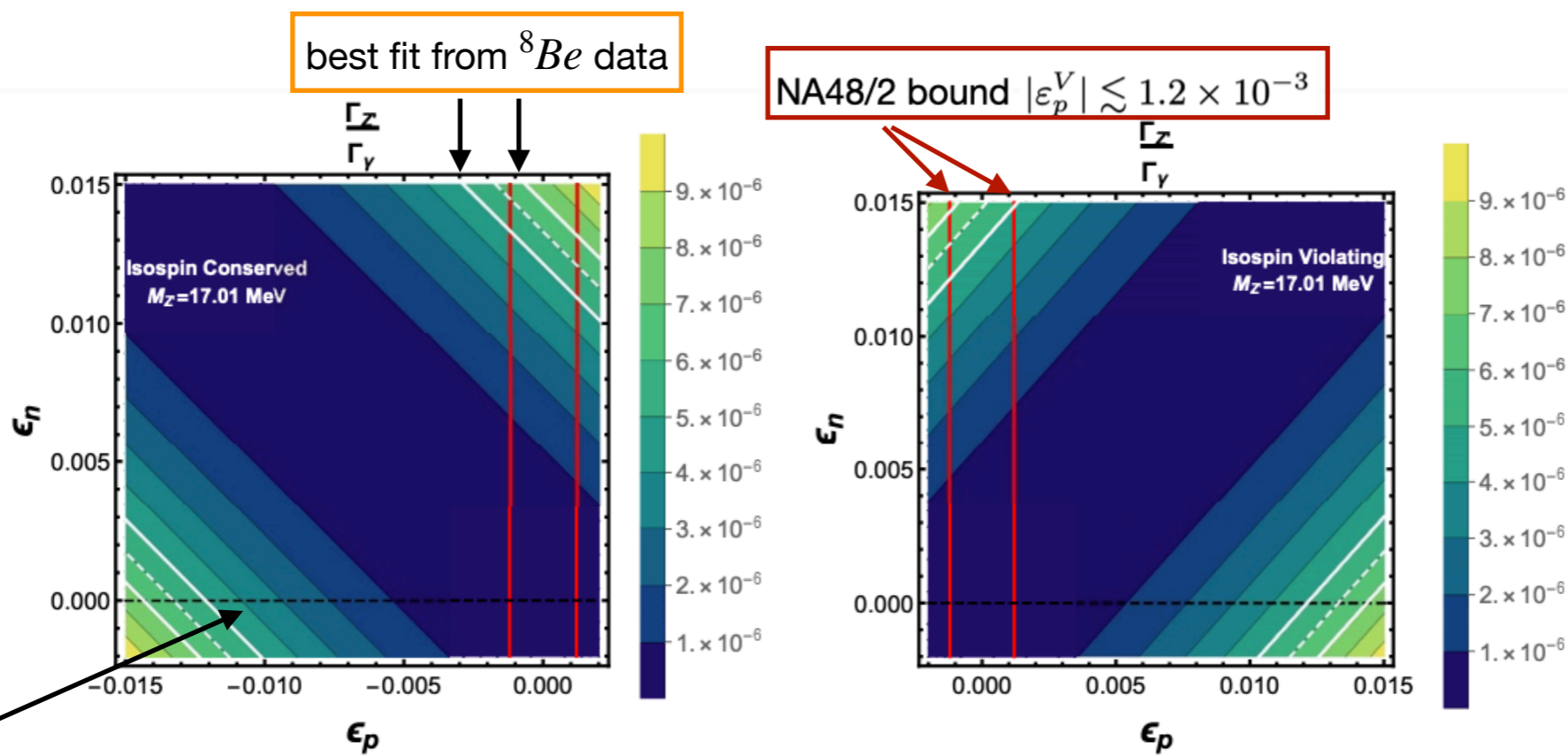
$$D_\mu \simeq \partial_\mu + \dots + i \frac{g}{\cos \theta_w} (T_3 f - \sin^2 \theta_w Q_f) Z_\mu + ie Q_f A_\mu + ie (\epsilon Q_f + \epsilon_{B-L} Q_f^{B-L}) Z'_\mu$$

with $\epsilon = \frac{\epsilon_k \cos \theta_w}{\sqrt{1 - \epsilon_k^2}}$ and $\epsilon_{B-L} = \frac{g_{B-L}}{e \sqrt{1 - \epsilon_k^2}}$

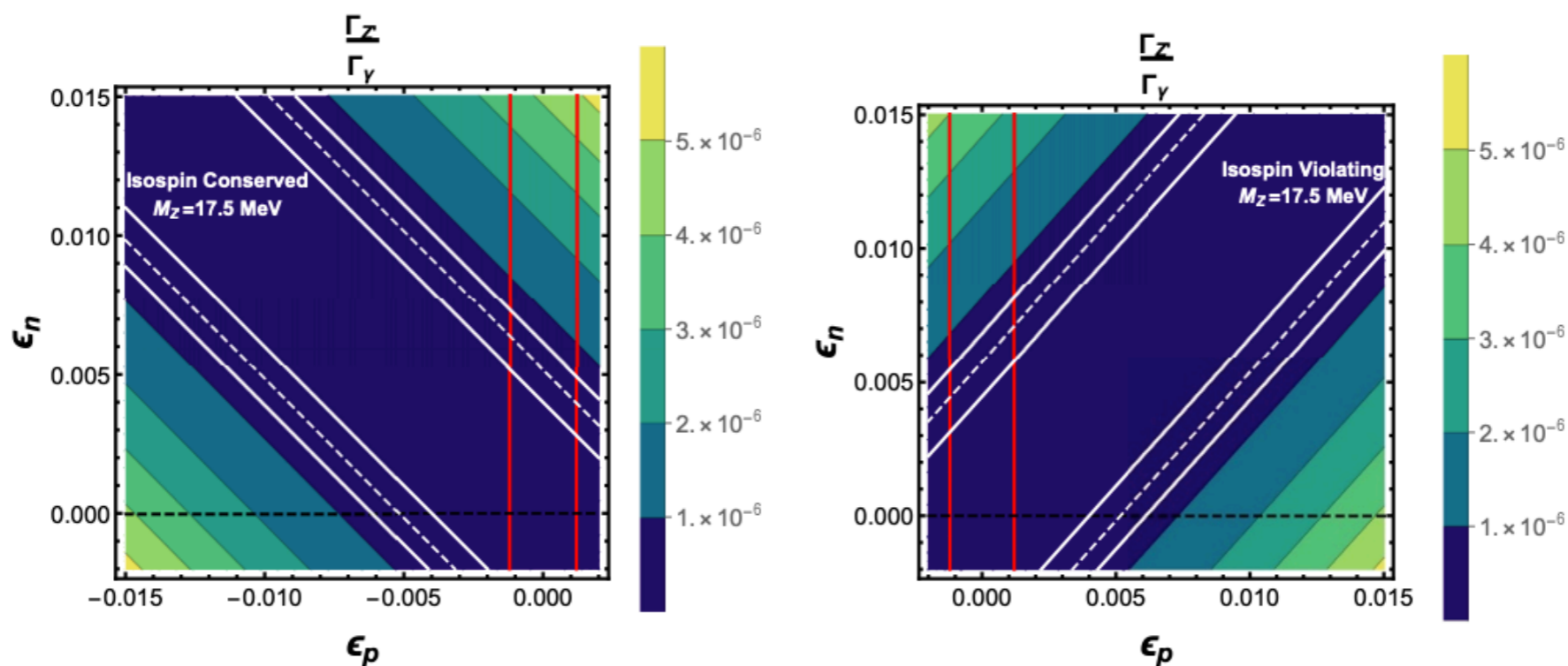
Nucleon couplings and mass: $\epsilon_p^V = \epsilon_{B-L} - \epsilon$, $\epsilon_n^V = \epsilon_{B-L}$, $m_{Z'}^2 \simeq 4\epsilon_{B-L}^2 v_X^2$

But also: $\epsilon_{\nu\nu}^A = -\epsilon_n^V$ neutrino coupling too large **XXX** more in a few slides

^8Be data and coupling to nucleons



Dark photon



$$2 \times 10^{-3} \lesssim |\epsilon_n^V| \lesssim 15 \times 10^{-3}$$

$$|\epsilon_p^V| \lesssim 1.2 \times 10^{-3}$$

${}^8\text{Be}$ data and coupling to leptons

Direct searches: negative results @ electron beam dump NA64

negligible production

$$\boxed{\epsilon_{ee}^{V2} + \epsilon_{ee}^{A2} < 1.1 \times 10^{-16}}$$

or

decay inside the beam dump

$$\boxed{\sqrt{|\epsilon_{ee}^V|^2 + |\epsilon_{ee}^A|^2} \gtrsim \frac{6.8 \times 10^{-4}}{\sqrt{\text{BR}(Z' \rightarrow e^+e^-)}}$$

Tight constraints from neutrino-electron scattering:

For LFU couplings and Dirac ν :

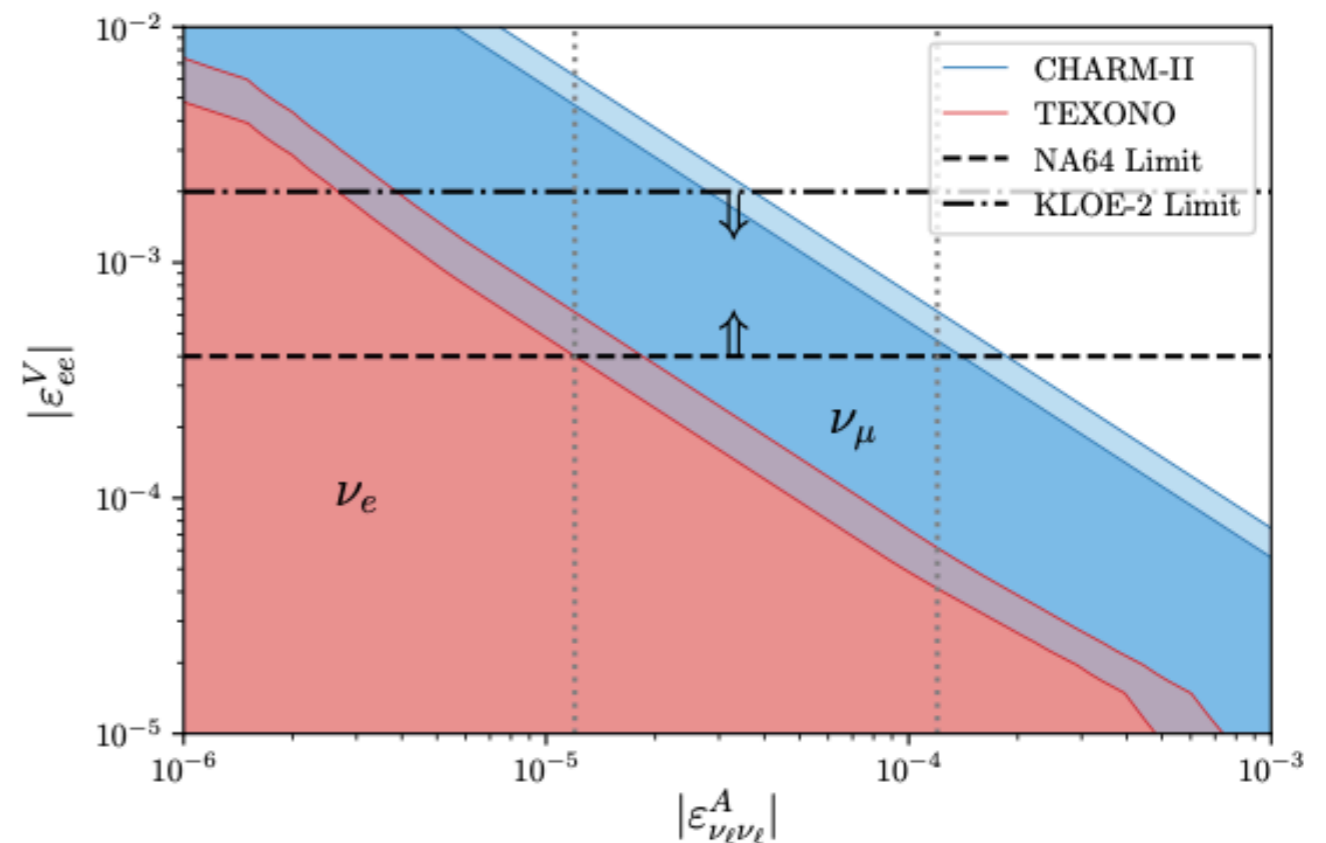
$$\sqrt{|\epsilon_{ee}^V \epsilon_{\nu\ell\nu\ell}^V|} < 7 \times 10^{-5} \quad \boxed{\text{Feng et al. PRD 2017}}$$

For Majorana ν the vector current is vanishing
requires new fit !

CHARM-II $\Rightarrow \nu_\mu - e$ scattering

TEXONO $\Rightarrow \nu_e - e$ scattering

$$\begin{aligned} |\epsilon_{\nu_e\nu_e}^A| &\lesssim 1.2 \times 10^{-5} \quad \& \\ |\epsilon_{\nu_\mu\nu_\mu}^A| &\lesssim 12.2 \times 10^{-5} \end{aligned}$$



But, we have seen that with SM fermion content

$$\boxed{\epsilon_{\nu\nu}^A = -\epsilon_n^V}$$

CH, Kriewald, Orloff, Teixeira JHEP 2020

Solution: Add 3 gens. of **vector-like** lepton doublets

mass mixing of L^0 with ν_L can arrange cancellations to give an acceptably small $\epsilon_{\nu\nu}^A$

$$\mathcal{L}_{\text{Yuk.}} \supseteq -y_\ell^{ij} h_{\text{SM}} \bar{\ell}_L^i e_R^j + y_\nu^{ij} \tilde{h}_{\text{SM}} \bar{\ell}_L^i N_R^j - \frac{1}{2} y_M^{ij} h_X \bar{N}_R^{i,c} N_R^j - \lambda_L^{ij} h_X \bar{\ell}_L^i L_R^j - M_L^{ij} \bar{L}_L^i L_R^j$$

- λ_L^{ij} needs to be (almost) diagonal to comply with **LFV** bounds: $\lambda_L^{ij} \rightarrow \lambda_{L\alpha}$
- M_L^{ij} can be chosen to be diagonal; **collider bounds:** mass scale ~ 100 GeV

$$\Rightarrow Z' \text{-}\nu\nu\text{-couplings get modified: } \epsilon_{\nu_\alpha \nu_\alpha} \simeq \epsilon_{B-L} \left(1 - \frac{\lambda_{L\alpha}^2 v_X^2}{M_{L\alpha}^2} \right)$$

$$\Rightarrow \lambda_{L\alpha}^2 v_X^2 \simeq M_{L\alpha}^2 \text{ is fixed for each lepton generation } \alpha !$$

But now the charged component of L mixes with left-handed SM charged leptons, but the right handed couplings remain unmodified

$$g_{Z',L}^{l_\alpha l_\alpha} \simeq -\epsilon + \left(\frac{\lambda_{L\alpha}^2 v_X^2}{M_{L\alpha}^2} - 1 \right) \epsilon_{B-L}$$

$$\epsilon_n^V = \epsilon_{B-L}$$

in conflict with

$$\text{Atomic parity violation in Caesium } |\epsilon_{ee}^A| \lesssim 2.6 \times 10^{-9}$$

Solution: Add 3 gens. of **vector-like** lepton isosinglets

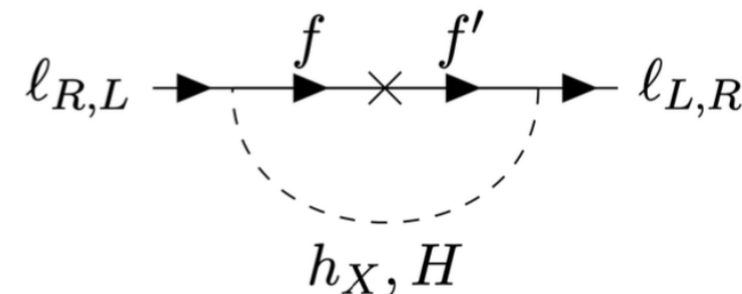
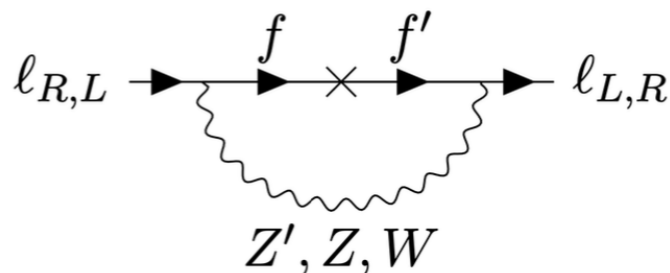
$$\mathcal{L}_{\text{Yuk.}} \supseteq -y_\ell^{ij} h_{\text{SM}} \bar{\ell}_L^i e_R^j + y_\nu^{ij} \tilde{h}_{\text{SM}} \bar{\ell}_L^i N_R^j - \frac{1}{2} y_M^{ij} h_X \bar{N}_R^{ic} N_R^j - \lambda_L^{ij} h_X \bar{\ell}_L^i L_R^j - M_L^{ij} \bar{L}_L^i L_R^j$$

$$- \lambda_E^{ij} h_X \bar{E}_L^i e_R^j - M_E^{ij} \bar{E}_L^i E_R^j - h^{ij} h_{\text{SM}} \bar{L}_L^i E_R^j + k^{ij} \tilde{h}_{\text{SM}} \bar{E}_L^i L_R^j$$

$$\Rightarrow \varepsilon_{l_\alpha l_\alpha}^A \simeq \frac{1}{2} \left(\frac{\lambda_{E\alpha}^2 v_X^2}{M_{E\alpha}^2} - \frac{\lambda_{L\alpha}^2 v_X^2}{M_{L\alpha}^2} \right) \varepsilon_{B-L} \Rightarrow \lambda_{E\alpha} \text{ is fixed for the 1. gen!}$$

$$\Rightarrow \varepsilon_{l_\alpha l_\alpha}^V \simeq -\varepsilon + \frac{1}{2} \left(\frac{\lambda_{L\alpha}^2 v_X^2}{M_{L\alpha}^2} + \frac{\lambda_{E\alpha}^2 v_X^2}{M_{E\alpha}^2} - 2 \right) \varepsilon_{B-L} \Rightarrow \text{fixes } \varepsilon \simeq -(8 - 20) \times 10^{-4}$$

\Rightarrow 2 new Yuk. matrices h^{ij} and k^{ij} (assumed to be diagonal): if different, their asymmetry will generate axial and pseudo-scalar couplings in $Z' - \ell L$ and $h_X - \ell L$ interactions

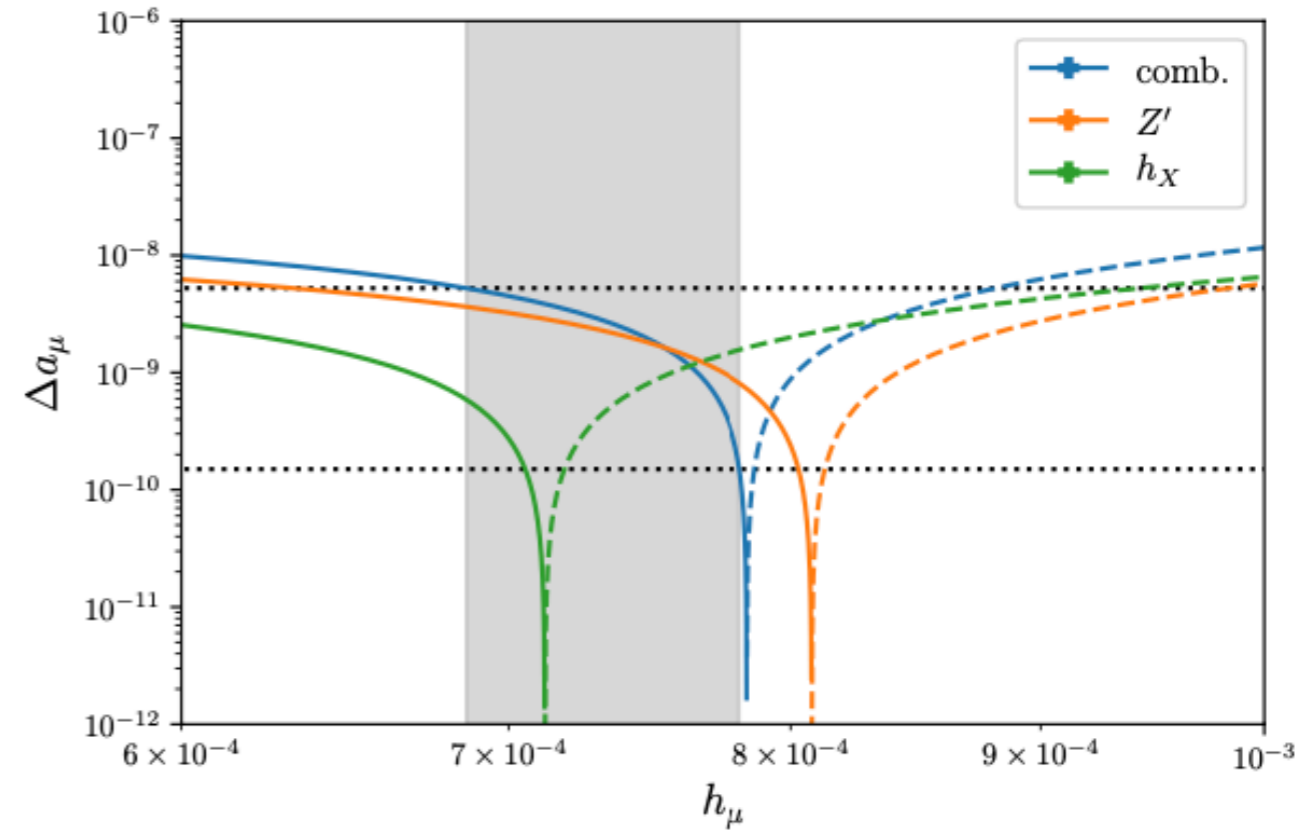
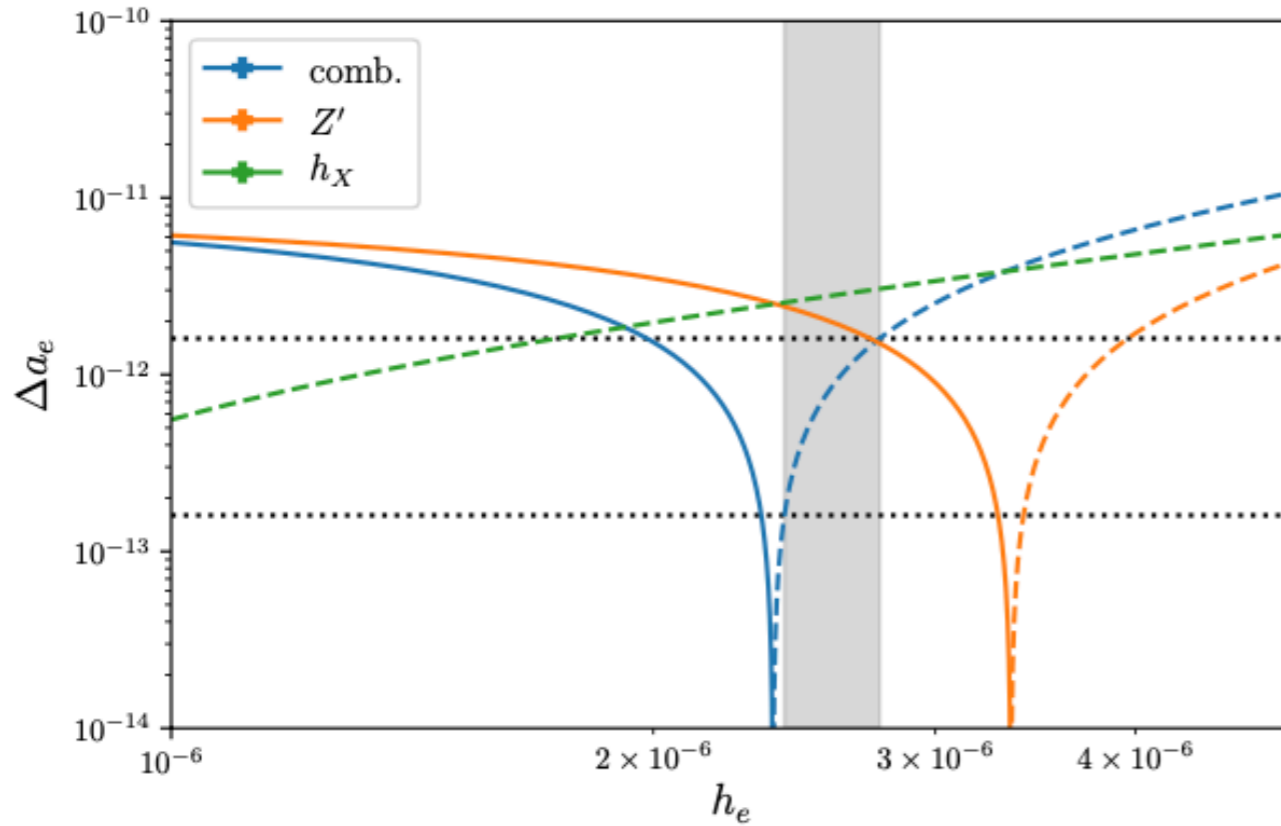


- Dominant contributions by Z' and h_X
- Mass-insertion $\propto h_\alpha$ and $\propto k_\alpha$

- Loop-functions for scalar/pseudo-scalar and vector/axial couplings have opposite sign

Explaining $(g - 2)_\mu$ and $(g - 2)_e$ simultaneously

CH, Kriewald, Orloff, Teixeira JHEP 2020



- $M_E = M_L \simeq 90 \text{ GeV}$, $\lambda_L = \lambda_E = M_L/v_X (\simeq 6.4)$, $m_{h_X} \simeq 70 \text{ GeV}$,
 $\varepsilon_{B-L} = 2 \times 10^{-3}$, $\varepsilon = -8 \times 10^{-4}$, $k_e = k_\mu = 10^{-7}$

Dashed lines: change of sign when pseudo-scalar contribution larger than scalar and/or axial larger than vector

Parameter space and predictability of the model

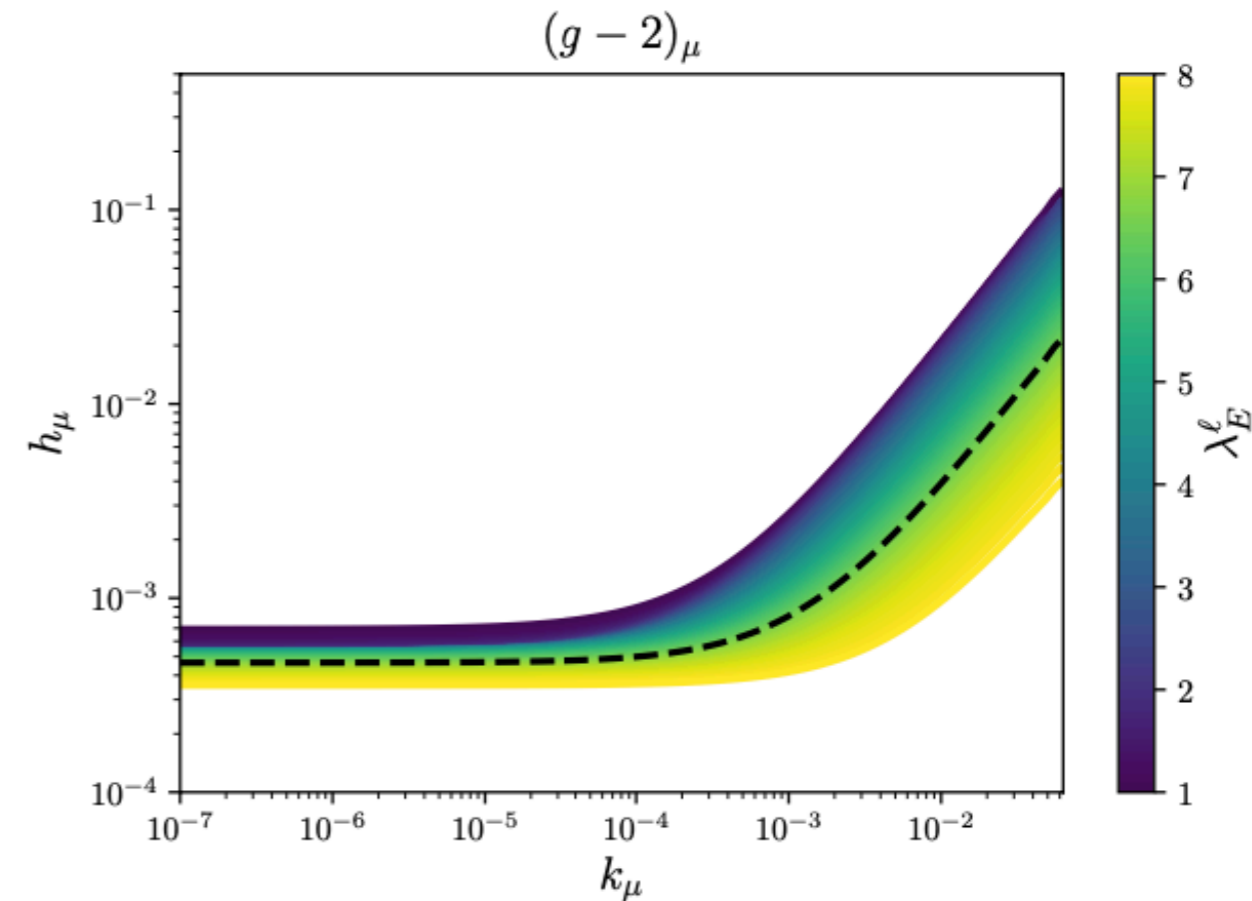
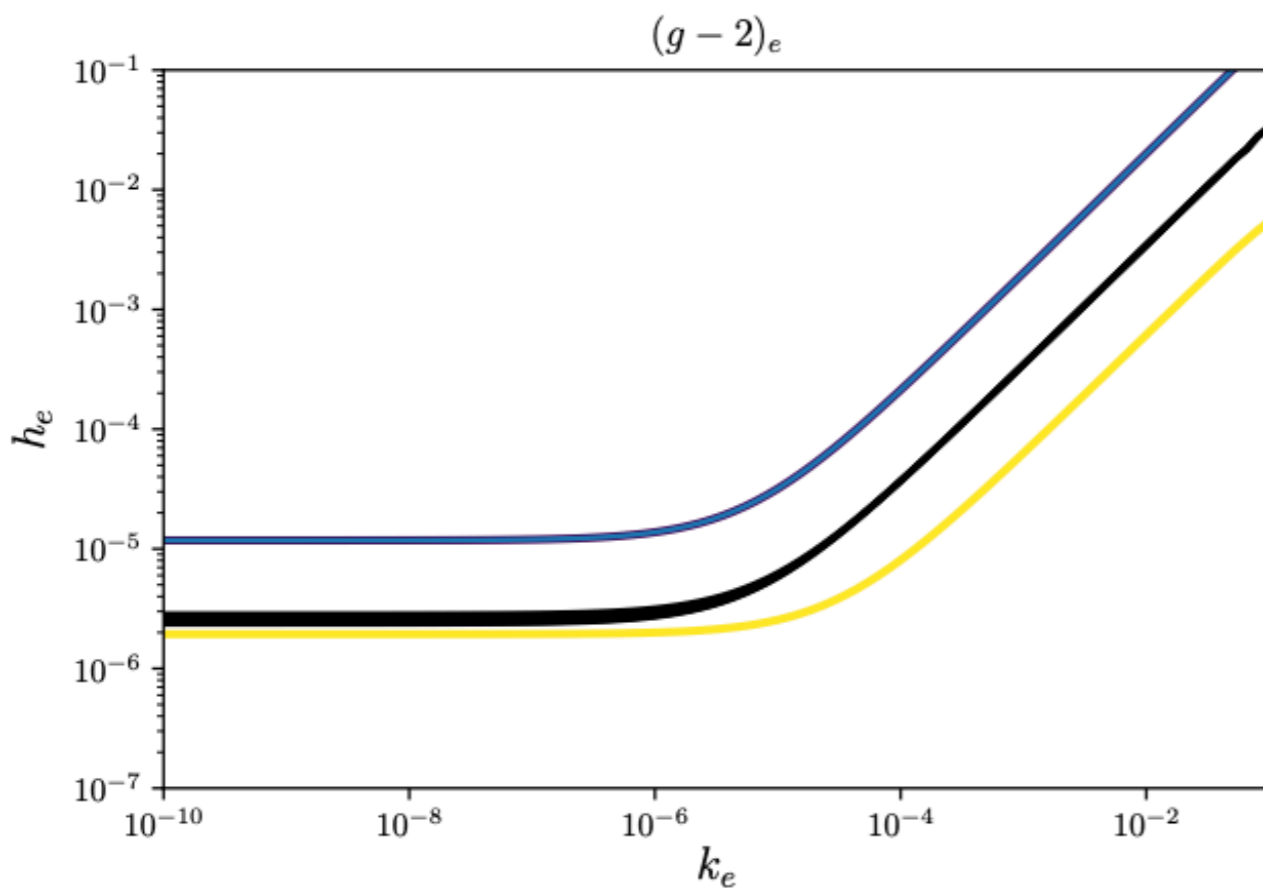
To explain ${}^8\text{Be}$:

$$\begin{aligned}
 2 \times 10^{-3} &\lesssim |\varepsilon_n^V| \lesssim 15 \times 10^{-3}, \\
 |\varepsilon_p^V| &\lesssim 1.2 \times 10^{-3}, \\
 0.68 \times 10^{-3} &\lesssim |\varepsilon_{ee}^V| \lesssim 2 \times 10^{-3}, \\
 |\varepsilon_{ee}^A| &\lesssim 2.6 \times 10^{-9}, \\
 |\varepsilon_{\nu_e \nu_e}^A| &\lesssim 7.8 \times 10^{-6}, \\
 |\varepsilon_{\nu_\mu \nu_\mu}^A| &\lesssim 8.4 \times 10^{-5}.
 \end{aligned}$$



$$\begin{aligned}
 v_X &\lesssim 14 \text{ GeV} & m_{Z'} \approx m_{B'} &= 2e |\varepsilon_{B-L}| v_X \\
 \varepsilon_{B-L} &= 0.002 & |\varepsilon_n^V| &= |\varepsilon_{B-L}| \\
 -0.002 &\lesssim \varepsilon \lesssim -0.0008 & |\varepsilon_p^V| &= |\varepsilon + \varepsilon_{B-L}| \\
 \left| 1 - \frac{\lambda_L^2 v_X^2}{M_L^2} \right| &\lesssim 0.01 & \left| \frac{\lambda_E^2 v_X^2}{M_E^2} - \frac{\lambda_L^2 v_X^2}{M_L^2} \right| &\lesssim 2.6 \times 10^{-6}
 \end{aligned}$$

CH, Kriewald, Orloff, Teixeira JHEP 2020



- Black line: $(g-2)_e$ explained ✓ coloured region: $(g-2)_\mu$ explained ✓✓

Concluding remarks



Currently many “tensions” with SM hosted in lepton-related observables

We have discussed three of such tensions in detail in the context of a simple prototype $U(1)_{B-L}$ extension

Light vector candidates to explain ^8Be is an exciting new physics possibility

Potential to address the lepton anomalous magnetic moments in simple NP extensions

Constrained parameter space: experimental bounds, ^8Be & $\Delta a_\mu \Rightarrow$ “predict” Δa_e

Exciting near-future @ “experimental” front!

FNAL update on $(g - 2)_\mu$ expected soon!

NA64 is getting ready to hunt down the X17 boson at the CERN SPS

2009.02756

Thank you for your attention!

Backup-I

$$\begin{pmatrix} A^\mu \\ Z^\mu \\ Z'^\mu \end{pmatrix} = \begin{pmatrix} \cos \theta_w & \sin \theta_w & 0 \\ -\sin \theta_w \cos \theta' & \cos \theta_w \cos \theta' & \sin \theta' \\ \sin \theta_w \sin \theta' & -\cos \theta_w \sin \theta' & \cos \theta' \end{pmatrix} \begin{pmatrix} B^\mu \\ W_3^\mu \\ B'^\mu \end{pmatrix}$$

$$\tan 2\theta' = \frac{2 \varepsilon' g' \sqrt{g^2 + g'^2}}{\varepsilon'^2 g'^2 + 4 m_{B'}^2 / v^2 - g^2 - g'^2}$$

$$M_A = 0, \quad M_{Z, Z'} = \frac{g}{\cos \theta_w} \frac{v}{2} \left[\frac{1}{2} \left(\frac{\varepsilon'^2 + 4 m_{B'}^2 / v^2}{g^2 + g'^2} + 1 \right) \mp \frac{g' \cos \theta_w \varepsilon'}{g \sin 2\theta'} \right]^{\frac{1}{2}}$$

Backup-II

$$\mathcal{L}_{\text{mass}}^\ell = (\bar{e}_L \bar{L}_L^- \bar{E}_L) \cdot M_\ell \cdot \begin{pmatrix} e_R \\ L_R^- \\ E_R \end{pmatrix} = (\bar{e}_L \bar{L}_L^- \bar{E}_L) \begin{pmatrix} y \frac{v}{\sqrt{2}} & \lambda_L \frac{v_X}{\sqrt{2}} & 0 \\ 0 & M_L & h \frac{v}{\sqrt{2}} \\ \lambda_E \frac{v_X}{\sqrt{2}} & k \frac{v}{\sqrt{2}} & M_E \end{pmatrix} \begin{pmatrix} e_R \\ L_R^- \\ E_R \end{pmatrix}$$

$$M_\ell^{\text{diag}} = U_L^\dagger M_\ell U_R$$

$$U_L = \begin{pmatrix} 1 - \frac{\lambda_L^2 v_X^2}{4M_L^2} & \frac{\lambda_L v_X}{\sqrt{2}M_L} - \frac{\lambda_L^3 v_X^3}{4\sqrt{2}M_L^3} & \frac{(k\lambda_L M_E + h\lambda_L M_L + \lambda_E M_E y) v v_X}{2M_E^3} \\ \frac{\lambda_L^3 v_X^3}{4\sqrt{2}M_L^3} - \frac{\lambda_L v_X}{\sqrt{2}M_L} & 1 - \frac{\lambda_L^2 v_X^2}{4M_L^2} & \frac{(kM_E M_L + h(M_E^2 + M_L^2))v}{\sqrt{2}M_E^3} \\ \frac{(h\lambda_L M_E - \lambda_E M_L y) v v_X}{4M_E^3} & -\frac{(kM_E M_L + h(M_E^2 + M_L^2))v}{\sqrt{2}M_E^3} & 1 \end{pmatrix}$$

$$U_R = \begin{pmatrix} 1 - \frac{\lambda_E^2 v_X^2}{4M_E^2} & \frac{\lambda_L v v_X}{2M_L^2} - \frac{\lambda_E (kM_E M_L + h(M_E^2 + M_L^2)) v v_X}{2M_E^3 M_L} & \frac{\lambda_E v_X}{\sqrt{2}M_E} - \frac{\lambda_E^3 v_X^3}{4\sqrt{2}M_E^3} \\ \frac{(h\lambda_E M_L - \lambda_L M_E y) v v_X}{2M_E M_L^2} & 1 & \frac{(hM_E M_L + k(M_E^2 + M_L^2))v}{\sqrt{2}M_E^3} \\ \frac{\lambda_E^3 v_X^3}{4\sqrt{2}M_E^3} - \frac{\lambda_E v_X}{\sqrt{2}M_E} & -\frac{(hM_E M_L + k(M_E^2 + M_L^2))v}{\sqrt{2}M_E^3} & 1 - \frac{\lambda_E^2 v_X^2}{4M_E^2} \end{pmatrix}$$

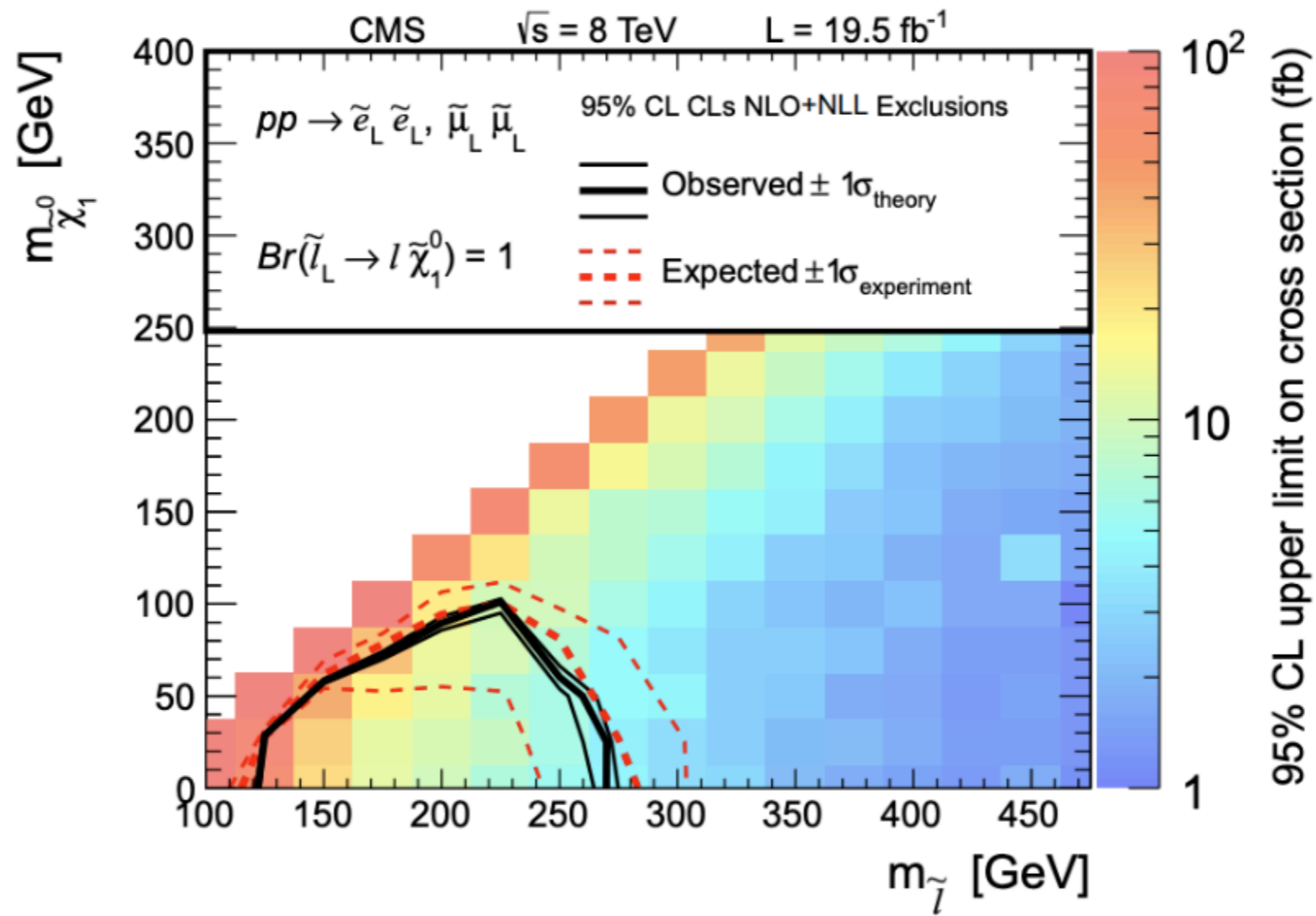
Backup-III

$$\begin{aligned}
 \mathcal{L}_{\text{mass}}^\nu &= \left(\nu^T \ N^c T \ L^{0T} \ L^{0cT} \right)_L C^{-1} \cdot M_\nu \cdot \begin{pmatrix} \nu \\ N^c \\ L^0 \\ L^{0c} \end{pmatrix}_L \\
 &= \left(\nu^T \ N^c T \ L^{0T} \ L^{0cT} \right)_L C^{-1} \begin{pmatrix} 0 & y_\nu \frac{v}{\sqrt{2}} & 0 & \lambda_L \frac{v_X}{\sqrt{2}} \\ y_\nu \frac{v}{\sqrt{2}} & y_M \frac{v_X}{\sqrt{2}} & 0 & 0 \\ 0 & 0 & 0 & M_L \\ \lambda_L \frac{v_X}{\sqrt{2}} & 0 & M_L & 0 \end{pmatrix} \begin{pmatrix} \nu \\ N^c \\ L^0 \\ L^{0c} \end{pmatrix}_L
 \end{aligned}$$

$$M_\nu^{\text{diag}} = \tilde{U}_\nu^T M_\nu \tilde{U}_\nu,$$

$$\tilde{U}_\nu = \begin{pmatrix} 1 - \frac{\lambda_L^2 v_X^2}{4M_L^2} - \frac{v^2 y_\nu^2}{2v_X^2 y_M^2} & \frac{v y_\nu}{v_X y_M} & \frac{\lambda_L v_X}{2M_L} & \frac{\lambda_L v_X}{2M_L} \\ -\frac{v y_\nu}{v_X y_M} & 1 - \frac{v^2 y_\nu^2}{2v_X^2 y_M^2} & 0 & 0 \\ -\frac{\lambda_L v_X}{\sqrt{2}M_L} & -\frac{\lambda_L v y_\nu}{\sqrt{2}M_L y_M} & \frac{1}{\sqrt{2}} & -\frac{\lambda_L^2 v_X^2}{4\sqrt{2}M_L^2} \\ 0 & 0 & -\frac{1}{\sqrt{2}} & \frac{1}{\sqrt{2}} \end{pmatrix}$$

Backup-IV



Recast searches for slepton/neutralino pair production: $h_X \rightarrow \tilde{\chi}^0$, $E, L \rightarrow \tilde{l}$